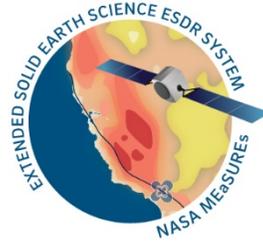


**Extended Solid Earth Science ESDR System (ES<sup>3</sup>):  
Algorithm Theoretical Basis Document (ATBD)**

**October 7, 2021**

**MEaSURES ROSES-17**



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**MEaSURES Web Pages**

<http://sopac-csrc.ucsd.edu/index.php/measures-2/>

**MGViz: Map and GNSS Products Visualization**

<http://geoapp20.ucsd.edu/?mission=ESESES>

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## 1. Overview

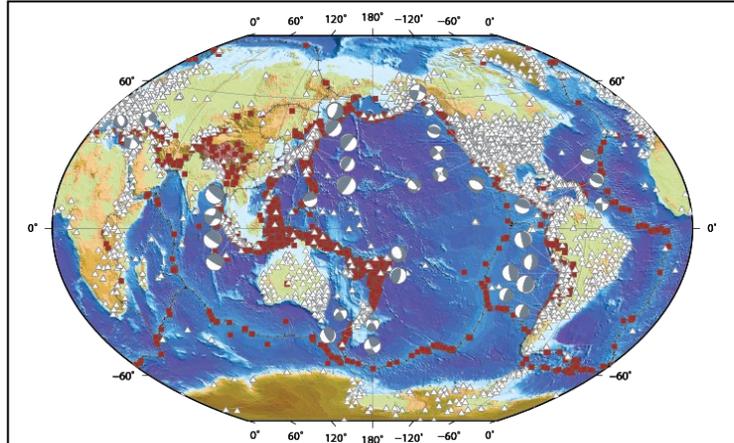
Since its inception in the early 1980's, GPS/GNSS geodesy has contributed to a wide range of scientific and societal applications including tectonic motion, crustal deformation, natural and anthropogenic processes and hazards, including earthquakes, tsunamis, volcanoes, the cryosphere, extreme weather, sea level rise, climate change and hydrology. Our project “Extended Solid Earth Science ESDR System” (ESESES), a continuation and expansion of the MEaSUREs “Solid Earth Science ESDR System” (SESES)

project (2012-2018), provides the basic infrastructure, data and data products for these applications. It is a collaborative effort of the Jet Propulsion Laboratory (JPL) and Scripps Institution of Oceanography (SIO) and its Scripps Orbit and Permanent Array Center (SOPAC). The Earth Science Data Records (ESDRs) from SESES (Table 1, items 1.1-1.5) now span thirty years for the earliest stations and are now available for thousands of global and regional continuous GPS stations (Figure 1). These ESDRs will continue to be generated for a significantly expanded list of stations. In ESESES we will

provide four new ESDRs (Table 1, items 2.1-2.3): (1) continuous high-rate (1 Hz) geodetic (GNSS) and seismogeodetic displacement records for historical earthquakes, (2) slow slip events (SSEs) and other transients, (3) weekly displacement and strain rate grids, and (4) total near-surface water content over the continental U.S. We will exploit technological developments including GPS modernization, multiple satellite constellations (GNSS) and new processing methods.

The purpose of this document is to describe the data products and the theoretical basis for their generation.

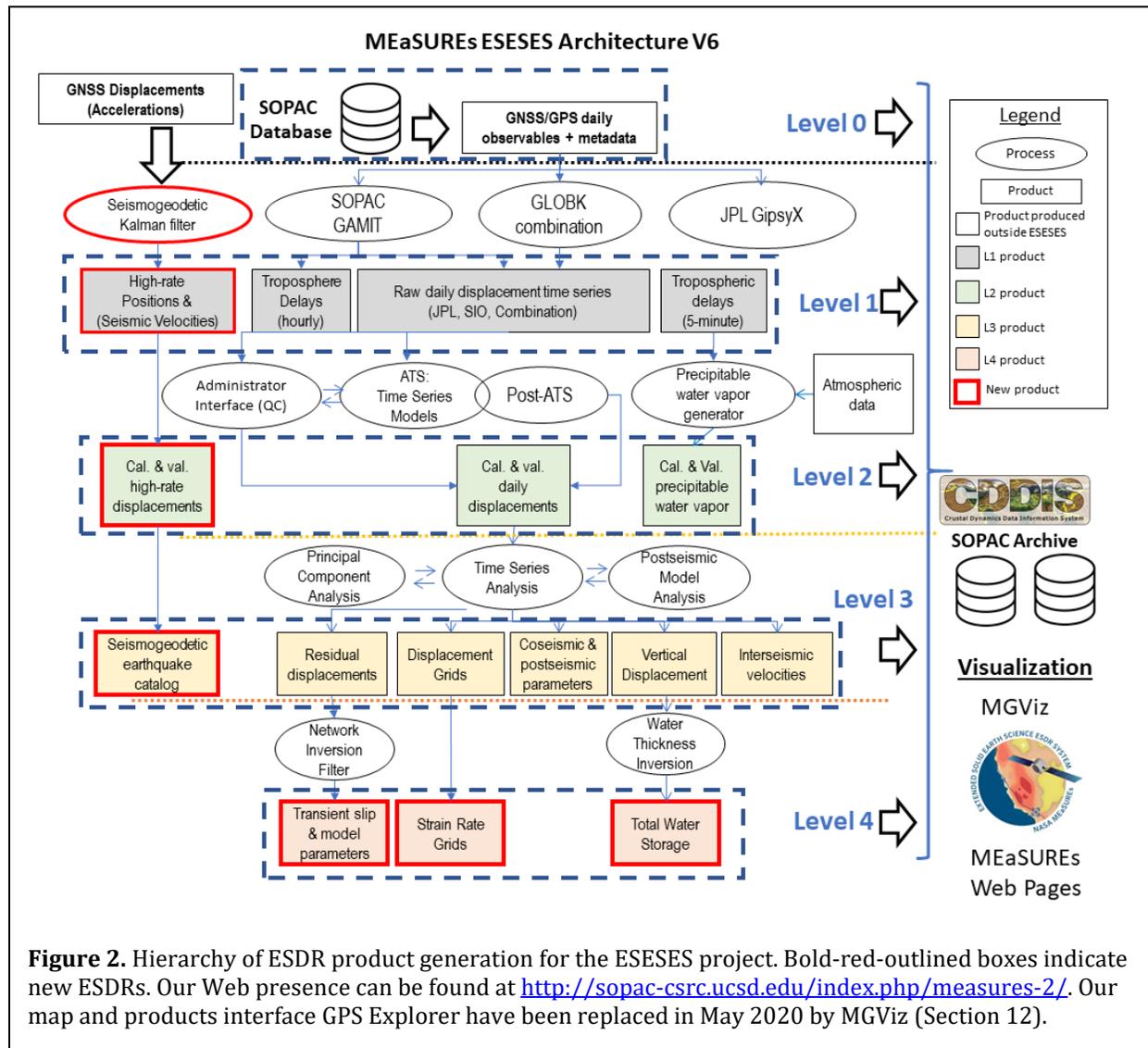
The ESDRs for the project (Table 1) are produced using the processes captured schematically in the flow diagram (Figure 2). They begin with the production of two Level 1 products: (1) long-term daily and continuous raw displacement time series that are generated using identical GNSS observations (carrier phase and pseudorange) and metadata stored in a unified database maintained at SOPAC. The JPL and SIO displacement time series are generated using independent processing strategies and software: the GipsyX Network Processor (NWPx) and GAMIT/GLOBK software,



**Figure 1.** The project is adding new ESDRs (Table 1) to enhance geographical coverage with hundreds of additional GNSS stations (white triangles) focusing on tectonic plate boundaries (black lines) for crustal deformation and natural hazards applications, and the continental U.S. for near-surface water content. Shown are earthquakes greater than magnitude 5 (brown squares) since 1990 with their global centroid moment tensor (CMT) solutions.

respectively; (2) troposphere delay estimates at two intervals (5 and 60 minutes at JPL and 60 minutes at SIO); and (3) high-rate GNSS and seismogeodetic (GNSS + accelerometer data) waveforms at SIO. Level 2 ESDRs include calibrated and validated ESDRs, (1) daily combined displacement time series (Figure 3) that underly the generation of higher-level ESDRs<sup>1</sup>; (2) troposphere and precipitable water time series at 5-minute intervals by JPL; and (3) high-rate displacement and seismic velocity waveforms for historical earthquakes at SIO.

The Level 3 ESDRs are derivatives of Level 2, including, (1) estimated displacement time series



**Figure 2.** Hierarchy of ESDR product generation for the ESESES project. Bold-red-outlined boxes indicate new ESDRs. Our Web presence can be found at <http://sopac-csrc.ucsd.edu/index.php/measures-2/>. Our map and products interface GPS Explorer have been replaced in May 2020 by MGViz (Section 12).

parameters (residuals, coseismic and postseismic, interseismic velocities and vertical

<sup>1</sup> This data production model originates in the recommendations from the science advisory council of the Southern California Integrated GPS Network (SCIGN) project and adopted by the Plate Boundary Observatory (PBO) and other monitoring projects.

displacements), (2) displacement grids including steady-state and physical transient motions (postseismic, hydrological, magmatic, etc.), and (3) seismogeodetic catalog of historical earthquakes. Level 4 include derived ESDRs, (1) transient slip and models in particular episodic and transient signals (ETS) in Cascadia (JPL), (2) strain-rate grids (SIO), and (3) total water storage for hydrological studies (JPL).

**Table 1:** Original proposed hierarchy of ESDRs from the ESESES proposal to NASA’s MEaSUREs program, which has been subsequently been modified as described in this ATBD document.

**Table 1: ESDRs to be produced under ESESES and their response to the Science Challenges posed by NASA’s Earth Surface and Interior**

ESDR	ESDR Description	Level	Algorithm Source	Need / Usage	CORE 2016* Sci. Challenge							
					1	2	3	4	5	6	7	
Continued Production (MEaSUREs 2012)	1.1 Global Calibrated/Validated Geodetic Displacement Time Series	1&2	NASA REASON MEaSUREs 2006 & 2012  (Davis, 1985; Bevis, 1992) JPL + NASA AIST + MEaSUREs 2012  NASA AIST 2008 + MEaSUREs 2012	Basis for all higher-level products. Need identified in CORE 2016.	X			X	X			
	1.2 Global Calibrated/Validated Geodetic Velocities	2		Long-term, high-resolution monitoring of changes in Earth’s surface addressing. Need identified in CORE 2016.	X			X	X			
	1.3 Calibrated/Validated Troposphere Delay Time Series	2		Forms the basis for Precipitable Water Vapor (PWV) ESDR and calibration maps for InSAR.	X			X	X			
	1.4 Calibrated/Validated Precipitable Water Vapor Time Series	2		Addresses key areas of uncertainty in the climate system and its potential changes (Gaffen, 2000).		X	X					
	1.5 Seismogeodetic records for historic earthquakes	3		Finite fault slip models, earthquake early warning and rapid response algorithms.	X					X		
New ESDRs	2.1 Continuous High-Rate Position time series	2	Penna et al. 2015	Investigate the full spectrum of Earth motions, transition from seismic to geodetic motions.	X			X	X			
	2.2 Plate Boundary Aseismic Transients	4	Crowell et al., 2016 + Liu et al., 2010, 2015b	Continuous monitoring of the state of subduction plate boundary; earthquake-cycle study and seismic hazard	X				X			
	2.3 Change in Total Water Storage Time Series	4	NASA ESI 2013	Determination of changes in total water storage at high resolution to constrain snow, soil moisture, and groundwater		X	X					X

We also present on the following 2 pages a quick reference to the products, relevant features and their access locations.

**Note: This incomplete**

Level	Product	Notes	Format	Location	Filename
1	Raw 3-D displacement time series	Gross outliers removed	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Raw_TrendNewTimeSeries_jpl*
		JPL	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Raw_TrendNewTimeSeries_jpl*
		SIO	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/ (temporarily discontinued)	WNAM_Raw_TrendNewTimeSeries_sopac*
1B	troposphere zenith delay	Combination	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/solutions/gipsy/trop	
		JPL (daily solutions)	trop format documented in README file	ftp://coddis.gsfc.nasa.gov/pub/GPS_Explorer/latest/trop/	
		JPL (timeseries)	SINEX_TRO V2.00	ftp://sopac-ftp.ucsd.edu/pub/solutions/<regional/global>	
		SIO (daily solutions)	GAMIT files		
1C	Cleaned/unfiltered displacement time series	Outliers and jumps removed	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_TrendNewTimeSeries_jpl*
		JPL	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_TrendNewTimeSeries_jpl*
		SIO	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_TrendNewTimeSeries_sopac*
		Combination	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_TrendNewTimeSeries_comb*
		PCA applied to cleaned series	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_jpl*
		JPL	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_jpl*
		SIO	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_sopac*
		Combination	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_comb*
		Difference of modeled series from cleaned time series	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_jpl*
		JPL	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_jpl*
		SIO	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_sopac*
		Combination	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_TrendNewTimeSeries_comb*
		Difference of modeled series from filtered time series	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_ResidNewTimeSeries_jpl*
		JPL	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_ResidNewTimeSeries_jpl*
		SIO	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_ResidNewTimeSeries_sopac*
		Combination	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Clean_ResidNewTimeSeries_comb*
		Difference of modeled series from filtered time series	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_ResidNewTimeSeries_jpl*
		JPL	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_ResidNewTimeSeries_jpl*
		SIO	self-documenting ASCII	ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_ResidNewTimeSeries_sopac*
		Combination	self-documenting ASCII	ftp://sopac-ftp.ucsd.edu/pub/timeseries/measures/ATS/WesternNorthAmerica/ftp://coddis.nasa.gov/pub/GPS_Explorer/latest/	WNAM_Filler_ResidNewTimeSeries_comb*

Level	Product	Notes	Format	Location	Filename
2	Velocity vectors				
		JPL	N E U sigma N sigma E sigma U (meters)	<a href="http://geocapp02.ucsd.edu:8080/gpseDB/vel?op=getNEUFile&amp;site_list=all&amp;coord=jpl_at">http://geocapp02.ucsd.edu:8080/gpseDB/vel?op=getNEUFile&amp;site_list=all&amp;coord=jpl_at</a>	
		SIO	N E U sigma N sigma E sigma U (meters)	<a href="http://geocapp02.ucsd.edu:8080/gpseDB/vel?op=getNEUFile&amp;site_list=all&amp;coord=sopac_at">http://geocapp02.ucsd.edu:8080/gpseDB/vel?op=getNEUFile&amp;site_list=all&amp;coord=sopac_at</a>	
		combination	N E U sigma N sigma E sigma U (meters)	<a href="http://geocapp02.ucsd.edu:8080/gpseDB/vel?op=getNEUFile&amp;site_list=all&amp;coord=comb_at">http://geocapp02.ucsd.edu:8080/gpseDB/vel?op=getNEUFile&amp;site_list=all&amp;coord=comb_at</a>	
2	Precipitable water vapor	JPL	SINEX_TRO V2.00	<a href="ftp://oddis.gsfc.nasa.gov/pub/GFS_Explorer/latavtrop">ftp://oddis.gsfc.nasa.gov/pub/GFS_Explorer/latavtrop</a>	
2	High-rate position timeseries	JPL		TBD	
		SIO		TBD	
3	Strain and Strain rate			TBD	
3	High-rate Seismogeodetic timeseries for significant earthquakes			<a href="ftp://sopac-ftp.ucsd.edu/pub/projects/Earthquakes">ftp://sopac-ftp.ucsd.edu/pub/projects/Earthquakes</a>	
4	Aseismic transients			TBD	
4	Water storage change			<a href="ftp://sopac-ftp.ucsd.edu/pub/projects/essses.2019">ftp://sopac-ftp.ucsd.edu/pub/projects/essses.2019</a>	

## 2. Displacement Time Series (Levels 1-2)

### 2.1 Methods

*Definition:* Long-term daily three-dimensional displacement time series of GNSS global and regional stations.

Both the JPL and the SIO analysis centers use the Level 0 GPS observables (dual-frequency phase and pseudorange stored in Hatanaka-compressed (<http://sopac-csrc.ucsd.edu/index.php/hatanaka>) stored as RINEX files – currently version 2.11 but we have been migrating to version 3 as it has propagated through the community. In addition, we use a single source of station information (metadata) stored in the SOPAC archive to ensure maximum consistency between our respective displacement time series. The stations used are identified by a master list of global and regional continuous GPS stations that is maintained through the SOPAC archive and database. The primary metadata consist of nominal station ITRF2014 positions, GPS equipment (receiver and antenna) models and serial numbers, and antenna offsets from the monument reference point. Changes in the metadata are entered into the database and reflected in IGS-formatted site logs obtained from other data centers, as well as for those stations managed by SOPAC (<http://sopac-csrc.ucsd.edu/index.php/sitelogs/>).

#### 2.1.1 JPL GIPSY Analysis & Raw Time Series

##### *Processing strategy - Precise Point Positioning*

The JPL Level 1 ESDR consists of daily GNSS station positions estimated using the GipsyX Network Processor (NWPx), which runs the GipsyX GPS data analysis software. The NWPx has been developed to analyze daily positions for large GPS networks using precise point positioning (PPP) (Zumberge *et al.*, 1997) with ambiguity resolution (Bertiger *et al.*, 2010) in a non-fiducial frame, later rotated into the IGS realization of ITRF. In the PPP strategy, satellite clock and orbits are fixed to the values provided from a separate precise orbit determination process. We use the JPL final (also historically termed JPL FLINN) non-fiducial orbits and satellite clock data products, which are the highest precision orbits released by JPL, with a latency of 4-14 days to allow for remote stations with slower data transmission to be included.

##### *Analysis strategy and physical models*

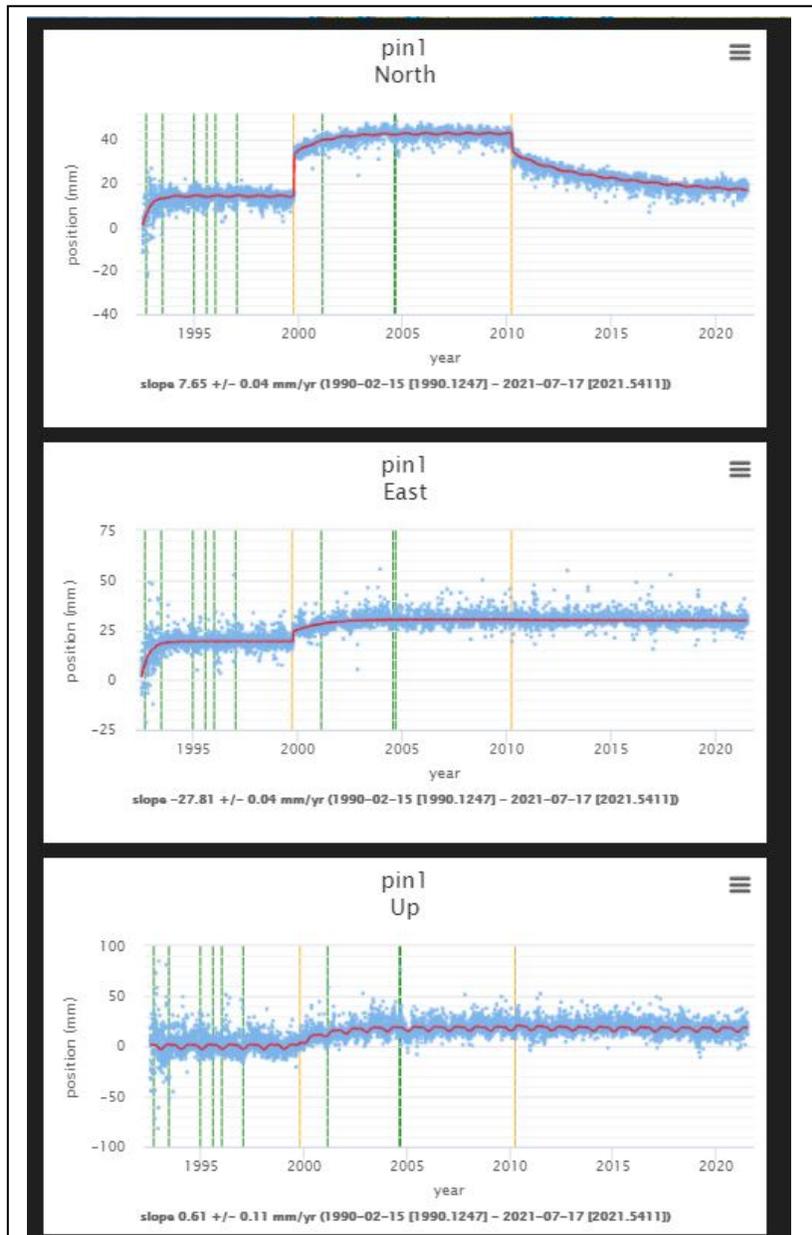
1. Solid Earth tides (IERS 2010 convention (*Petit and Luzum, 2010*))
2. Ocean tidal loading (IERS 2010 convention)
3. Pole tide (IERS 2010 convention)
4. Satellite yaw model (GYM95 (*Bar-Sever, 1996*))
5. GPT2w (*Boehm, 2015*) tropospheric mapping function for hydrostatic and wet components of the troposphere
6. General relativity effect (periodic clock corrections and gravity bending corrections applied) (IERS 2010 convention)

7. Absolute IGS phase center maps for receiver and transmitter antennas ([http://ftp.igs.org/pub/station/general/antenna\\_README.pdf](http://ftp.igs.org/pub/station/general/antenna_README.pdf))
8. GNSS data observations decimated to 5-minute intervals
9. Elevation angle cut-off set at 7 degrees

The wet zenith delay and two tropospheric gradient parameters are estimated as random walk parameters, updated every 5 minutes (*Bar-Sever et al., 1998*), with variance of  $5 \times 10^{-8}$  km/sqrt(sec) and  $5 \times 10^{-9}$  km/sqrt(sec), respectively.

*A priori information and constraints*

The GNSS analysis software requires the following a priori information for each station: station coordinates, antenna and receiver equipment type, phase center offsets for antenna, and the vector from the station monument to the reference point on the antenna. These metadata are kept up-to-date by SOPAC and are managed through the Oracle database. JPL retrieves this information from an XML file generated from the database and placed in the SOPAC archive for retrieval via http. A priori values for hydrostatic and wet delays are extracted



**Figure 3: Example of L1 product.** Unfiltered combined displacement time series in North, East, and Vertical components for station PIN1 from 1992 to July 2021. The time series are detrended and include the effects of coseismic and postseismic deformation. Thin vertical lines denote non-tectonic offsets primarily due to unlike antenna changes. The early scatter in the data (1992-1995) is due to insufficient infrastructure for GPS orbit and reference frame determination preceding the establishment of the International GNSS Service (e.g., Noll et al., 2009).

from the GPT2w model (*Boehm, 2015*).

#### *Ambiguity Resolution*

Single station ambiguity resolution is performed using Wide Lane Phase Bias Files delivered with the JPL orbits (*Bertiger et al., 2010*).

#### *Raw 3-D daily displacements and variance-covariance matrices*

The GipsyX solutions are stored in daily STACOV files, available from <http://garner.ucsd.edu/pub/solutions/gipsy/>. There are two files in each directory:

- (1) The loosely-constrained STACOV file with station positions and full variance-covariance matrices. The station positions resulting from this analysis are in a non-fiducial frame, defined by the orbits and clocks used in the PPP analysis. These station positions are then rotated with minimal internal constraints into the ITRF2014 (*Altamimi et al., 2016*) using a 7-parameter Helmert transformation, defined in a file provided with the JPL precise satellite ephemeris. **The daily STACOV file is input to the (JPL/SIO) combination along with the loosely-constrained GAMIT h-files, as described in section 2.1.3.**
- (2) The ITRF-constrained solution with the XYZ station positions and the (symmetric) 3x3 variance-covariance matrix for each station (represented by six elements corresponding to 3 sigma values and 3 correlations) - the cross-station covariances are excluded. The XYZ positions and full variance-covariance matrices extracted from the STACOV files are uploaded to the SOPAC database, extracted and converted to NEU coordinates as described in section 2.1.4. The reference epoch is chosen as the date of the first deployment of receiver/antenna at a station, as stored in the SOPAC database and extracted from IGS station log files. These solutions are constrained to the latest realization of ITRF (currently IGS14/ITRF2014).

**The NEU time series make up the Level 1 JPL “raw” displacement time series, available in “trended” and “detrended” versions (section 2.2). (Figure 5)**

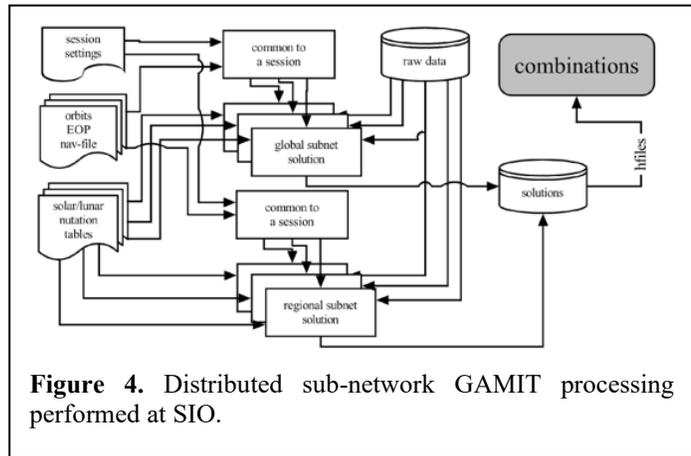
### 2.1.2 SOPAC GAMIT Analysis

#### *Processing Strategy - Distributed sub-network processing*

Daily GPS processing is carried out using the GAMIT/GLOBK software (<http://www-gpsg.mit.edu/~simon/gtgk/>; <http://sopac-csrc.ucsd.edu/index.php/gambit-globk/>); (*Herring et al.,*

2018) using a distributed processing approach (Zhang, 1996) on two sets of stations: global and regional (Scheme 1). Both solutions use 24-hour (0:00-23:59:30 GPST) RINEX-formatted data sampled at 30 s. The global solution uses data from 300+ IGS sites, divided in multiple (~8) sub-networks. The regional solution uses data from approximately 2000 western North America stations and stations of certain regions of special interest (Figure 1), divided into ~40 sub-

networks. Any individual sub-network has at least 3-6 overlapping stations with its immediate neighboring sub-network, in order to provide the necessary ties within a common reference frame in the process of combining the sub-networks using the GLOBK software (Figure 4).



**Figure 4.** Distributed sub-network GAMIT processing performed at SIO.

GAMIT solutions are iterated. That is, a pre-fit solution is followed by a post-fit solution to refine the modeling errors by taking advantage of post-fit residuals. In this process, a set of elevation-dependent functions, based on actual observations, are constructed on a site-by-site basis to down-weight noisier data at lower elevations.

#### *Physical Models*

1. Solid Earth tides (IERS 2010 convention (*Petit and Luzum, 2010*))
2. Ocean tidal loading (FES04 model with center of mass correction) (*Agnew, 2012*)
3. Pole tide (IERS 2010 convention)
4. Satellite yaw model (GYM95 (*Bar-Sever, 1996*))
5. VMF1 tropospheric mapping function (*Boehm et al., 2006*) for hydrostatic and wet components of the troposphere
6. 2<sup>nd</sup> and 3<sup>rd</sup> order ionospheric correction using the IGS AC published IONEX model
7. Absolute IGS phase center maps for station and satellite antennas  
([https://files.igs.org/pub/station/general/antenna\\_README.pdf](https://files.igs.org/pub/station/general/antenna_README.pdf))
8. General relativity effects (IERS 2010 convention)
9. IGS differential code bias (DCB, *Wang et al., 2016*)
10. BERN 15-parameter solar radiation model (*Springer et al., 1999*)

In addition, the first-order ionospheric effects and the satellite and receiver clock errors are eliminated through double differencing of the GPS observations (*Dong and Bock, 1989*). The elevation cutoff is set to 10° while automatic data cleaning uses all data regardless of their elevation. The atmospheric tidal loading model in GAMIT is currently not applied.

#### *A priori information and constraints*

The a priori parameters include IGS rapid orbits, IERS Bulletin A Earth orientation parameters (EOP) <https://www.iers.org/IERS/EN/DataProducts/EarthOrientationData/eop.html>, and station positions. The a priori positions (in the current definition of ITRF, currently ITRF2014) are taken from SOPAC's previous weekly solution, except IGS14 (IGS realization of ITRF2014) core stations whose epoch-date positions are taken as published (IGSMail 7399; <http://igs-rf.ign.fr/pub/IGS14>; <http://igs-rf.ensg.eu/pub/IGS14>). ITRF core station positions are constrained to 2-3 mm horizontally, and 5-10 mm vertically. For other reference stations, the constraints are set to 25 mm horizontally and 50-150 mm vertically. New stations are allowed to freely adjust. For orbit and radiation parameters, the constraints are 10 cm. For polar motion X and Y components, they are constrained to 3 mas (~10 cm) in position, and to 0.1 mas/day in rate. For UT1-UTC, the constraints are set to 0.02 ms in epoch, 0.1 ms/day in rate. The tropospheric zenith delays are constrained to 0.5 m within each estimation interval (hourly), and their variations are constrained to 10 cm between intervals with correlation time set to 100 hours.

During per station modeling and automatic data cleaning, GAMIT uses all observations at the specified sampling interval, currently 30 s. To save computational time, at the stage of solving the normal equations, the pre-fit solution only uses every 10<sup>th</sup> double-difference observable epoch (=300 s sampling interval). The post-fit solution uses every 4<sup>th</sup> epoch (=120 s sampling interval).

#### *Solutions and estimated parameters*

1. Satellite orbits (3 xyz and 3 XYZ velocities plus 9 radiation parameters (*Springer et al., 1999*) 24 hourly)
2. Earth orientation parameters (EOP) (24 hourly)
3. Station positions (24 hourly)
4. Tropospheric zenith delay parameters (hourly)
5. Tropospheric delay gradients (12-hourly in north-south and east-west directions)
6. L1 and L2 phase ambiguities

#### *Four-step GAMIT solution*

1. Coordinates and orbits constrained, phase ambiguities are free.
2. Coordinates and orbits constrained, phase ambiguities are fixed to integer values.
3. Coordinates and orbits loosely constrained, phase ambiguities are free.
4. Coordinates and orbits loosely constrained, phase ambiguities are fixed to integer values.

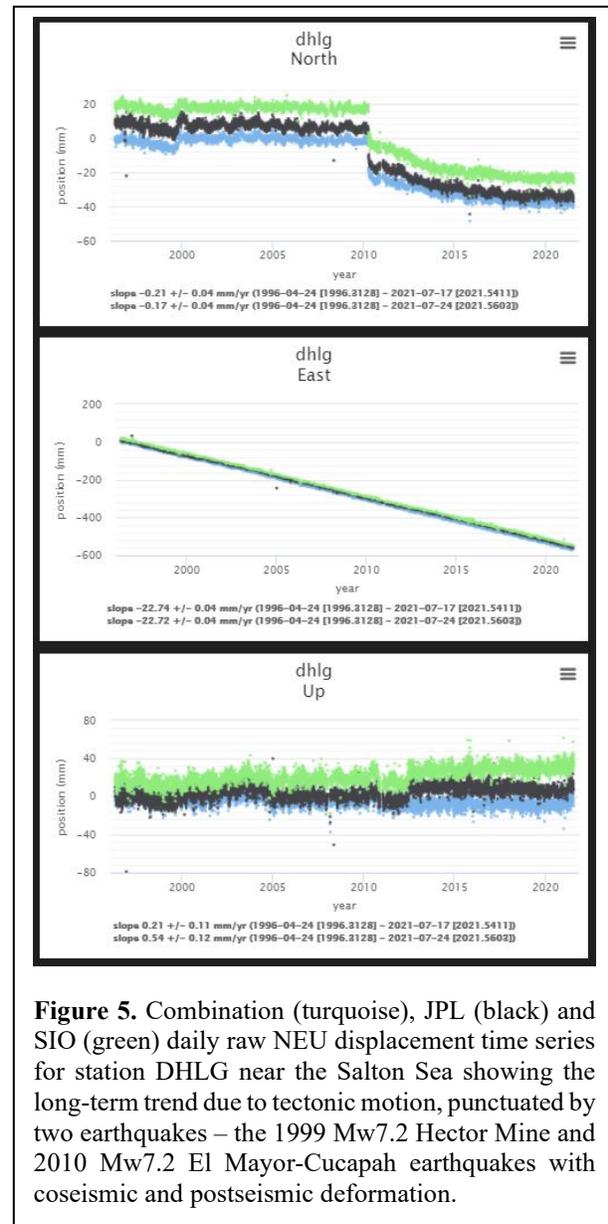
The estimated parameters and the full covariance matrices of step 4 for each of the individual sub-networks is saved into a set of GAMIT solution files (h-files) as the quasi observations for further processing for the SIO and combined raw displacement time series.

The loosely-constrained daily sub-network GAMIT h-files are located at <http://garner.ucsd.edu/solutions/regional> and <http://garner.ucsd.edu/solutions/global/>. The h-files are input to the (JPL/SIO) combination along with the loosely-constrained GipsyX STACOV files, as described in section 2.1.3.

#### *GLOBK adjustment for SIO raw time series*

The daily sub-network GAMIT h-files are combined weekly with GLOBK, tightly constrained to IGS14/ITRF14. The output .org files (e.g., gk2110\_pos.org) are located at <http://garner.ucsd.edu/pub/combinations/> sorted by GPS week. The XYZ values and their 3x3 covariance matrices (corresponding to three sigma values and three correlations) are uploaded to the SOPAC database, extracted and converted to NEU displacements, sigma values and correlations (section 2.14). The reference epoch is chosen as the date of the first deployment of receiver/antenna at a station, as stored in the SOPAC database and extracted from IGS station log files.

The daily NEU values make up the Level 1 SIO “raw” displacement time series, available in “trended” and “detrended” versions (section 2.2). (Figure 5)



**Figure 5.** Combination (turquoise), JPL (black) and SIO (green) daily raw NEU displacement time series for station DHLG near the Salton Sea showing the long-term trend due to tectonic motion, punctuated by two earthquakes – the 1999 Mw7.2 Hector Mine and 2010 Mw7.2 El Mayor-Cucapah earthquakes with coseismic and postseismic deformation.

### 2.1.3 Combination Analysis

*Definition:* Daily displacement time series of continuous GNSS stations based on the combined solutions from the JPL and SIO analysis centers.

The primary ESDR for the project and the basis for further ESDRs is an optimal combination of the JPL STACOV files and SIO h-files into a single set of daily displacements that are intended/assumed to be more precise than the individual and independent JPL and SIO solutions described in sections 2.1.1 and 2.1.2. Although JPL and SIO use different GNSS software and processing strategies, they both use the identical metadata from the SOPAC database and the same set of a priori station positions for the GipsyX and GAMIT analyses.

We are testing two strategies for estimating the combined time series:

- (1) Use a weighted mean algorithm to combine the post-ATS SIO and JPL Raw\_M XYZ time series (cleaned of outliers and non-coseismic offsets – section 2.1.9). Since both sets of time series are with respect to the latest version of ITRF/IGS14 (currently, ITRF2014/IGS14) the assumption is that it is valid to take their weighted mean without applying transformation parameters between the JPL and SIO time series. The algorithm is performed on a station-by-station basis assuming that there are no temporal processes (correlations in time) and there are no correlations between stations but using the variance-covariance matrices for each solution. We believe that this approach is also useful in identifying single- to multiple-epoch outliers for each station. It is also very efficient. The weighted mean algorithm is given in Appendix A.3.

- (2) Use the GLOBK software described in section 2.1.2 for the SIO time series but instead use the software to combine both the unconstrained SIO and JPL time series. This approach applies a Kalman filter using the full variance-covariance matrices and estimating transformation parameters between the two solutions in the process of estimating a combined solution with respect to ITRF/IGS14 (currently ITRF2014/IGS14) (section 2.1.4).

In both cases, the XYZ values are transformed into an NEU system using the transformed geodetic coordinates of the first epoch of data in the file rather than the date of the first receiver and antenna installation as recorded in the IGS station log files and entered into the SOPAC database. This is done to address the problem when we haven't processed the earlier data from a station that is in the process of being backfilled in preparation for reprocessing by JPL and SIO.

**The daily NEU values make up the Level 1 “raw” Combination displacement time series, available in “trended” and “detrended” versions (section 2.2). (Figure 5)**

### 2.1.4 Coordinate systems

The JPL and SIO analyses provide daily station position estimates ( $X, Y, Z$ ) in a global Earth-fixed, Earth-centered terrestrial reference frame (the latest being the IGS14 (IGSMail 7399; <http://igs-rf.ign.fr/pub/IGS14>; <http://igs-rf.ensg.eu/pub/IGS14>) realization of ITRF2014 – Altamimi et al. (2016)) and their covariance matrices collected in STACOV (GIPSY) and h-files (GAMIT), respectively. We transform these coordinates into more intuitive and physically meaningful horizontal and vertical displacements ( $\Delta N, \Delta E, \Delta U$ ) at epoch  $t_i$  with respect to station positions ( $X_0, Y_0, Z_0$ ) at an initial epoch  $t_0$ , according to:

$$\begin{aligned} \begin{bmatrix} \Delta N \\ \Delta E \\ \Delta U \end{bmatrix}_{t_i} &= \begin{bmatrix} -\sin\phi \cos\lambda & -\sin\lambda \sin\phi & \cos\phi \\ -\sin\lambda & \cos\lambda & 0 \\ \cos\lambda \cos\phi & \cos\phi \sin\lambda & \sin\phi \end{bmatrix}_{t_0} \left\{ \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_i} - \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_0} \right\} \\ &= G^T \left\{ \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_i} - \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{t_0} \right\} \end{aligned} \quad (1)$$

The relationship between “geodetic” coordinates ( $\phi, \lambda, h$ ), (ellipsoidal latitude, longitude and height) and spatial ( $X, Y, Z$ ) coordinates is

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} (\eta + h) \cos\phi \cos\lambda \\ (\eta + h) \cos\phi \sin\lambda \\ [\eta(1 - e^2) + h] \sin\phi \end{bmatrix}; \eta = a/(1 - e^2 \sin^2\phi)^{1/2}; e^2 = 2f - f^2 \quad (2)$$

with semimajor axis  $a$ , inverse flattening ( $1/f$ ), and  $e$  the ellipsoidal eccentricity. The parameters used in the transformation are the WGS84 values:  $a=6378137$  and  $1/f=298.257223563$ . The initial epoch  $t_0$  refers to the first daily position and is in general different for each station.

Given the covariance matrix  $\mathbf{C}_{X,Y,Z}$  from the GPS position analysis,

$$\mathbf{C}_{X,Y,Z} = \begin{bmatrix} \sigma_X^2 & \sigma_{XY} & \sigma_{XZ} \\ \sigma_{XY} & \sigma_Y^2 & \sigma_{YZ} \\ \sigma_{XZ} & \sigma_{YZ} & \sigma_Z^2 \end{bmatrix} \quad (3)$$

the propagation to the covariance matrix in the local frame at epoch  $t$  is given by

$$\mathbf{C}_{\Delta N, \Delta E, \Delta U} = \begin{bmatrix} \sigma_{\Delta N}^2 & \sigma_{\Delta N \Delta E} & \sigma_{\Delta N \Delta U} \\ \sigma_{\Delta N \Delta E} & \sigma_{\Delta E}^2 & \sigma_{\Delta E \Delta U} \\ \sigma_{\Delta N \Delta U} & \sigma_{\Delta E \Delta U} & \sigma_{\Delta U}^2 \end{bmatrix} = \mathbf{G} \mathbf{C}_{X,Y,Z} \mathbf{G}^T. \quad (4)$$

### 2.1.5 Offsets in Displacement Time Series

The daily displacement time series may contain various offsets due to either geophysical sources (i.e., earthquake rupture – coseismic displacements) or non-coseismic sources (e.g., antenna height changes, metadata errors, changes to unlike antennas, phase center modeling errors, reference

frame inconsistencies between the two analysis centers). Most of the non-geophysical offsets are due to changes in the type of antenna. Although both analysis centers use absolute antenna phase center models provided by the IGS, there still are residual offsets due to imperfections in the antenna production and calibrations (manifested mostly in the horizontal components). Other than possible reference frame inconsistencies (for example, an update from ITRF2008 to ITRF2014), which are initiated by either SIO and/or JPL at different times, in principle, all other offsets should be present in both solutions. In most cases, non-coseismic offsets are considered to apply to both horizontal and vertical components. The complete set of identified offsets (from SIO and JPL) are carried over to the combination time series (section 2.1.3), where additional offsets may become apparent through, for example, visual inspection of the affected time series.

The dates of the non-coseismic offsets are derived from IGS-type station log files when a change is detected (this information is incorporated into the database) and the dates coseismic offsets from earthquake catalogs (e.g., from the USGS). An antenna and/or receiver change may or may not result in a significant offset. Occasionally, the cause of an offset may be unknown. It is the responsibility of the time series administrator to identify significant offsets and assign new offset parameters. A pernicious problem are metadata changes that are not incorporated into the database in a timely fashion, that is, after the GAMIT and/or GipsyX analysis. In this case, additional offsets may be required. Infrequent and costly reruns of the entire data holdings, motivated by the change in the ITRF definition, will allow these offsets to be retroactively estimated.

### 2.1.6 Time Series Analysis

The position estimates (XYZ) and their variance-covariance matrices are output as ITRF-constrained STACOV files from the Gipsy-X analysis (section 2.1.1) and the GLOBK output (constrained adjustment of the GAMIT subnetwork h-files) (section 2.1.2) from which the Level 1 JPL and SIO displacement time series are derived (section 2.2). The JPL and SOPAC XYZ solutions are converted to displacements in an NEU system (section 2.1.4) using the WGS84 ellipsoid parameters and the epoch ( $t_0$ ) as the reference epoch. The reference epoch is chosen as the date of the first deployment of receiver/antenna at a station, as stored in the SOPAC database and extracted from IGS station log files. For each station, the 3x3 block diagonal elements (represented by 6 elements based on the symmetry of the covariance matrices) are retained for each station's NEU displacements after transformation from global (X, Y, Z) coordinates (equation 1). We can neglect the cross-correlations between stations based on the analysis of Zhang (1996) who shows that their values are insignificant. Furthermore, the NEU correlations are small ( $<0.1$ ) (not the XYZ correlations) and it is justified to perform a parametric time series analysis, separately for each component.

An individual component time series ( $\Delta N$ ,  $\Delta E$ , or  $\Delta U$ ) at discrete epochs  $t_i$  can be modeled as

$$y(t_i) = a + bt_i + c\sin(2\pi t_i) + d\cos(2\pi t_i) + e\sin(4\pi t_i) + f\cos(4\pi t_i) + \\ + \sum_{j=1}^{n_g} g_j H(t_i - T_{g_j}) + \sum_{j=1}^{n_h} h_j H(t_i - T_{h_j}) t_i +$$

$$+ \sum_{j=1}^{n_k} k_j \left(1 - e^{\left[-\left(\frac{t_i - T_{k_j}}{\tau_j}\right)\right]}\right) H(t_i - T_{k_j}) + \varepsilon_i \quad (12)$$

where  $H$  denotes the discrete Heaviside function,

$$H = \begin{cases} 0, & t_i - T_{k_j} < 0 \\ 1, & t_i - T_{k_j} \geq 0 \end{cases}$$

The coefficient  $a$  is the value at the initial epoch  $t_0$  and  $t_i$  denotes the time elapsed from  $t_0$  in units of years. The linear rate (slope)  $b$  represents the interseismic secular tectonic motion, typically expressed in mm/yr. The coefficients  $c$ ,  $d$ ,  $e$ , and  $f$  denote unmodeled annual and semi-annual variations present in GPS position time series. Annual and semiannual terms are estimated when enough data (12 months for velocity and seasonal terms) have been collected. Amplitude and phase of annual and semiannual signals are expressed according to the sine convention  $A \cdot \sin(\omega(t - t_Y) + \phi)$ , where  $t_Y$  is January 1. The magnitudes  $g$  of  $n_g$  offsets (jumps, steps, discontinuities) are due to coseismic deformation and/or non-coseismic changes at epochs  $T_g$  (section 2.5). Possible  $n_h$  changes in velocity are denoted by new velocity values  $h$  at epochs  $T_h$ . Coefficients  $k$  are for  $n_k$  postseismic deformation starting at epochs  $T_k$  and decaying exponentially with a time constant  $\tau_j$ . The “logarithmic” model is another parameterization associated with afterslip on the fault surface; the exponential model is associated with motion below the crust (mantle) (Wang et al. 2012a). The logarithmic model is expressed as

$$\sum_{j=1}^{n_k} k_j \log\left(1 + \frac{t_i - T_{k_j}}{\tau_j}\right) H(t_i - T_{k_j}) \quad (13)$$

and was applied, for example, to 2004 Mw6.0 Parkfield, California earthquake (Freed 2007).

The event times  $T$  ( $g$ ,  $h$ ,  $k$ ) can be determined from earthquake catalogs, site logs, automatic detection algorithms, or by visual inspection. The postseismic decay times  $\tau_j$  are typically estimated separately by maximum likelihood methods, so that estimation of the remaining time series coefficients can be expressed as a linear inverse problem.

$$\mathbf{y} = \mathbf{A}\mathbf{x} + \boldsymbol{\varepsilon}; E\{\boldsymbol{\varepsilon}\} = \mathbf{0}; D\{\boldsymbol{\varepsilon}\} = \sigma_0^2 \mathbf{C}_\varepsilon \quad (14)$$

where  $\mathbf{A}$  is the design matrix and  $\mathbf{x}$  is the parameter vector,

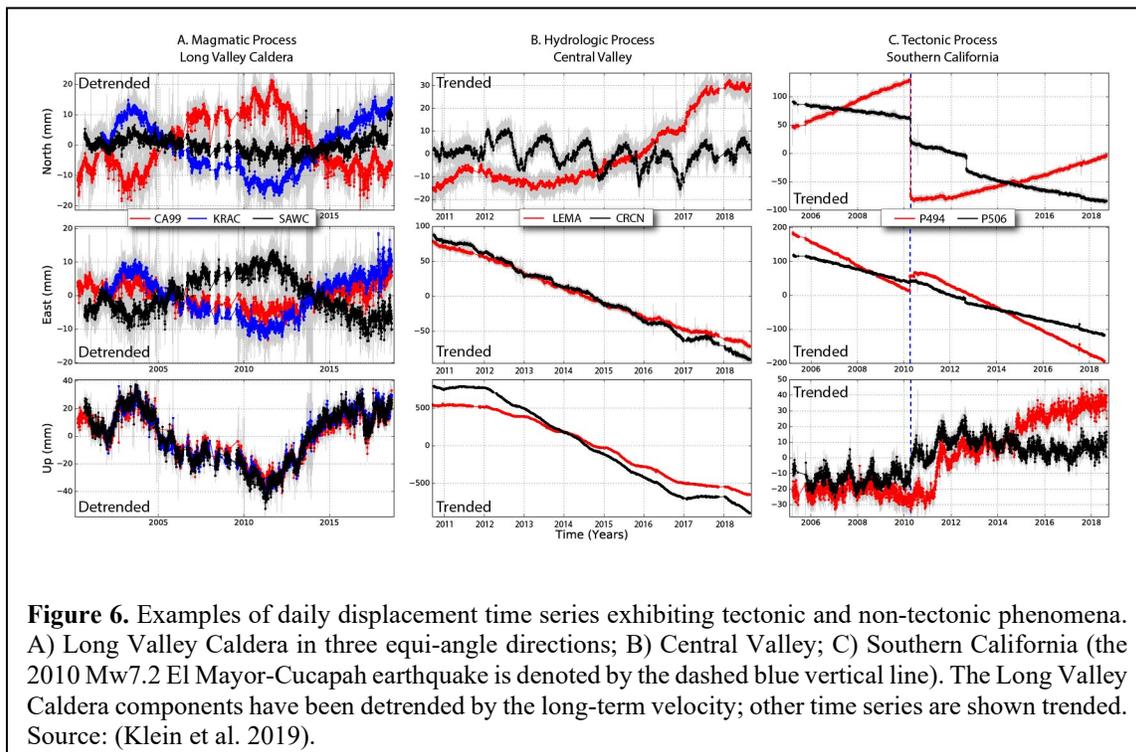
$$\mathbf{x} = (a \ b \ c \ d \ e \ f \ \mathbf{g} \ \mathbf{h} \ \mathbf{k})^T. \quad (15)$$

$E$  denotes statistical expectation,  $D$  denotes statistical dispersion,  $\mathbf{C}_\varepsilon$  is the covariance matrix of observation errors,  $\mathbf{P} = \mathbf{C}_\varepsilon^{-1}$  is the weight matrix, and  $\sigma_0^2$  is an *a priori* variance factor. The output from the adjustment are the modeled daily displacement series, the model parameters and their uncertainties. An examination of the postfit residuals  $\hat{\boldsymbol{\varepsilon}} = \mathbf{y} - \mathbf{A}\hat{\mathbf{x}}$  are important to identify deviations from the parametric model, including any physical transients, and mismodeling.

The time series analysis is performed by JPL’s `analyz_tseri` (ATS) software ([https://qoca.jpl.nasa.gov/advclass/tsa\\_intro.html](https://qoca.jpl.nasa.gov/advclass/tsa_intro.html)) for the individual JPL and SIO time series and for the combination.

Other parameters can be estimated in the ATS adjustment but have not been generally applied. For example, a local polynomial is available to model local environmental changes due to groundwater extraction in California’s Central Valley or geophysical activity such as magmatic swelling of the Long Valley Caldera (Figure 6).

A tutorial for the ATS process can be found at [https://qoca.jpl.nasa.gov/advclass/tsa\\_intro.html](https://qoca.jpl.nasa.gov/advclass/tsa_intro.html); [https://qoca.jpl.nasa.gov/tutor\\_base.html](https://qoca.jpl.nasa.gov/tutor_base.html)).



### 2.1.7 Regionally-filtered time series (PCA)

Examination of the post-fit residuals  $\hat{\boldsymbol{\epsilon}} = \mathbf{y} - \mathbf{A}\hat{\mathbf{x}}$  from the least squares adjustment often reveals common signatures within a geographical region (e.g., Western U.S.), indicating a larger-scale source. Spatio-temporal filtering of the residuals can be used to estimate and remove the “common-mode error (CME)” allowing for improved discernment of tectonic signals. An early study suggested a simple stacking procedure (Wdowinski et al. 1997), a simple form of principal component analysis (PCA) (Dong et al. 2006).

PCA is used to perform spatio-temporal regional filtering as described in *Dong et al.* (2006). Currently, PCA is only performed for the western North America stations. We are also considering

a focused filter on other regional sub-networks. The PCA analysis generates both the major principal component time series, as well as the spatial responses of each station for the major principal components. The advantage of the PCA method compared to the traditional removal of the CME calculated using a stacking method (*Wdowinski et al. 1997*) is the elimination of the implicit assumption of uniform CME across the network. Furthermore, PCA identifies the modes of 3D motion common to all sites and allows for spatial weighting of the CME. After the CME estimates are subtracted, the same time series estimation process described in the previous section is repeated.

It is important to note that the effect of PCA is to reduce the noise (rms) of the displacement time series so that signals of interest are more recognizable. It does not eliminate the signals of interest, e.g., postseismic deformation, episodic tremor and slip (ETS – section 8). In addition, a subset of stations may be excluded from the PCA analysis because of the presence of unmodeled effects (e.g., magmatic motion at Long Valley caldera). However, the common modes can be eliminated for those stations, as well. Currently, we only apply the first principal component.

The PCA process is as follows (*Dong et al. 2006*). The post-fit residuals are stored column-wise in a matrix  $\mathbf{X}$  according to the displacement components in north, east and up directions for epoch  $m$  ( $m=1, M$ ) and station  $n$  ( $n=1, N$ ) assuming  $m > n$  (this is always the case in geodetic analysis). The “covariance” matrix is defined by

$$\mathbf{B} = \frac{1}{M-1} \mathbf{X}^T \mathbf{X}, \quad (16)$$

which is decomposed by

$$\mathbf{B} = \mathbf{V} \mathbf{\Lambda} \mathbf{V}^T. \quad (17)$$

$\mathbf{B}$  is a full rank matrix of dimension  $N$ ,  $\mathbf{V}$  is the eigenvector matrix and  $\mathbf{\Lambda}$  has  $k$  non-zero eigenvalues along its diagonal ( $N \geq k$ ). Then, using  $\mathbf{V}$  as an orthonormal basis at epoch  $i$

$$X(t_i, x_n) = \sum_{k=1}^N a_k(t_i) v_k(x_n) \quad (18)$$

$$a_k(t_i) = \sum_{n=1}^N X(t_i, x_n) v_k(x_n) \quad (19)$$

The eigenvalue  $a_k(t_i)$  is the  $k$ th principal component representing the temporal variations and  $v_k(x_n)$  is the corresponding eigenvector representing the spatial responses to the principal components. The largest principal component corresponds to the primary contributor to the variance of the network-wide residual time series, while the smallest principal component has the least contribution.

All the “cleaned” time series are subject to a Principal Component Analysis (PCA) (*Dong et al., 2006*) to reduce noise. Currently, we only apply the first principal component, which is similar to removing the common mode signature as described by *Wdowinski et al. (1996)*. The PCA filter

does not remove signal (e.g., episodic tremor and slip – it only reduces the noise, thereby improving the time series model estimates. Currently, only the “Western North America (WNAM)” stations are filtered. We maintain a list of stations whose time series are used in the PCA process – other stations exhibit large systematic signatures that can bias the principal components. However, the results of the PCA are applied to all WNAM time series.

**The daily NEU displacements resulting from PCA make up the Level 2 “WNAM\_Filter” time series (section 2.2), available in “trended” and “detrended” versions.**

### 2.1.8 Residuals

The post-fit “residuals”  $\hat{\epsilon} = \mathbf{y} - \mathbf{A}\hat{\mathbf{x}}$  from the time series analysis (ATS) are differences between the observed and (parametrically) modeled time series and indicate how well the model fits the data. The residual time series are not subject to the post-ATS step (section 2.1.9). There are residual time series for the cleaned and filtered time series (sections 2.1.6 and 2.1.7). They are detrended by definition since the slope is one of the estimated parameters.

**The daily NEU residuals from the JPL, SIO and Combination ATS processes make up the “Clean\_ResidNeu” time series (section 2.2).**

### 2.1.9 Post-ATS Analysis

In Year 3 we introduced an improved set of displacement time series products derived from the SIO, JPL and combination ATS solutions. Using Post-ATS Python scripts we remove the outliers detected in the ATS process, correct for any non-coseismic offsets and reinsert any coseismic offsets. This results in a modified raw time series that reflects the actual physical motions of the stations after removing non-physical artifacts. We refer to these modified raw data files as “Raw\_M” time series, which has not been modeled. They include for WNAM and GLOBAL stations:

- (3) Detrended and trended NEU time series: **WNAM\_Raw\_M\_DetrendNeu** & **WNAM\_Raw\_M\_DetrendNeu**
- (4) Trended XYZ positions: **WNAM\_Raw\_TrendXYZ**
- (5) Trended XYZ positions **RawJumps\_TrendXYZ** with both non-coseismic and coseismic offsets intact, with outliers removed.

*Note:* The RawJumpsXYZ time series have been created by request for the Crustal Motion Model (CMM) (<http://scecinfo.usc.edu/resources/data/index.html>) developed under the aegis of the Southern California Earthquake Center (SCEC). This allows our time series to be compatible with other community time series.

The residual time series (section 2.1.8) are not subject to the post-ATS step.

### 2.1.10 Calibration, Validation and Verification

**Calibration** is the process of discovering biases and scale factors in a method of processing instrument data and correcting the data for these factors. **Validation** ensures that a system satisfies the stated functional intent of the system and the requirements of a project. **Verification** ensures the correct operation of a process according to its stated operating specifications.

#### **Calibration**

Calibration is carried out at all ESDR levels. It is listed at Level 2 since the quality of all higher-level products are informed by accurate calibration.

- (6) Level 0: Accuracy and timeliness of metadata, in particular changes in antenna model and height. Metadata are gathered through collection of station log files and ingested into the database. Late and/or inaccurate metadata will propagate into the ESDRs and introduce spurious offsets into the displacement time series, as well as loss of precision. This requires setting an offset parameter in the time series analysis. The offset can be removed after a re-analysis of the GNSS data.
- (7) Level 0: Completeness and timeliness of station RINEX data. RINEX data that do not arrive on time cause gaps in the time series and disruptions in the production of ESDRs. However, missing data can be back-filled prior to a re-analysis of the entire data holdings.
- (8) Detection of outliers in the ATS process (Table 2). Individual criteria can be specified for each station, as needed:

*weak\_obs (big sigma) criteria (mm)*: based on the formal errors.

If at one epoch the formal sigma values of one site are bigger than the specified criteria, the solution of this site at this epoch will be ignored. The order is e, n, up.

*outlier (big o-c) criteria (mm)*: based on the postfit residuals.

If at one epoch the residuals of one site are bigger than the specified criteria, the solution of this site at this epoch will be ignored. This command prevents outliers from contaminating the time series analysis results. The order is e, n, up.

*very bad\_obs criteria (mm)*: based on gross outlier threshold.

If the data have gross outliers the initial adjustments will be biased. They are removed before the adjustment. The order is e, n, up.

**Table 2.** Default criteria from the analyze\_tseri driver file

Criteria	East(mm)	North(mm)	Up(mm)
weak_obs (big sigma)	40.	40.	80.
outlier (big o-c)	25.	25.	35.
very bad_obs	1000.	1000.	3000.

- (9) Further detection of data outliers occurs through visual inspection, which is flagged during any of the different product levels, for example, by anomalies in the displacement grids (section 5). We maintain a Google document called “omit\_span” where outliers are recorded and removed in subsequent ATS analyses: **Note: Not publicly available – available on request**

[https://docs.google.com/spreadsheets/d/1lp6dZSycCT1by7xxbO1b6H\\_D-1L29Ep5/edit#gid=213666945](https://docs.google.com/spreadsheets/d/1lp6dZSycCT1by7xxbO1b6H_D-1L29Ep5/edit#gid=213666945))

**Note: All time series ESDRs have all outliers removed (from ATS and post-ATS processes)**

- (10) The GAMIT and GIPSY analyses that produce the Level 1 SIO and JPL raw time series are seeded with a-priori station coordinates derived from the latest weekly ATS processes (preferably the cleaned combination solution). Gross errors in the a priori coordinates can adversely affect the analyses and result in gaps in the time series. The a priori coordinates are entered by JPL and SIO through parallel processes that extract the information from the SOPAC database. JPL uses station XML files, while SOPAC uses a flat file generated from the SOPAC database. These need to be checked periodically to ensure that they are indeed equivalent.
- (11) Large adjustments from the a priori coordinates are flagged on a weekly basis for review by the time series administrator. These can be due to geophysical signals (e.g., coseismic displacements), inaccurate metadata or problems in the GNSS analyses.
- (12) The latest estimated velocities (section 4) estimated by JPL and SIO are regularly compared to identify, understand and repair any significant differences – we focus on discrepancies greater than 5 mm/yr (Figure 7). In addition, we identify annual amplitude terms (section 2.1.6) that exceed a certain percentage (50% for the horizontal and 150% for the vertical).
- (13) We maintain a Master List (<http://geoapp02.ucsd.edu:8080/gpseDB/psite?op=showCleanList> – VPN required) of stations that are processed. From time to time a station may be removed altogether based on several factors, for example, very few data points have been recorded for a defunct station (no longer operational).
- (14) Interactive examination of the displacement time series is performed to identify and flag problematic time series related to the eight items above. This is performed by the time series administrator through the GPS Explorer interface that is in the process of moving to a different platform. This requires administrator privileges. The administrator is also responsible for adding new parameters for the time series analysis. For example, after an earthquake occurs coseismic offsets must be estimated for all stations that have had significant permanent (static) displacements and eventually postseismic parameters must be set. Depending on the earthquake's fault mechanism (strike-slip, thrust, normal), the time series may only require horizontal (N and E) offsets. Likewise, a limited number of stations closest to the epicenter may also require vertical offsets as was the case for the July 6, 2019 Mw7.1 Ridgecrest earthquake in Central California. When an antenna model change has been recorded in the station log files, the date is flagged and the administrator determines if it has caused a significant offset in the time series. Our philosophy is to add a new model parameter only when it is required.

## Validation and Verification

This document describes the elements of our ESESES system, as summarized in the flow chart of Figure 2 with the agreed upon ESDRs. Validation requires the verification of a complete and accurate transfer of these products to CDDIS, according to the schedule determined by the nature of the product. For example, the displacement time series tar files (section 2.2) are delivered to CDDIS once per week, while the ETS transients (section 7) are updated as ETS events occur (with an interval of about 14 months).

## 2.2 Displacement Time Series

This information can also be found at

[http://garner.ucsd.edu/pub/timeseries/measures/ats/ATS\\_TarFile\\_README.txt](http://garner.ucsd.edu/pub/timeseries/measures/ats/ATS_TarFile_README.txt)

We produce a series of displacement time series summarized below and described in the following subsections. There are three overall sets including JPL (“jpl”), SIO (“sopac”) and combined (“comb”) products. Currently, the time series are divided according to stations in Western North America (WNAM) and all other geographic locations (GLB). The time series are extended weekly and a set of new tar files are created. We use two coordinate systems, XYZ and NEU (section 2.1.4). All the time series are appended with seven data points each week and recalculated weekly.

Each week, a set of tar files are created and stored at two archives:

SOPAC:

[http://garner.ucsd.edu/pub/timeseries/measures/ats/WesternNorthAmerica/Index\\_of/pub/timeseries/measures/ats/Global\(ucsd.edu\)](http://garner.ucsd.edu/pub/timeseries/measures/ats/WesternNorthAmerica/Index_of/pub/timeseries/measures/ats/Global(ucsd.edu))

CDDIS: [http://cddis.nasa.gov/pub/GPS\\_Explorer/latest/](http://cddis.nasa.gov/pub/GPS_Explorer/latest/) ! **Note this may change**

Note that:

- The time series can be viewed with MGviz (section 10.2)
- File headers contain estimated time series model parameters (section 2.1.6)
- The file headers in the “Raw\_M” time series are included for documentation purposes – they have not gone through a time series analysis but have used information from the modeled cleaned time series (location of offsets and outliers)
- All the time series except “Raw” have outliers and jumps (non-coseismic offsets) removed
- PCA filtering is only performed for “WNAM” time series
- YYYYMMDD indicates the date that the tar file was created

### (1) NEU raw time series

***Trended:***

#### (a) Western North America

WNAM\_Raw\_TrendNeuTimeSeries\_comb\_20210512.tar

WNAM\_Raw\_TrendNeuTimeSeries\_jpl\_20210512.tar

WNAM\_Raw\_TrendNeuTimeSeries\_sopac\_20210512.tar

#### (b) Global

GLB\_Raw\_TrendNeuTimeSeries\_comb\_20210512.tar  
GLB\_Raw\_TrendNeuTimeSeries\_jpl\_20210512.tar  
GLB\_Raw\_TrendNeuTimeSeries\_sopac\_20210512.tar

**(2) NEU modeled (“Clean”) time series**

***Trended:***

**(a) Western North America**

WNAM\_Clean\_TrendNeuTimeSeries\_comb\_YYYYMMDD.tar  
WNAM\_Clean\_TrendNeuTimeSeries\_jpl\_YYYYMMDD.tar  
WNAM\_Clean\_TrendNeuTimeSeries\_sopac\_20200330.tar

**(b) Global**

GLB\_Clean\_TrendNeuTimeSeries\_comb\_YYYYMMDD.tar  
GLB\_Clean\_TrendNeuTimeSeries\_jpl\_YYYYMMDD.tar  
GLB\_Clean\_TrendNeuTimeSeries\_sopac\_20200330.tar

***Detrended:***

**(a) Western North America**

WNAM\_Clean\_DetrendNeuTimeSeries\_comb\_YYYYMMDD.tar  
WNAM\_Clean\_DetrendNeuTimeSeries\_jpl\_YYYYMMDD.tar  
WNAM\_Clean\_DetrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(b) Global**

GLB\_Clean\_DetrendNeuTimeSeries\_comb\_YYYYMMDD.tar  
GLB\_Clean\_DetrendNeuTimeSeries\_jpl\_YYYYMMDD.tar  
GLB\_Clean\_DetrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(3) NEU residual displacements (detrended by definition)**

**(a) Western North America**

WNAM\_Clean\_ResidNeuTimeSeries\_comb\_YYYYMMDD.tar  
WNAM\_Clean\_ResidNeuTimeSeries\_jpl\_YYYYMMDD.tar  
WNAM\_Clean\_ResidNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(b) Global**

GLB\_Clean\_ResidNeuTimeSeries\_comb\_YYYYMMDD.tar  
GLB\_Clean\_ResidNeuTimeSeries\_jpl\_YYYYMMDD.tar  
GLB\_Clean\_ResidNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(4) PCA-filtered displacements (WNAM only)**

***Trended:***

WNAM\_Filter\_TrendNeuTimeSeries\_comb\_YYYYMMDD.tar  
WNAM\_Filter\_TrendNeuTimeSeries\_jpl\_YYYYMMDD.tar  
WNAM\_Filter\_TrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

***Detrended:***

WNAM\_Filter\_DetrendNeuTimeSeries\_comb\_YYYYMMDD.tar  
WNAM\_Filter\_DetrendNeuTimeSeries\_jpl\_YYYYMMDD.tar

WNAM\_Filter\_DetrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(5) NEU filtered residual displacements (detrended by definition)**

WNAM\_Filter\_ResidNeuTimeSeries\_comb\_YYYYMMDD.tar

WNAM\_Filter\_ResidNeuTimeSeries\_jpl\_YYYYMMDD.tar

WNAM\_Filter\_ResidNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(6) NEU raw-modified (Raw\_M) time series**

***Trended:***

**(a) Western North America**

WNAM\_Raw\_M\_TrendNeuTimeSeries\_comb\_YYYYMMDD.tar

WNAM\_Raw\_M\_TrendNeuTimeSeries\_jpl\_YYYYMMDD.tar

WNAM\_Raw\_M\_TrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(b) Global**

Global\_Raw\_M\_TrendNeuTimeSeries\_comb\_YYYYMMDD.tar

Global\_Raw\_M\_TrendNeuTimeSeries\_jpl\_YYYYMMDD.tar

Global\_Raw\_M\_TrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

***Detrended:***

**(a) Western North America**

WNAM\_Raw\_M\_DetrendNeuTimeSeries\_comb\_YYYYMMDD.tar

WNAM\_Raw\_M\_DetrendNeuTimeSeries\_jpl\_YYYYMMDD.tar

WNAM\_Raw\_M\_DetrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(b) Global**

GLB\_Raw\_M\_DetrendNeuTimeSeries\_comb\_YYYYMMDD.tar

GLB\_Raw\_M\_DetrendNeuTimeSeries\_jpl\_YYYYMMDD.tar

GLB\_Raw\_M\_DetrendNeuTimeSeries\_sopac\_YYYYMMDD.tar

**(7) ITRF2014 XYZ displacements**

***Raw time series – coseismic and non-coseismic offsets uncorrected, outliers removed***

**(a) Western North America**

WNAM\_RawJumps\_TrendXYZTimeSeries\_comb\_YYYYMMDD.tar

WNAM\_RawJumps\_TrendXYZTimeSeries\_jpl\_YYYYMMDD.tar

WNAM\_RawJumps\_TrendXYZTimeSeries\_sopac\_YYYYMMDD.tar

**(b) Global**

GLB\_RawJumps\_TrendXYZTimeSeries\_comb\_YYYYMMDD.tar

GLB\_RawJumps\_TrendXYZTimeSeries\_jpl\_YYYYMMDD.tar

GLB\_RawJumps\_TrendXYZTimeSeries\_sopac\_YYYYMMDD.tar

***Raw time series – non-coseismic jumps corrected, outliers removed***

**(a) Western North America**

WNAM\_Raw\_TrendXYZTimeSeries\_comb\_YYYYMMDD.tar

WNAM\_Raw\_TrendXYZTimeSeries\_jpl\_YYYYMMDD.tar

WNAM\_Raw\_TrendXYZTimeSeries\_sopac\_YYYYMMDD.tar

**(a) Global**

GLB\_Raw\_TrendXYZTimeSeries\_comb\_YYYYMMDD.tar

GLB\_Raw\_TrendXYZTimeSeries\_jpl\_YYYYMMDD.tar

GLB\_Raw\_TrendXYZTimeSeries\_sopac\_YYYYMMDD.tar

**3. Troposphere Delay & Precipitable Water****3.1 Method****3.1.2 Troposphere delay**

As described in sections 2.1 and 2.2 (Level 1A) both JPL and SIO estimate troposphere parameters as part of the GIPSY/OASIS and GAMIT analysis, respectively. The total tropospheric delay (TD) observed by GPS is the integrated refractivity of the atmosphere,  $N$ , over the signal ray path

$$TD = \int_{s=\text{raypath}} N ds = \int_{s=\text{raypath}} \left( k_1 \frac{P}{T} + k_2 \frac{e}{T} + k_3 \frac{e}{T^2} \right) ds$$

where  $P$  is the atmospheric pressure,  $T$  is temperature,  $e$  is water vapor partial pressure, and the  $k$ 's are empirically determined physical constants in an expression for  $N$  (Bevis *et al.*, 1994). Therefore, the estimated tropospheric signal delay provides information about the unknown moisture above the station. The tropospheric delay observed for a given satellite at angle  $\theta$  from vertical is modeled as Davis *et al.* (1994),

$$TD(\theta) = ZHD \times mh(\theta) + ZWD \times mw(\theta)$$

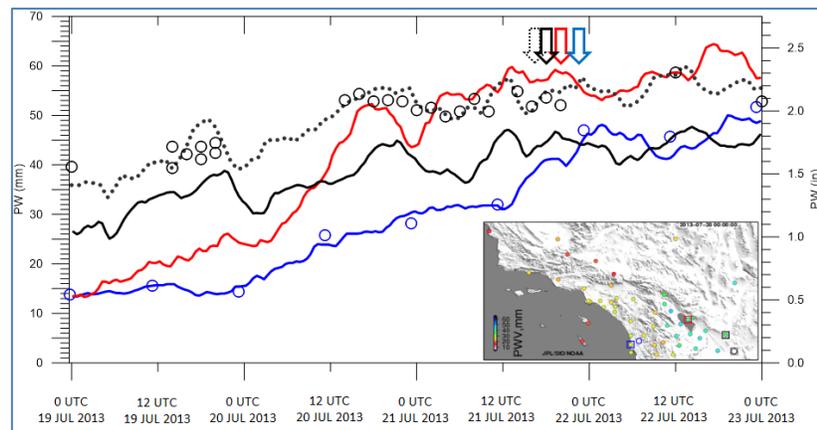
where ZHD is the zenith hydrostatic delay, ZWD is the zenith wet delay, and  $mh$  and  $mw$  are mapping functions that describe the variation of ZHD and ZWD with varying elevation angle. Both JPL and SIO currently utilize the gridded Vienna Mapping Function [VMF1GRID – (Boehm *et al.* 2006); <http://ggosatm.hg.tuwien.ac.at/delay.html>] for a priori hydrostatic and wet troposphere delay components values and to model zenith delay variance. Use of final GPS orbits (at 7- to 10-day latency) ensures the highest fidelity troposphere series for retrospective studies (Moore *et al.*, 2016; Wang *et al.*, 2019). Troposphere delays are estimated at 5-minute resolution by JPL and hourly by SIO. These solutions are available from <http://garner.ucsd.edu/solutions/gipsy/trop/>. The SOPAC solutions are in <http://garner.ucsd.edu/pub/troposphere> but have not been updated since 2011. **The data beyond 2011 need to be extracted from the GAMIT output. Currently, there is no combination solution for the troposphere ESDRs.**

### 3.1.2 Precipitable Water Vapor

With a modest investment in computation following established algorithms (e.g., Bevis et al., 1994), the zenith total delays (ZTD) necessarily estimated during the displacement time series processing with temporal resolution up to 5 min become the basis for an ESDR consisting of precipitable water vapor (PWV) time series. The conversion to PWV requires the zenith wet delay (ZWD), obtained by subtracting from the ZTD an accurate zenith hydrostatic delay (ZHD) (Saastamoinen, 1973) as a function of surface pressure, latitude, and orthometric height. 1 hPa of pressure error implies uncertainty of 0.35mm in PWV (Nilsson and Elgered, 2008), an accuracy easily obtained by onsite barometers. PWV time series are useful for tracking extreme weather events such as monsoons (Figure 7) and atmospheric rivers that can lead to flash flooding (Moore et al., 2015; Wang et al., 2019). We produce PWV records in the SINEX\_TRO2.0 Provisional format for stations with onsite meteorological measurements. The

conversion from ZWD to PWV further requires a measure of mean atmospheric temperature, which can be estimated from surface temperature (Bevis, 1994) and is a lesser source of PWV error in comparison to pressure.

These PWV solutions are available at [http://cddis.nasa.gov/pub/GPS\\_Explorer/latest/trop/](http://cddis.nasa.gov/pub/GPS_Explorer/latest/trop/).



**Figure 7: GPS PWV measurements were used both operationally to track a North American Monsoon event and forecast flash flooding.** Circles represent PW (cm) for radiosondes at San Diego, California (blue), and Yuma, Arizona (black). Solid traces show GPS PW measurements at San Diego, California (blue), Durmid, California (red), Glamis, California (black), and Yuma, Arizona (dotted black). Arrows indicate the times of passage of an upper low at the identified GPS-Met sites. Map locates GPS stations with squares at San Diego (blue), Durmid (red), Glamis (black), and Yuma (dotted black), and radiosondes with circles at San Diego (blue) and Yuma (black). PW in mm at the GPS stations is shown, according to the color scale, at 1700 PDT 19 Jul (0000 UTC 20 Jul). Source: (Moore et al. 2015).

### 3.2 Nomenclature

The Level 1 ESDRs are referred to as “**raw troposphere delay**” time series. These ESDRs form the basis for the Level 2 “precipitable water vapor” time series.

### 3.3 Status

JPL 5-minute troposphere delay and PWV time series since 1992 uploaded to CDDIS and automatically updated weekly.

Need to replace GAMIT troposphere delay solutions (1-hour intervals) from ITRF2014 reprocessing completed in Year 3.

## 4. Level 3 Displacement Products

### 4.1 Description

*Definition:* Weekly updates of displacement products: 3-D Velocities, Coseismic, Postseismic

The analysis of the Level 2 displacement time series (section 2.1.6) results in estimated parameters that represent the different phases of the crustal deformation cycle (interseismic, coseismic, postseismic). The time series also include unmodeled effects of irregular uplift and subsidence, magmatism and other transient motions that may obscure the tectonic signals. Level 4 products include transient signals related to episodic tremor and slip (ETS) (section 7) and strain-rate grids (section 8), as well as hydrological signals (section 9).



**Figure 8:** An example of ITRF2004 horizontal velocities estimated from the combined time series of JPL and SIO. Significant ( $M > 6$ ) earthquakes denoted by red circles. This is a screen shot from MGviz.

### 4.2 Station Velocities

The 3-D station velocity estimates at each station (Figure 8) are a direct product of the time series analysis (section 2.1.6). The velocity is represented as the slope of the displacement time series

(equation 12 – parameter  $b$ ) where all offsets (coseismic and non-coseismic) and seasonal and postseismic effects have also been simultaneously modeled. A new velocity is produced weekly for each of the solution types, the combined, JPL and SIO time series, both unfiltered and filtered. Since the time series analysis is performed separately for each coordinate (NEU displacement), the 3D velocities are assumed to be uncorrelated (zero covariances). The velocity uncertainties are scaled according to Williams (2003) to take into account colored noise

$$\hat{\sigma}_b^2 \cong \frac{9b_k^2}{16\Delta T^2(N^2-1)}. \quad (20)$$

where  $n$  is the number of time series data points equally spaced in time,  $T$  is the total time span and  $b_k$  is the colored noise coefficient.

The horizontal and vertical velocities and their estimates can be viewed with MGviz.

Station motions may not be adequately modeled by a single velocity (Figure 6). There is a provision for assigning multiple velocities but we no longer use this option since it is quite subjective. We prefer to let the user examine the postfit residuals to study these transients.

The velocities are estimated in the ITRF (currently ITRF2014) rather than a regional frame such as the Stable North America Reference Frame (SNARF) (<https://www.unavco.org/projects/past-projects/snarf/snarf.html>) or a plate-fixed frame (e.g., Pacific plate). The velocities can then be transformed from ITRF to any other reference frame with the appropriate transformation parameters (e.g., plate parameters, Helmert transformation parameters). We plan to provide the option to transform the velocities to a plate-fixed frame, currently limited to North America and the Pacific since Western North America has been the focus of the project. With ESESES, we will review this approach.

### *Product details*

A single station velocities file is created every week in parallel with the displacement time series. They are extracted from the time series file headers of the unfiltered combined weighted mean product (combwm) (section 2.2). The files are stored at:

[http://garner.ucsd.edu/pub/measuresESESES\\_products/Velocities/](http://garner.ucsd.edu/pub/measuresESESES_products/Velocities/)

The file naming convention is:

ESESES\_velocities\_YYYYMMDD-combwm.txt

e.g., ESESES\_velocities\_20210920-combwm.txt

Older files are moved to the “previous” directory

For CDDIS the filename is

~/GPS\_Explorer/archive/Velocities/ ESESES\_velocities\_YYYYMMDD-combwm.txt

The file header contains the information on the contents of the file. Here is an example of the header with several velocities:

NASA MEaSUREs project: Extended Solid Earth Science ESDR System (ESESES)

Station velocities and uncertainties in mm/yr

Ellipsoidal height in meters

Derived from daily displacement time series - combined product (weighted mean)

Uncertainties include the effects of colored noise in daily time series

The north, east and up velocities are assumed to be uncorrelated

Note: Stations include a minimum of 2.5 years of data

Reference:

Bock, Y., Moore, A.W., Argus, D. F., Fang, P., Jiang, S., Kedar, S., Knox, S.A. Liu, Z. & Sullivan A. (2021),  
 Extended Solid Earth Science ESDR System (ES3): Algorithm Theoretical Basis Document: Chapter 4.2  
<http://sopac-csrc.ucsd.edu/wp-content/uploads/2021/08/ESESES-ATBD.pdf>

Site	Longitude	Latitude	Height	Nvel	Evel	Uvel	Nerr	Eerr	Uerr
7odm	242.906808	34.116407	762.06757	6.48	-27.31	0.92	0.11	0.16	0.25
ab01	185.795244	52.209505	25.46008	-22.73	-6.62	1.6	0.39	0.18	0.32
ab02	191.14533	52.970606	192.78532	-21.07	-7.99	1.5	0.17	0.15	0.26

### 4.3 Coseismic offsets

The weekly time series analysis (section 2.1.6) includes estimates of offsets (jumps, discontinuities) that can be due to sudden coseismic motions or data artifacts due to (mostly) antenna model changes, metadata errors, changes in reference frames, or unknown sources (e.g., Figure 3). The offsets are modeled as:

$$+ \sum_{j=1}^{n_g} g_j H(t_i - T_{g_j})$$

with magnitudes  $g$  of  $n_g$  offsets (jumps, steps, discontinuities) at epochs  $T_g$  (section 2.5). In this parameterization, we do not distinguish between coseismic and “non-coseismic” offsets, however, they are selected and identified in the headers of the time series files (section 2.2). Furthermore, non-coseismic offsets are estimated and corrected in the various time series products, while the coseismic offsets are not corrected in order that the time series reflect only physical motions of the stations. A particular earthquake may cause significant coseismic offsets at hundreds of stations for the largest earthquakes, for example, the 2019 Mw7.1 Ridgecrest earthquake displaced almost 300 stations (by >2-3 mm to about a meter) within a radius of about 250 km from its epicenter. Non-coseismic offsets mostly correlate with changes in antenna models although not all antenna changes will result in a visible offset. There have been efforts to automatically detect offsets in displacement time series used various algorithms but these are not foolproof and some user interaction is required through the administrator interface. In order to reduce the number of offset

parameters, current practice is to keep track of antenna changes and then determine visually if there is a significant offset to be estimated. Although, the IGS calibrates the absolute phase centers of all available geodetic-quality antennas, these are not perfect and may leave residual offsets in the displacement time series (see also section 2.1.5). Note that coseismic offsets may only be applied to horizontal components (N.E), while non-coseismic offsets are automatically applied to all three components. Also note, for daily displacement time series the offset is usually applied to the day after the recorded date if the antenna changed or earthquake occurred after 12:00 UTC.

### *Product details*

The coseismic offsets are extracted from the combwm time series file headers (section 2.1.10). The files are updated weekly and stored at:

[http://garner.ucsd.edu/pub/measuresESESES\\_products/CoseismicOffsets/](http://garner.ucsd.edu/pub/measuresESESES_products/CoseismicOffsets/)

The file naming convention is:

ESESES\_CoseismicOffsets\_YYYYMMDD-combwm.txt

e.g., ESESES\_CoseismicOffsets\_20210920-combwm.txt

Older files are moved to the “previous” directory

For CDDIS the filename is

~/GPS\_Explorer/archive/CoseismicOffsets/ESESES\_CoseismicOffsets\_YYYYMMDD-combwm.txt

Although there may not be a new earthquake every week, sometimes we will add coseismic offsets for particular events as the time series grow. Therefore, for simplicity we create a weekly update. Furthermore, the offsets are re-estimated every week.

The coseismic product should identify the number of stations affected by particular earthquakes (events). Therefore, the file is sorted by date and then by site. It is unusual to have two separate effects occur on the same date – this can be addressed by checking the geographic locations of the stations. The steps are:

- (1) Sort coseismic offsets by date
- (2) Check that they are in the same geographic location
- (3) Look up table of earthquakes and add header for each event
- (4) Sort event by coseismic offset (sum of squares of three components)

The coseismic offsets file header contains the information on the contents of the file. Here is an example of a header:

NASA MEaSURES project: Extended Solid Earth Science ESDR System (ESESES)  
Derived from daily displacement time series - combined product (weighted mean)  
The coseismic offsets are sorted by earthquake (event)  
The north, east and up offsets are assumed to be uncorrelated

Reference:

Bock, Y., Moore, A.W., Argus, D. F., Fang, P., Jiang, S., Kedar, S., Knox, S.A. Liu, Z. & Sullivan A. (2021),  
Extended Solid Earth Science ESDR System (ES3): Algorithm Theoretical Basis Document: Section 4.3  
<http://sopac-csrc.ucsd.edu/wp-content/uploads/2021/08/ESESES-ATBD.pdf>

Station coseismic offsets and uncertainties in mm

Ellipsoidal height in meters; latitude and longitude (East) in decimal degrees

Site Latitude Longitude Height Date YYYY-MM-DDD Noffset Eoffset Uoffset Nerr Eerr Uerr

The estimated coseismic offsets and their uncertainties estimates can be viewed with MGviz.

#### 4.4 Postseismic parameters

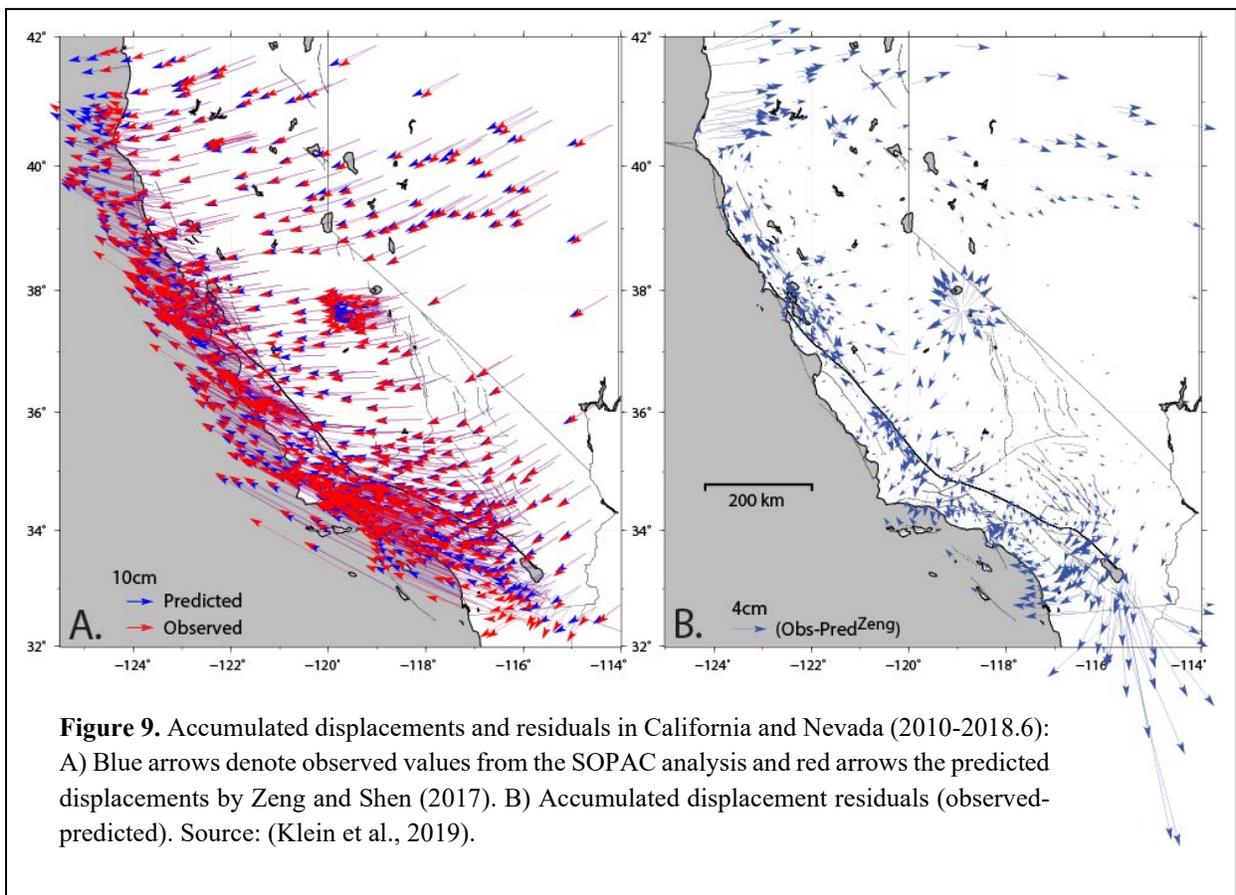
**Enter URL**

## 5. Level 3: Displacement Fields (Grids)

### 5.1 Background

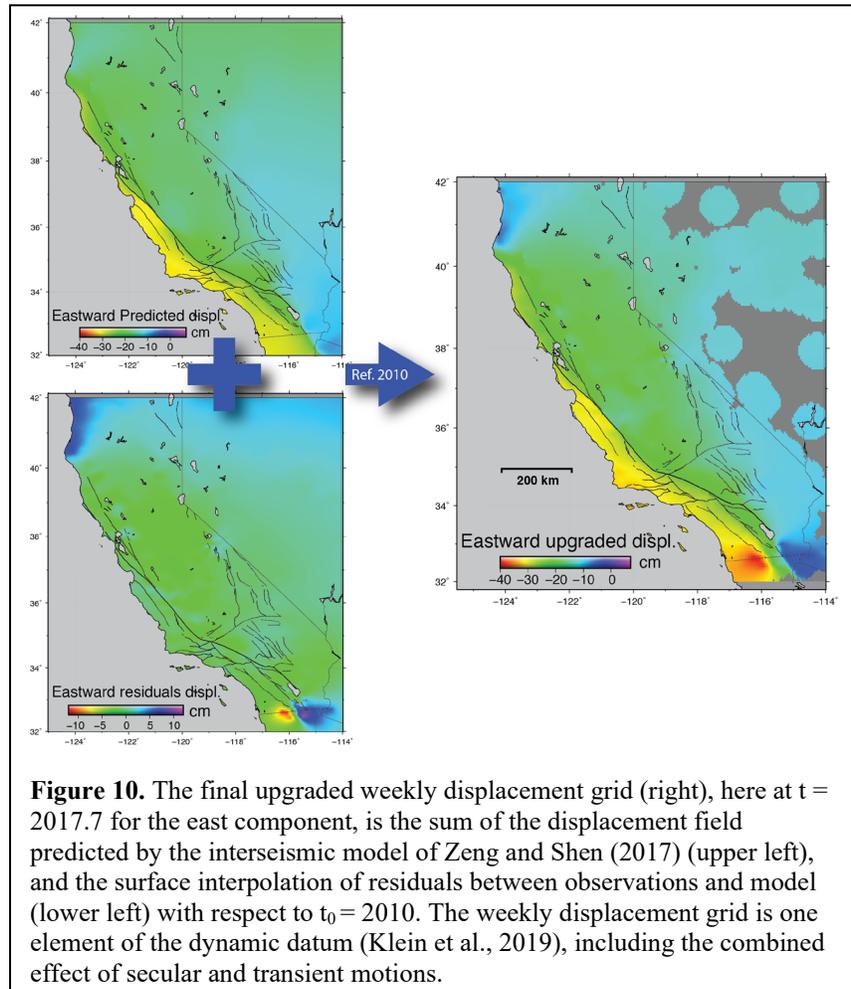
*Definition:* Automated weekly update of horizontal and vertical displacement grids

The Level 2 displacement time series provide a record of horizontal and vertical transient motions over and above secular, long-term processes such as interseismic deformation, represented by station velocities (Figure 9). The transient motions include coseismic and postseismic motions from earthquakes, magmatic deformation at Long Valley Caldera (e.g., Liu et al., 2011), subsidence in California’s San Joaquin Valley (Argus et al., 2017), and episodic tremor and slip (ETS) in Cascadia (Rogers and Dragert, 2003). Transients other than coseismic and postseismic deformation are not modeled as part of the time series analysis (section 5.1). The detection of transients is important in fault slip modeling and assessing seismic risk and is the basis of the Level 4 ESDRs (section 7).



## 5.2 Methodology: Horizontal Displacement Fields

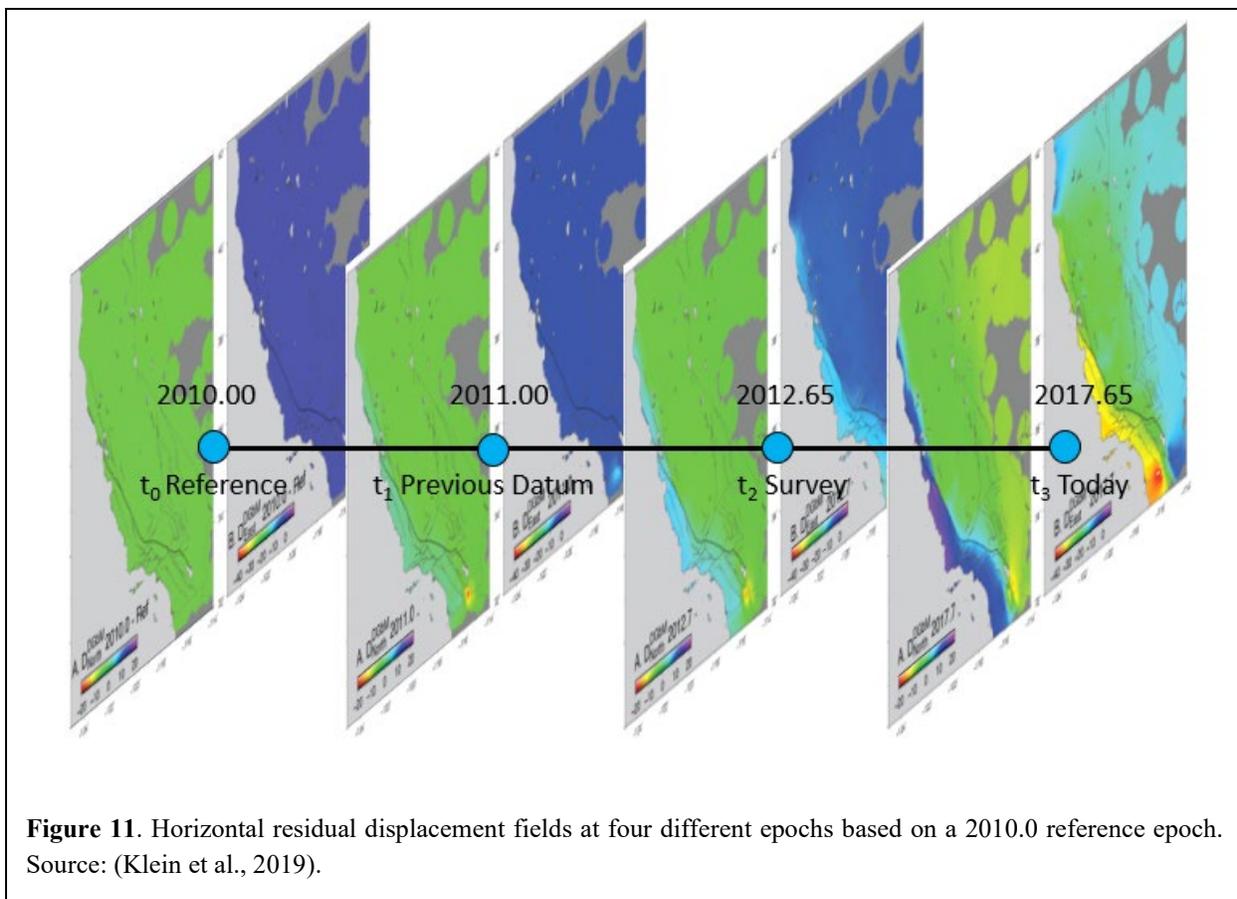
The station displacements corrected for non-coseismic offsets (section 2.1.5) are interpolated on a weekly basis to generate an updated displacement field (grid). Direct interpolation of the observed horizontal displacements is not optimal in the near-field of active geologic faults, where elastic deformation is occurring and the number and spatial distribution of stations is lacking. Therefore, we supplement our Level 2 displacements with displacements predicted by forward modeling the secular horizontal fault slip model of Zeng and Shen (2017) for the western U.S. that takes into account fault geometry and slip rates. Their model is derived from survey-mode and cGPS data supplemented by geologic slip rates. The residuals in Figure 10 are defined as the difference between the observed weekly station displacements minus the geologic-based model-predicted displacements and reflect transient motions (Klein et al., 2019). In Figure 9B, we show the accumulated transient displacements from an arbitrary initial epoch 2010.0 to 2018.6 compared to the secular model, showing the effects of postseismic deformation, subsidence, magmatism, as well as deviations from the Zeng and Shen (2017) secular model.



First, we use a median filter to create a weekly time series. Then, the interpolation of the horizontal displacement residuals is accomplished using a remove/interpolate/restore approach as follows:

- (1) Construct north and east horizontal displacement 1 km grid spacing at some time  $t$  after a reference epoch (for demonstration purposes we use  $t_0 = 2010.00$  – Figure 11) by multiplying Zeng and Shen (2017) surface velocity map by  $t - t_0$ .

- (2) Subtract the model displacements from the observed displacements (residuals) at the reference stations in north and east directions. We assume here that the residuals will be smooth so they have spatial variations at length scales greater than the spacing of the cGPS sites ( $> 10$  km).
- (3) Interpolate the north and east residuals (modeled minus predicted displacements) at a 1 km grid spacing using a 2-D elastic model to provide coupling between the two horizontal components (Haines & Holt, 1993; Haines et al. 2015; Sandwell & Wessel, 2016). This is accomplished using *gpsgridded* in the GMT software (<https://www.soest.hawaii.edu/gmt/>) where one quarter of the number of eigenfunctions are compared with the number of data points; the residual grid fits the displacement residuals to within their uncertainties.
- (4) Add the residual grid to the ZS2017 displacement model to achieve the final horizontal displacement grids, with 1 km spatial resolution.

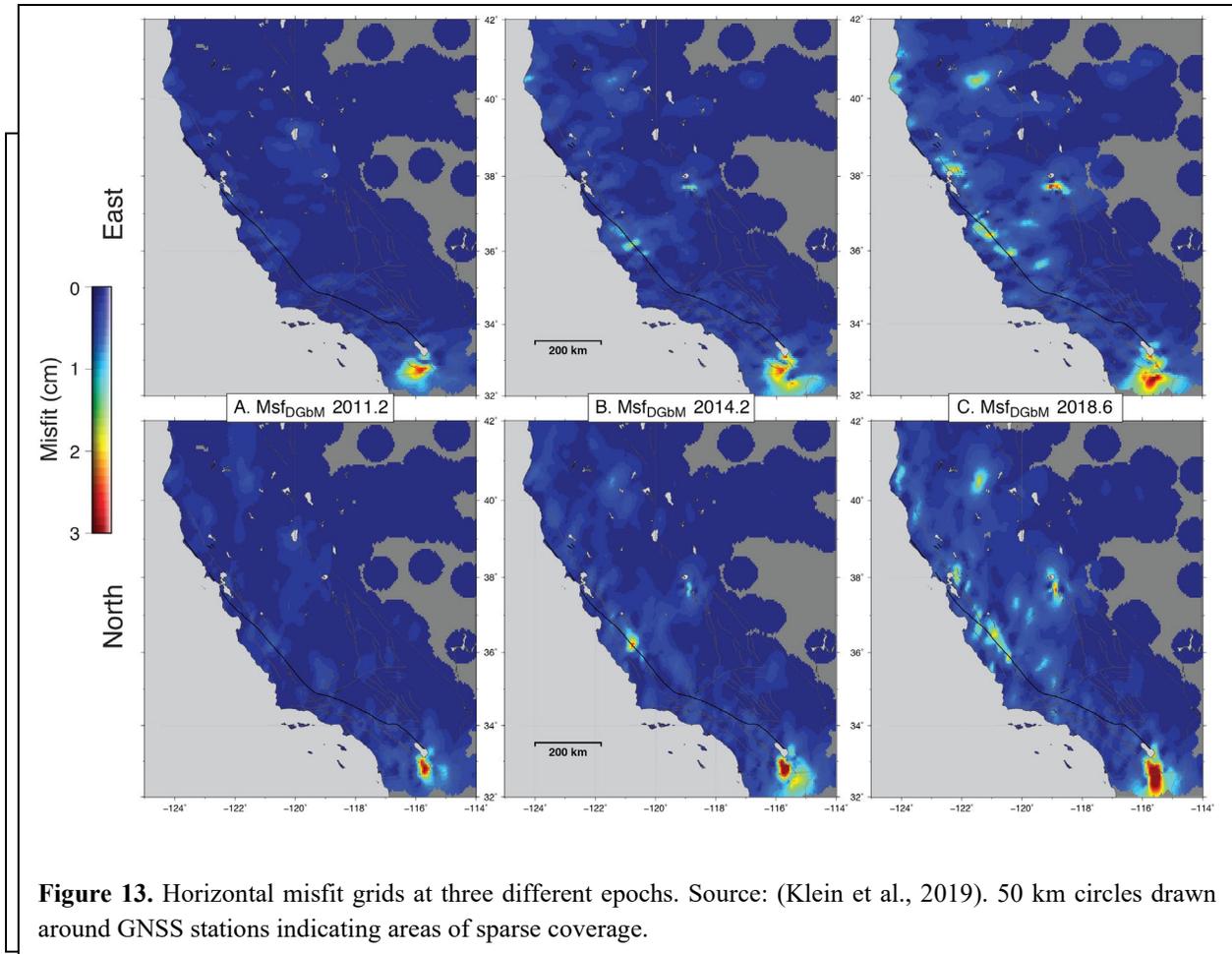


The grids now contain the total motion accumulated since the initial epoch, that is, the predicted secular motions plus the observed transient motions (Figure 10). Each week's displacement field is stored in the SOPAC archive. Horizontal displacement fields from 4 epochs are shown in Figure 11. Moving between different epochs provides the basis of a dynamic datum (reference frame) (Klein et al., 2019).

In addition to the total displacement grids, we also create grids of the residual displacements representing the transient motions, tables of input data at the reference stations and movies that highlight the time evolution of each product. One product shows the non-accumulating weekly residual motions so that effects such as postseismic motions will appear to dissipate in time.

### 5.3 Vertical Displacements

For the vertical component, we spatially interpolate the vertical displacements without the use of an underlying model as described by Klein et al. (2019). In Figure 12 we show the accumulated



vertical displacements between 1999.5 and 2018.6 in California and Nevada. The accumulated weekly vertical displacement maps, tables and movies are also archived on a weekly basis.

### 5.4 Misfits

The misfits between the observed displacements and those interpolated from the displacement fields at the reference stations provide a measure of uncertainty at any location within the area of interest (here in California and Nevada) in the horizontal (Figure 13) and, similarly for the vertical

components. They are created by comparing the observed displacements and the interpolated displacements at the reference stations, and gridding the results. The misfit fields are also archived on a weekly basis.

## 5.5 Products

The input to the displacement products is weekly median values of daily displacements time series (although the resolution could be modified for special cases), updated weekly and uploaded to CDDIS (Table 3). The movies described in Table 4 provide the user with a powerful visual representation of crustal motions over time.

The .grd files are a type of netCDF file built within the GMT environment and hold all the displacement data values for each epoch of time for each given grid type. These can be used within GMT (<https://docs.generic-mapping-tools.org/latest/>), as well as other software types (e.g., GDAL, MATLAB).

YYYYMMDD indicates end date of the weekly grid

**Table 3. Displacement Products**

<b>Dynamic Datum</b>	
<b>Horizontal</b>	
<b>Vectors</b>	<b>Description</b>
dispNVec_YYYYMMDD.pdf	Interseismic model + horizontal (NE) transients = accumulating total displacements since t0 (input to dynamic datum grids): Note: This shows the total motions so may partially obscure in time the transient motions and vice versa.
<b>Grids</b>	
dispNgrid_YYYYMMDD.pdf/grd; dispEgrid_YYYYMMDD.pdf/grd	Gridded North/East total displacements accumulating since t0. Zeng and Shen (2017) prediction [ucerf3_0.05_itrf_v*.grd] + surface interpolation of residuals between observations and model; Areas >75 km from GPS stations are masked.
misfitNgrid_YYYYMMDD.pdf/grd; misfitEgrid_YYYYMMDD.pdf/grd	Gridded North/East accumulating misfits, > 75 km mask. Gridded point values of displacements compared to interpolated values at reference stations.
<b>Residuals</b>	
residualNgridM_YYYYMMDD.pdf/grd; residualEgridM_YYYYMMDD.pdf/grd	Median North and East residuals between observed GNSS motions and Zeng and Shen (2017) interseismic predicted model motions
<b>Data Tables</b>	
dispNEgrid_YYYYMMDD.dat	North and East dynamic datum observations and predictions (FORMAT: lon; lat; NobsTotal; EobsTotal; NpredDynDat; EpredDynDat). Total displacements and dynamic datum
misfitNEgrid_YYYYMMDD.dat	North and East misfits dynamic datum observations and prediction (FORMAT: lon; lat; NobsTotal; EobsTotal; misfitNpredDynDat; misfitEpredDynDat). Total displacements and dynamic datum
residualNEgridM_YYYYMMDD.dat;	Median North and East residuals between observed GNSS motions and Zeng and Shen (2017) interseismic predicted model motions (FORMAT: lon; lat; Nresid; Eresid).
<b>Vertical</b>	
<b>Vectors</b>	<b>Description</b>
dispUvec_YYYYMMDD.pdf	Up displacements accumulating since t0

<b>Grids</b>	
dispUgrid_YYYYMMDD.pdf/grd	Gridded up displacements accumulating since t0; >75 km mask.
misfitUgrid_YYYYMMDD.pdf/grd	Gridded Up of accumulating computed misfits, > 75 km mask. Gridded <u>absolute values</u> of residuals between dynamic datum displacements compared to interpolated values at reference stations.
<b>Residuals</b>	
residualUvec_YYYYMMDD.pdf/grd	Residuals between point value at station and interpolated grid value. <b>Note:</b> Corresponds to residualUgrid
residualUgrid_YYYYMMDD.pdf/grd	Gridded Up residuals between point value at reference station and interpolated grid values (observation - interpolated value). <b>Note:</b> misfitUgrid*.grd calculated using these values; see residualUvec*.dat data tables for station point values.
<b>Data Tables</b>	
dispUgrid_YYYYMMDD.dat	Observed up displacements and predicted up displacement from the green spline interpolation (FORMAT: lon; lat; measured; predicted).
residualUvec_YYYYMMDD.dat	Residual up values between observed displacement and the interpolated predicted values (FORMAT: lon; lat; Residual).
<b>Horizontal Transients</b>	
<b>Vectors</b>	<b>Description</b>
transientNEvec_YYYYMMDD.pdf	Horizontal transients (observed – predicted from interseismic model) accumulating since t0 at reference stations. Shows non-steady state transient deformation processes (postseismic deformation, creep, magmatic activity, etc.); transient portion of the dynamic datum. <b>Note:</b> components are gridded to transientNgrid and transientEgrid
transientNEvecW_YYYYMMDD.pdf	Horizontal weekly ( <b>W</b> ) transients (observed – predicted from interseismic model) non-accumulating since t0 at reference stations. Weekly non-steady state transient deformation processes (postseismic deformation, creep, magmatic activity, etc.) – postseismic transients, for example, will dissipate over time. <b>Note:</b> components are gridded to transientNgridW and transientEgridW
<b>Grids</b>	
transientNgrid_YYYYMMDD.pdf/grd; transientEgrid_YYYYMMDD.pdf/grd	Gridded North/East transients between observed and long-term interseismic model at the reference stations (accumulating). <b>Note:</b> Corresponds to transientNEvec
transientNgridW_YYYYMMDD.pdf/grd; transientEgridW_YYYYMMDD.pdf/grd	Gridded North/East weekly ( <b>W</b> ) transients between observed and predicted interseismic model at the reference stations (non-accumulating). <b>Note:</b> Corresponds to transientNEvecW
<b>Data Tables</b>	
transientNEgrid_YYYYMMDD.dat	North and East observed displacements and interseismic model predictions accumulating (FORMAT: lon; lat; NobsTotal; EobsTotal; NpredModelDat; EpredModelDat). Separate components of dynamic datum
transientNEgridW_YYYYMMDD.dat	North and East observed displacements and total interseismic model predictions non-accumulating ( <b>W</b> ) weekly (FORMAT: lon; lat; NobsTotal; EobsTotal; NpredModelDatW; EpredModelDatW). Separate components of dynamic datum (weekly)

**Table 4. Displacement Movies**

Movie Name	Description
<b>Dynamic Datum</b>	
<b>Vectors</b>	
dispNEvec_YYYYMMDD.mp4	Dynamic Datum horizontal
dispUvec_YYYYMMDD.mp4	Dynamic Datum up
residualNEvec_YYYYMMDD.mp4	Residual North and East vectors (accumulating)
residualUvec_YYYYMMDD.mp4	Residual vectors (U); difference of reference station values and interpolated values (accumulating)
<b>Grids</b>	
dispNgrid_YYYYMMDD.mp4; dispEgrid_YYYYMMDD.mp4; dispUgrid_YYYYMMDD.mp4	Dynamic data grids North, East, Up
misfitNgrid_YYYYMMDD.mp4; misfitEgrid_YYYYMMDD.mp4; misfitUgrid_YYYYMMDD.mp4	Dynamic data grid misfits North, East, Up
<b>Transients</b>	
<b>Vectors</b>	
transientNEvec_YYYYMMDD.mp4	Transient North East vectors (accumulating)
transientNEvecW_YYYYMMDD.mp4	Transient North East vectors weekly (non-accumulating)
<b>Grids</b>	
transientNgrid_YYYYMMDD.mp4; transientEgrid_YYYYMMDD.mp4	Transient grids (accumulating) North, East
transientNgridW_YYYYMMDD.mp4; transientEgridW_YYYYMMDD.mp4	Transient grids (non-accumulating) North, East

### 5.6 Archive Structure

File sent to CDDIS: **DisplacementGridsYYYYMMDD.tar.gz**

YYYYMMDD is the date that the file was created

SOPAC archive location:

[http://garner.ucsd.edu/pub/measuresESESES\\_products/DisplacementGrids](http://garner.ucsd.edu/pub/measuresESESES_products/DisplacementGrids)

#### Readme.txt

```
dynamic datum >
  vector_products >
    horizontals >
      dispNEvec_YYYYMMDD .pdf
```

```

residualNgridM_YYYYMMDD .pdf
residualEgridM_YYYYMMDD.pdf
residuals >
    residualNgridM_YYYYMMDD.pdf
    residualEgridM_YYYYMMDD.pdf
data_tables >
    dispNEgrid_YYYYMMDD.dat
    misfitNEgrid_YYYYMMDD.dat
    residualNEgrid_YYYYMMDD.dat
verticals >
    dispUvec_YYYYMMDD.pdf
residuals >
    residualUvec_YYYYMMDD.pdf
data_tables >
    dispUgrid_YYYYMMDD.dat
    residualUvec_YYYYMMDD.dat
gridded_products >
    horizontals >
        dispNgrid_YYYYMMDD.pdf/grd
        dispEgrid_YYYYMMDD.pdf/grd
        misfitNgrid_YYYYMMDD.pdf/grd
        misfitEgrid_YYYYMMDD.pdf/grd
        residuals >
            residualNgridM_YYYYMMDD.pdf/grd
            residualEgridM_YYYYMMDD.pdf/grd
        verticals >
            dispUgrid_YYYYMMDD.pdf/grd
            misfitUgrid_YYYYMMDD.pdf/grd
        residuals >
            residualUgrid_YYYYMMDD.pdf/grd
    transients >
        vector_products >
            horizontals >
                transientNEvec_YYYYMMDD.pdf/grd
                transientNEvecW_YYYYMMDD.pdf/grd
            data_tables >
                transientNEgrid_YYYYMMDD.dat
                transientNEgridW_YYYYMMDD.dat
        gridded_products >
            horizontals >
                transientNgrid_YYYYMMDD.pdf/grd
                transientEgrid_YYYYMMDD.pdf/grd
                transientNgridW_YYYYMMDD.pdf/grd
                transientEgridW_YYYYMMDD.pdf/grd
    movies >
        dynamic_datum >
            vectors >
                dispNEvec_YYYYMMDD.mp4

```

dispUvec\_YYYYMMDD.mp4  
residualNEvec\_YYYYMMDD.mp4  
residualUvec\_YYYYMMDD.mp4

**gridded >**

dispNgrid\_YYYYMMDD.mp4  
dispEgrid\_YYYYMMDD.mp4  
dispUgrid\_YYYYMMDD.mp4  
misfitNgrid\_YYYYMMDD.mp4  
misfitEgrid\_YYYYMMDD.mp4  
misfitUgrid\_YYYYMMDD.mp4

**transients >**

**vectors >**

transientNEvec\_YYYYMMDD.mp4  
transientNEvecW\_YYYYMMDD.mp4

**gridded >**

transientNgrid\_YYYYMMDD.mp4  
transientEgrid\_YYYYMMDD.mp4  
transientNgridW\_YYYYMMDD.mp4  
transientEgridW\_YYYYMMDD.mp4

## 6. Level 3: High-Rate GNSS & Seismogeodetic Records for Historical Earthquakes

### 6.1 Background

Our level 1 products include daily GNSS displacements based on 24-hours of data, typically sampled at 15 seconds. Another product is high-rate, typically 1-10 Hz, displacements. The analysis of high-rate GNSS data is referred to as “GNSS seismology” since it can also sense dynamic motions generated by, for example, earthquakes in addition to high-rate displacements (Bock and Melgar, 2016 and references therein). “Coseismic” refers to motions during an earthquake that are a superposition of dynamic displacements and static (permanent) displacements. A comprehensive archive of GPS high-rate displacements of 29 earthquakes from 2003-2018 with moment magnitudes of Mw 6.0-9.0 is described by (Ruhl et al., 2019). However, the sensitivity of seismic instruments to ground motions is much higher than that of GNSS, which cannot sense the arrival of low-amplitude (sub mm) seismic P waves even in the near field of a great earthquake. GNSS networks have captured large amplitude teleseismic waves (seismic signals greater than about a thousand kilometers from an earthquake’s location). However, at these distances dynamic GNSS displacements are only accurate enough to discern S waves from large earthquakes ( $\sim M > 7.5$ ), while traditional seismic measurements at any location on Earth can resolve earthquakes as small as  $> M 5.3$ , a factor of 1000 better than geodesy. “Seismogeodesy,” the optimal combination of collocated high-rate GNSS and seismic (strong motion accelerometer) data, provides coseismic (static and dynamic) displacements and seismic velocities that can detect P waves. Table 5 shows earthquakes that have been observed with GPS seismology and seismogeodesy through 2019. A review of GNSS seismology and seismogeodesy is provided by Bock and Melgar (2016) and Bock and Wdowinski (2020), and references therein.

**Table 5.** Significant earthquakes measured with GPS seismology and seismogeodesy

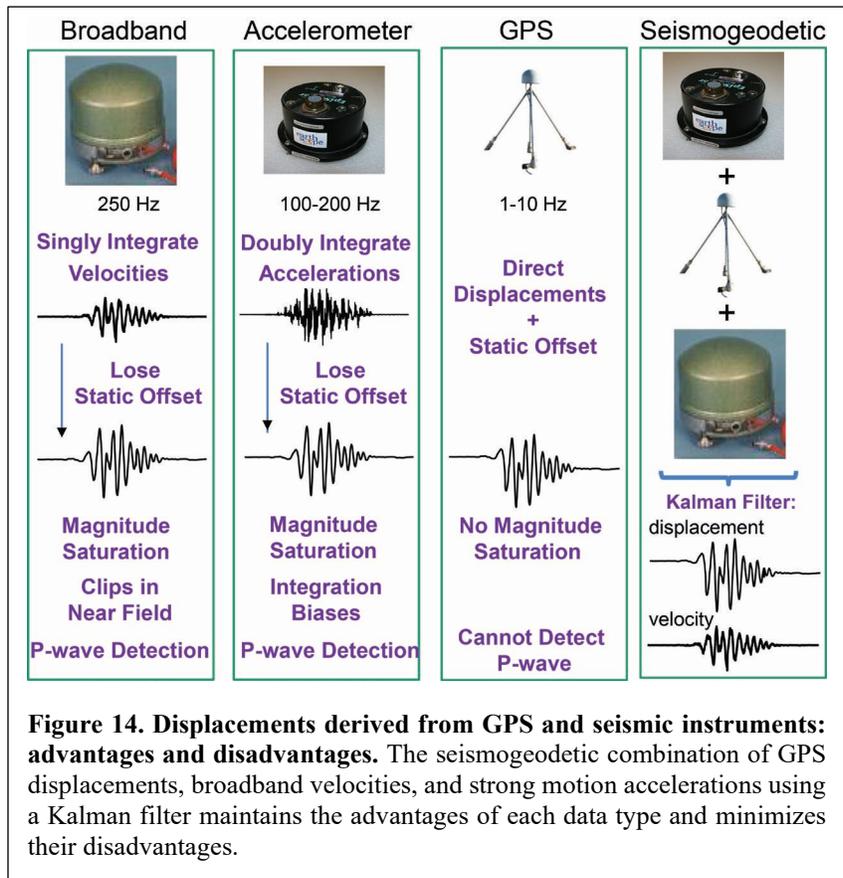
Earthquake	Mw	References
2002 Denali fault, Alaska (teleseismic – 4000 km from source)	7.9	(Larson et al. 2003; Kouba 2003; Bock et al. 2004)
2003 San Simeon, California	6.6	(Ji et al. 2004)
2003 Tokachi-oki, Japan <sup>1</sup>	8.3	(Miyazaki et al. 2004; Emore et al. 2007; Crowell et al. 2009; Crowell et al. 2012)
2004 Parkfield, California	6.0	(Langbein et al. 2005; Barbot et al. 2009)
2004 Sumatra-Andaman, Indonesia (teleseismic – 14,000 km from source)	9.3	(Davis and Smalley 2009)
2005 West Off Fukuoka Prefecture, Japan	7.0	(Kobayashi et al. 2006)
2008 Wenchuan, China	8.0	(Yin et al. 2013)
2010 Mentawai, Indonesia	7.7	(Melgar et al. 2015)
2010 Maule, Chile <sup>1</sup>	8.8	(Melgar et al. 2015) (Yue et al. 2014)
2010 El Mayor-Cucapah, Mexico <sup>1</sup>	7.2	(Crowell et al. 2012)

2011 Tohoku-oki, Japan <sup>1</sup>	9.0	(Crowell et al. 2012) (Melgar et al. 2013; Bletery et al. 2014) (Grapenthin and Freymueller 2011 - teleseismic)
2012 Nicoya, Costa Rica	7.5	(Melgar et al. 2015) (Yin and Wdowinski 2014)
2014 Napa, California <sup>1</sup>	6.1	(Melgar et al. 2015)
2014 Aegean Sea, Greece	6.5	(Melgar et al. 2015)
2014 Iquique, Chile	8.2	(Melgar et al. 2016)
2015 Illapel, Chile <sup>1</sup>	8.3	(Melgar et al. 2016)
2016 Kumamoto, Japan <sup>1</sup>	7.0	(Kawamoto et al. 2016)
2016 Kaikoura, New Zealand	7.8	(Kaiser et al. 2017)
2017 Chiapas, Mexico <sup>1</sup>	8.2	(Ye et al. 2017)
2019 Ridgecrest, California earthquakes <sup>1</sup>	6.2/7.1	(Xu et al., 2019)

<sup>1</sup>Sufficient GPS/accelerometer collocations available for seismogeodesy

GPS seismology and seismogeodesy are particularly advantageous in the near field (within 100’s of km) of large earthquakes, for local earthquake and tsunami warning and rapid response. Figures 14 and 15 indicates the advantages and disadvantages of seismic (broadband seismometers, strong-motion accelerometers) and geodetic (GPS/GNSS) instruments compared to the seismogeodetic combination. Broadband

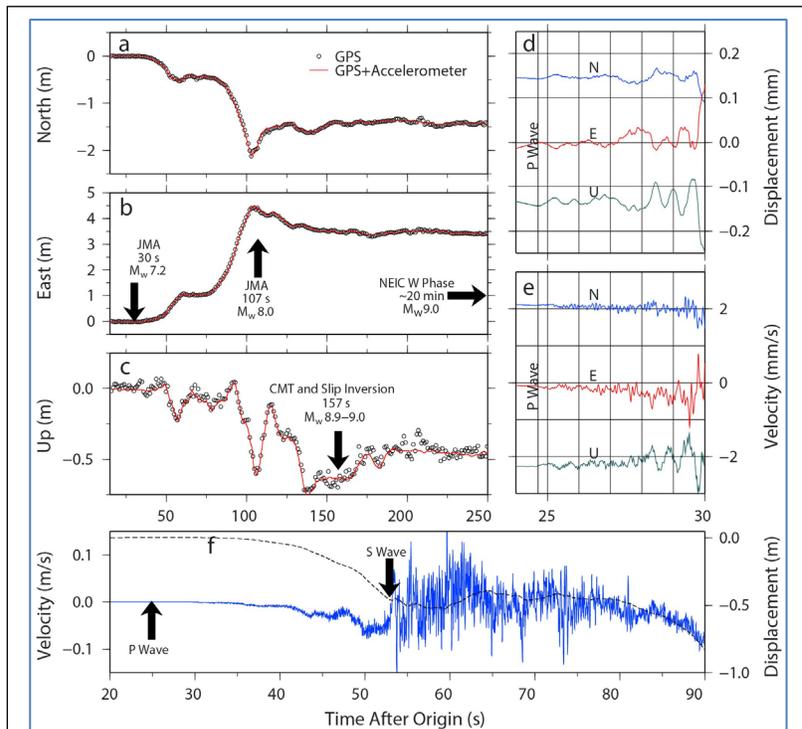
seismometers that measure ground velocities go off-scale (“clip”) when close to an earthquake’s epicenter, while GPS does not. Therefore, seismic stations are equipped with strong-motion instruments (accelerometers) that do not clip. Absolute station displacement is the most useful measurement for down-stream modeling of the earthquake source, but seismology requires single integration of observed broadband velocities or a double integration of accelerations. The accuracy of absolute displacements from broadband seismometers is poor because of its limits in dynamic range. Doubly-integrating accelerations to displacements is subject to various spurious



**Figure 14. Displacements derived from GPS and seismic instruments: advantages and disadvantages.** The seismogeodetic combination of GPS displacements, broadband velocities, and strong motion accelerations using a Kalman filter maintains the advantages of each data type and minimizes their disadvantages.

breaks, termed “baseline” errors (not to be confused with GNSS baselines), due to numerical errors in the integration procedure, mechanical hysteresis, and cross-axis sensitivity between the test mass/electromechanical system used to measure each component of motion. The main disadvantage is that accelerometers are incapable of discerning between rotational and translational motions, leading to unphysical drifts in the resulting displacements. Baseline corrections are usually taken into account by a high-pass filter, resulting in accurate recovery of the mid- to high-frequency portion of the displacement record. However, in the process long-period information in particular the static offset is lost. The static offset (permanent motion) is critical for rapid estimation of earthquake magnitude and mechanism, an essential element for earthquake and tsunami early warning. Finally, unlike GNSS, seismic instruments are subject to magnitude saturation, meaning that is not possible to distinguish between, say, a magnitude 8 and 9 earthquake (a factor of about 30 in energy release), since the scaling relationships between seismic wave arrivals and earthquake magnitude break down at the higher magnitudes.

For earthquake early warning where timely near-source observations are critical, GNSS is not sensitive enough to detect seismic P-waves, particularly in the vertical direction where the P-wave with mm-level amplitudes is most pronounced; the precision of real-time GPS instantaneous displacements is about 1 cm in the horizontal components and 5-10 cm in the vertical (Genrich and Bock 2006). The displacement precision observed with seismogeodesy during dynamic shaking is reduced by a factor of two in the vertical and by about 20% in the horizontal component, compared to GPS alone, though



**Figure 15. Demonstration of the utility of GNSS and seismogeodetic data for rapid earthquake and tsunami warning systems.** 3-D seismogeodetic displacements and velocities estimated from 1 Hz GPS displacements at Japan’s GEONET station 0914 (black circles) and 100 Hz K-NET accelerometer MYG003, 155 km from the earthquake’s epicenter determined by the Japan Meteorological Agency. The Japanese earthquake early warning system, dependent on regional seismic station data, estimated an initial magnitude of Mw7.2, 30 seconds after earthquake onset time and Mw8.0 after 107 seconds, a classic example of magnitude saturation. Replay of the event with seismogeodetic data or GNSS data alone (black circles) indicates that a magnitude of Mw8.9-9.0 within 157 seconds. The seismogeodetic data also allows the P wave to be detected as a basis for earthquake early warning. Rapid and accurate magnitude estimation is key for issuing tsunami early warnings. Source: (Melgar et al. 2013).

still dominated by long-period errors in the GPS observations due to multipath (Saunders et al. 2016). Since the dynamic range of GPS instruments has no upper limit, GPS and broadband seismic sensors cover together the entire possible range of dynamic and static surface displacement (up to the Nyquist frequency). A study comparing the displacements and seismic velocities obtained with observatory-grade accelerometers and inexpensive Microelectromechanical (MEMS) accelerometers demonstrated the same level of precision in seismic velocity at distances of tens of km for earthquakes as small as  $\sim M4$ , where there is no permanent displacement (Saunders et al. 2016; Goldberg and Bock 2017).

## 6.2 Description of ESDR

The preferred analysis for GPS seismology is the method of precise point positioning (PPP) (Zumberge et al., 1997; Kouba et al., 2001) since it is performed with respect to a global reference frame rather than relative positioning, which requires base stations that may be in the zone of deformation of a large earthquake. As in our daily displacement Level 1C ESDRs, JPL and SIO use different PPP software. JPL uses the GipsyX software (<https://gipsy-oasis.jpl.nasa.gov/index.php?page=software>) and SIO uses a variation of the PANDA software (Geng et al., 2012), the PRIDE PPP\_AR software (<http://pride.whu.edu.cn>; <http://igs.gnsswhu.cn/pub/whu/phasebias/>) from Wuhan University (not the GAMIT software used for earlier ESDRs).

- (1) Using a common source of metadata from the SOPAC archive, the two groups will independently analyze the historical record of GPS/GNSS data collected during significant earthquakes and any new earthquakes during the project period to produce a time series of high-rate displacements. These data will be supplemented from data archived at other centers. Although the data were collected in real time, the PPP analysis will be performed in 24-hour batches and a solution will include 1 Hz displacement spanning a day (i.e., 86,400 samples). If data are available at a higher rate (PBO stores data collected at 10 Hz for large events within their zone of coverage), we will analyze the data at the higher rates (up to 864,000 samples per day). Of course, one can then average the high-rate solutions to any sub-daily interval to study other phenomena. We will include data from one full day before to three full days after each event, that is, if the earthquake occurs at mid-day on day  $x$ , then a full day of data will be collecting for  $x-3$  and  $x+3$ . SOPAC maintains an archive of relevant high-rate data from stations in the Western U.S. to capture the early postseismic period.
- (2) SIO will also process data from collocated seismic (accelerometer) and GNSS stations using the seismogeodetic approach (Bock et al., 2011; Saunders et al., 2016); Goldberg and Bock, 2017) (Figure 18) for historical events and new events occurring over the project period. High-rate displacements and seismic velocities will be estimated at the sampling rate of the seismic instruments (typically, 100 Hz).
- (3) The high-rate GNSS and seismic displacements and the raw data will be archived at SOPAC and at the CDDIS DAAC for use by other investigators.

### 6.3 Products

Our products are delivered to the CDDIS in a tar file, *EarthquakeDisplacements\_MEaSURES\_ESESES\_YYYYMMDD* that is updated with the most recent significant earthquakes. *YYYYMMDD* is the date of the most recent submission.

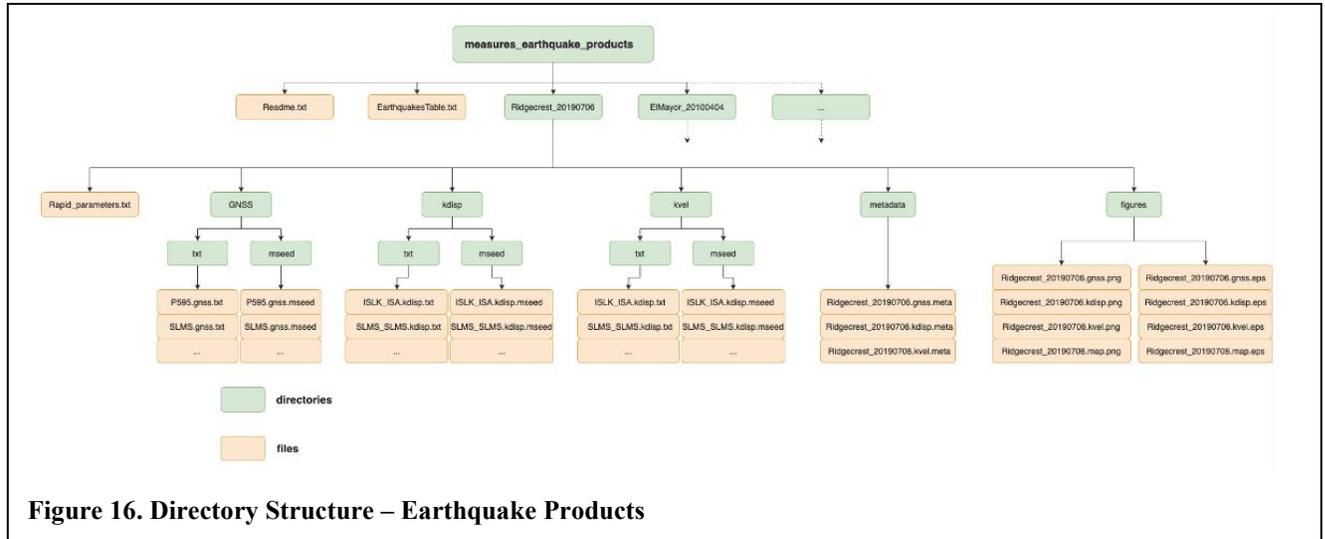


Figure 16. Directory Structure – Earthquake Products

### SOPAC archive directory

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/](http://garner.ucsd.edu/pub/measures_earthquake_products/)

### File Descriptions

- (1) Readme.txt – this file (top level)
- (2) EarthquakesTable.txt (top level)

earthquakeName(\_Solution) examples (name\_YYYYMMDD):

Ridgecrest\_20190706  
 Ridgecrest\_20190706\_2  
 Parkfield\_20040928  
 Tohoku\_20110311

Note: these names refer to a particular high-rate analysis of an earthquake rather than the earthquake itself. For example, there could be a 2<sup>nd</sup> analysis by a different research group. In the directory structure we would specify a second file, Ridgecrest\_20190706\_2 or another designation after the underscore instead of “2”.

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/EarthquakesTable.txt](http://garner.ucsd.edu/pub/measures_earthquake_products/EarthquakesTable.txt)

### Example:

# Event Name;Country;Mw;Origin Time (UTC);Latitude(deg. N);Longitude (deg. E);Depth (km);Mechanism;GNSS Stations;Collocated stations;GNSS processing

Ridgecrest\_20190706;United States;7.1;2019\_07\_06T03:19:53.0;35.770;-117.599;8.0;StrikeSlip;490;91;PPP

Second level (See Directory Structure figure):

(3) “metadata” (text file) (third level)

### Examples of Metadata Files

*GNSS Only Displacements Ridgecrest\_20190706.gnss.meta*

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/metadata/Ridgecrest71.gnss.meta](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/metadata/Ridgecrest71.gnss.meta)

# GNSS Network;GNSS Station;Latitude (N);Longitude (E);Elevation (m);Sampling Rate (Hz);Gain;Units

NOTA;BBDM;34.582201;-119.981518;204.885800;1.00;1000.00;counts/m

*Seismogeodetic Displacements (Ridgecrest\_20190706.kdisp.meta)*

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/metadata/Ridgecrest71.kdisp.meta](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/metadata/Ridgecrest71.kdisp.meta)

# GNSS Network;GNSS Station;Latitude (N);Longitude (E);Elevation (m);Sampling Rate (Hz);Gain;Units;Seismic Network  
;Seismic Station;Latitude (N);Longitude (E);Elevation (m)

NOTA;SONG;33.380750;-117.560270;23.000000;100.00;1000.00;counts/m;CI;SOC;33.387610;-117.5801;52.000000

*Seismogeodetic Velocities (Ridgecrest\_20190706.kvel.meta)*

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/metadata/Ridgecrest71.kvel.meta](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/metadata/Ridgecrest71.kvel.meta)

# GNSS Network;GNSS Station;Latitude (N);Longitude (E);Elevation (m);Sampling Rate (Hz);Gain;Units;Seismic  
Network;Seismic Station;Latitude (N);Longitude (E);Elevation (m)

NOTA;SONG;33.380750;-117.560270;23.000000;100.00;1000.00;counts/(m/s);CI;SOC;33.387610;-  
117.580130;52.000000

(4) “figures” directory (figures are available in PNG and EPS formats)

*GNSS displacements:*

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/figures/Ridgecrest71.gnss.png](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/figures/Ridgecrest71.gnss.png)

*Seismogeodetic displacements (Figure 17)*

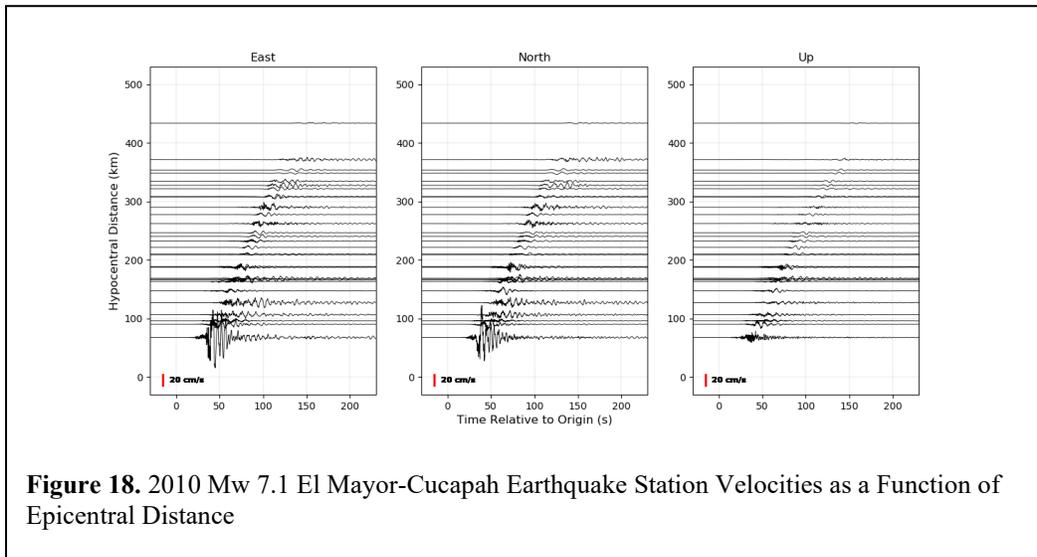
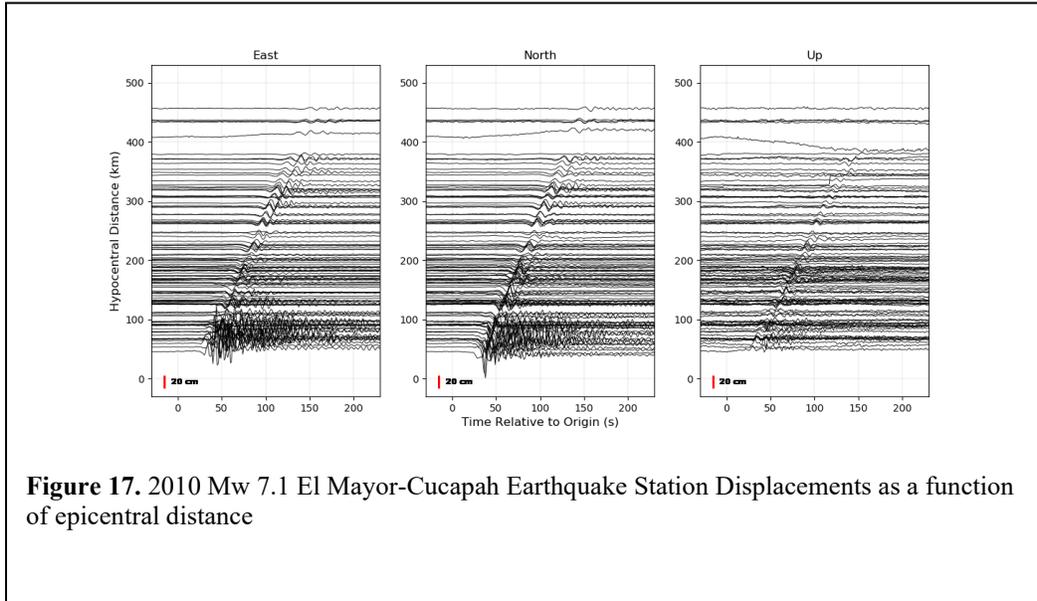
[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/figures/Ridgecrest71.kdisp.eps](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/figures/Ridgecrest71.kdisp.eps)

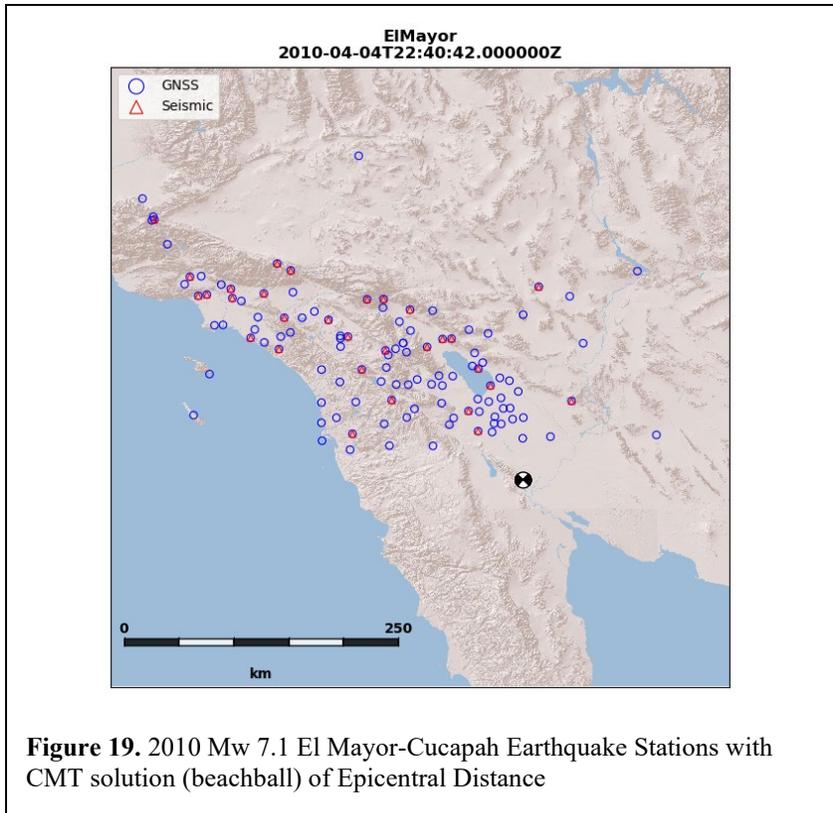
*Seismogeodetic velocities (Figure 18)*

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/figures/Ridgecrest71.kvel.png](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/figures/Ridgecrest71.kvel.png)

*Map (Figure 19)*

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/figures/Ridgecrest71.m ap.png](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/figures/Ridgecrest71.m ap.png)





**Data Directories (time tags are UTC):**

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/gnss/](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/gnss/)

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/kdisp/](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/kdisp/)

[http://garner.ucsd.edu/pub/measures\\_earthquake\\_products/Ridgecrest\\_20190706/kvel/](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/kvel/)

(5) “GNSS” - GNSS-only solutions

MiniSEED (“.mseed”) binary file

e.g., [ACSB.gnss.mseed.gz](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/gnss/ACSB.gnss.mseed.gz) (ACSB is 4-character GNSS station code)

Text (“.txt”) file

e.g., [ACSB.gnss.txt.gz](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/gnss/ACSB.gnss.txt.gz)

(6) “kdisp” – Seismogeodetic displacements

MiniSEED (“.mseed”) – binary file

e.g., [BILL BLL.kdisp.mseed.gz](http://garner.ucsd.edu/pub/measures_earthquake_products/Ridgecrest_20190706/kdisp/BILL_BLL.kdisp.mseed.gz) (BILL is 4-character GNSS station code; BLL is accelerometer station code)

Text (.txt) file

e.g., [BILL BLL.kdisp.txt.gz](#)

(7) “kvel” – Seismogeodetic velocities

MiniSEED (“.mseed”) – binary file

e.g., [BILL BLL.kvel.mseed.gz](#)

Text (.txt) file

e.g., [BILL BLL.kvel.txt.gz](#)

**(8) “Coseismic\_Parameters”**

Filename: Coseismic\_parameter.txt

Header: Network Station BI Lat Lon Alt(m) dE(mm) dN (mm) dU (mm) dE presig(mm)  
 dNpresig(mm) dUpresig(mm) dEpostsig(mm) dNpostsig(mm) dUpostsig(mm) PGD(mm)  
 PGDtime(s) SNR(all) SNR(hor) Hyp.Distance(km)

**Table 6.** Coseismic Parameters<sup>1</sup>

Parameter	Units	Description
Network		Name of real-time network
Station		GNSS 4-character code/Accelerometer Code
BI <sup>2</sup>		Band code: general sampling rate and response band. For example: S for short period, H for high broad band, I – instrument code. What is being measured. For example: H is high gain seismometer, N is an accelerometer.
Lat	Decimal degrees	Latitude of station
Lon	Decimal degrees	Longitude of station
Altitude	Meters	
dE	Millimeters	East component
dN	Millimeters	North component
dU	Millimeters	Up component
dE presig	Millimeters	Pre-earthquake displacement sigma East
dNpresig	Millimeters	Pre-earthquake displacement sigma North
dUpresig	Millimeters	Pre-earthquake displacement sigma Up
dE postsig	Millimeters	Post-earthquake displacement sigma East
dNpostsig	Millimeters	Post-earthquake displacement sigma North
dUpostsig	Millimeters	Post-earthquake displacement sigma Up
PGD <sup>3</sup>	Millimeters	Peak ground displacement
PGDtime	Seconds	Time of peak ground displacement from earthquake onset time
SNR(all)		Single/Noise ratio all components (N, E, U)
SNR(hor)		Single/Noise ratio horizontal (N, E)
Hypocentral Distance	Kilometers	Distance of station to hypocenter

<sup>1</sup> Golriz et al. (2021), in press

<sup>2</sup> [http://www.fdsn.org/pdf/SEEDManual\\_V2.4\\_Appendix-A.pdf](http://www.fdsn.org/pdf/SEEDManual_V2.4_Appendix-A.pdf)

<sup>3</sup> Ruhl et al. (2019)

**MiniSEED** – binary format (has provision for displacements and seismic velocities)

Reference: <https://ds.iris.edu/ds/nodes/dmc/data/formats/miniseed/>

**Convert MiniSeed to Text:** <https://github.com/iris-edu/mseed2ascii/blob/master/doc/mseed2ascii.md>

**Text** – format is described in the header of each file:

# East;North;Up;time(sec. relative to origin)

Positions are taken relative to 10 seconds average before origin time

Data start 1-minute before origin time, and end 15-minutes after, depending on availability

**Note:** We have expanded and modified the approach taken by the zenodo archive of GNSS earthquake displacement waveforms described by Ruhl et al. (2019). They do not archive seismogeodetic velocities.

### References:

Bock, Y., D. Melgar, B. W. Crowell (2011), Real-Time Strong-Motion Broadband Displacements from Collocated GPS and Accelerometers, Bulletin Seismological Society of America, 101, 2904-2925, doi: 10.1785/0120110007.

Bock, Y. & D. Melgar (2016), Physical Applications of GPS Geodesy: A Review, Rep. Prog. Phys. 79, 10, doi:10.1088/0034-4885/79/10/106801

Bock, Y. & S. Wdowinski (2020), GNSS Geodesy in Geophysics, Natural Hazards, Climate, and the Environment, in Position, Navigation, and Timing Technologies in the 21st Century: Integrated Satellite Navigation, Sensor Systems, and Civil Applications, IEEE, 2021, 741-820, doi: 10.1002/9781119458449.ch28.

Ruhl, C.J., Melgar, D., Geng, J., Goldberg, D.E., Crowell, B.W., Allen, R.M., Bock, Y., Barrientos, S., Riquelme, S., Baez, J.C. and Cabral-Cano, E. (2019). A global database of strong-motion displacement GNSS recordings and an example application to PGD scaling. Seismological Research Letters, 90(1), pp.271-279.

Zenodo Web Page (2018): <https://zenodo.org/record/1434374#.X-udln-YLQl>

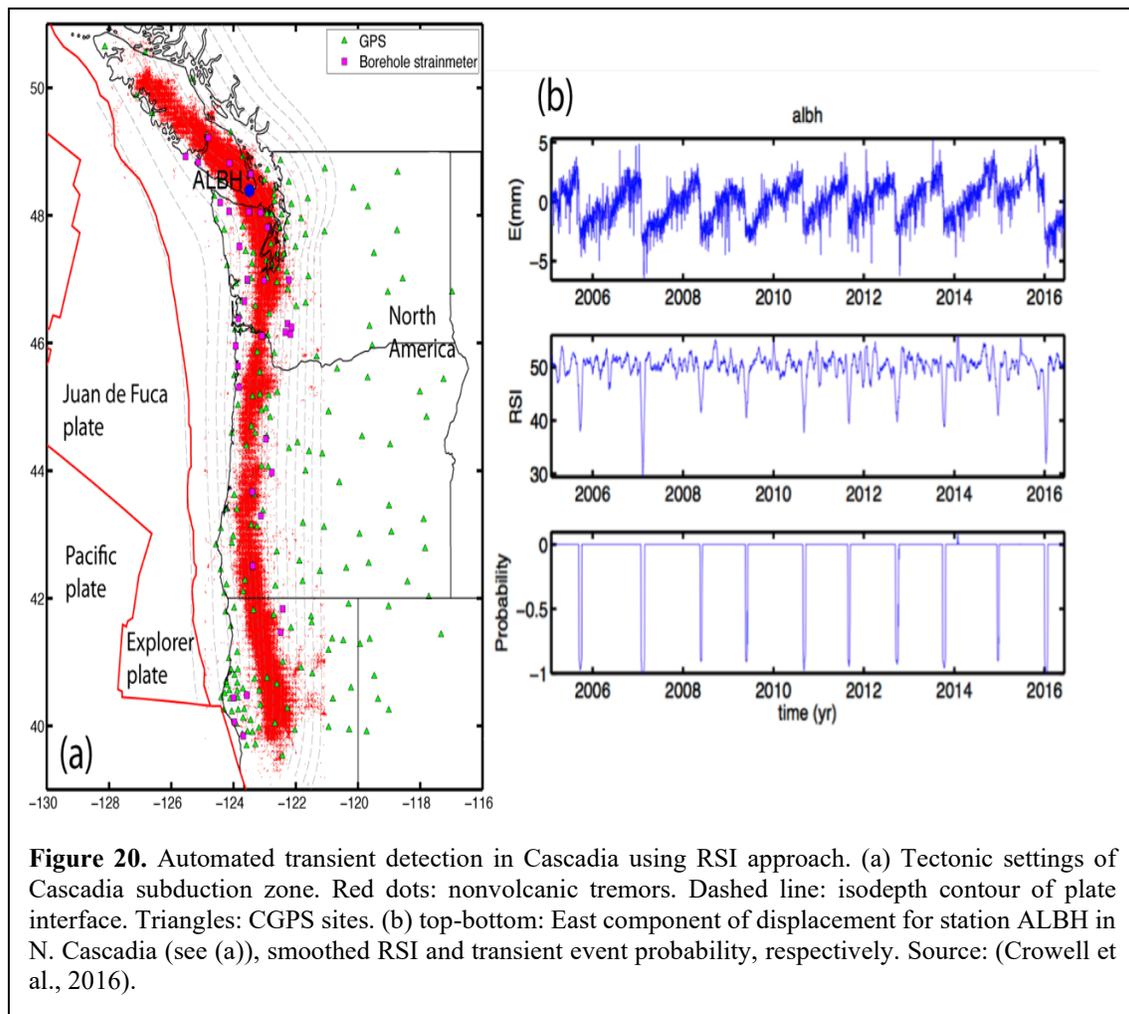
Zenodo Archive:

[https://zenodo.org/record/1434374/files/dataset\\_ruhl\\_et\\_al\\_2018\\_version2.tar.gz?download=1](https://zenodo.org/record/1434374/files/dataset_ruhl_et_al_2018_version2.tar.gz?download=1)

## 7. Level 4: ETS Transients

### 7.1 Plate Boundary Aseismic Transients

Advances in observational techniques in geodesy and seismology have led to the discovery of a diverse spectrum of slow earthquakes such as slow slip events (SSEs), non-volcanic tremor, low frequency earthquakes and very low frequency earthquakes (Peng and Gomberg, 2010). These slow earthquakes have distinctive scaling relations (Ide et al., 2007) and rupture characteristics compared to conventional earthquakes. The discovery of slow slip events such as episodic tremor and slip (ETS) in Cascadia margin over the past decades has changed our understanding of tectonic hazards and the earthquake cycle (Dragert et al., 2001; Rogers and Dragert, 2003). Slow slip transients can change stress on the fault interface, trigger earthquake swarms or seismicity (e.g., Segall et al., 2006; Lohman and McGuire, 2007; Fu et al., 2015), and release accumulated elastic strain on the fault interface (e.g., Liu et al., 2015a; Dixon et al., 2014). They seem to occur



throughout the interseismic period and have now been observed at a number of subduction zones (Beroza and Ide, 2011). As slow slip transient may evolve into catastrophic megathrust

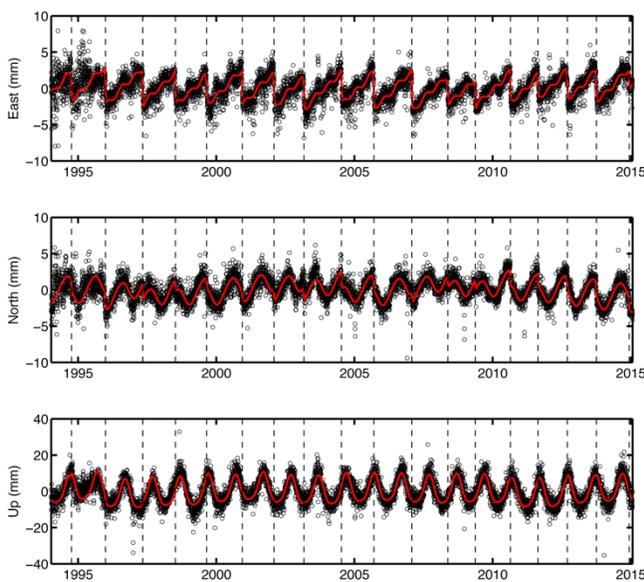
earthquakes (Segall and Bradley, 2012), proper detection and characterization of slow slip events is crucial in our understanding of earthquake hazard. Combined with seismic tremor catalog, a high-quality transient catalog enables the investigation of the genesis and mechanism of slow earthquakes.

The L2 residual displacement time series (after taking out known model components) time series analysis can be mined for transient motions that can vary both temporally and spatially.

## 7.2 Methodology

For the Level 4 ESDR we will use a methodology developed for the financial sector, a financial momentum oscillator based on relative strength index (RSI) to detect when the residual time series deviate above the normal variance. Kurtosis minimization is then used to quantify the transient probabilities associated with any detected events (Figure 21). This approach has been applied by Crowell et al. (2016) to Level 1C residual time series to detect episodic tremor and slip events (RTS) in northern Cascadia. An advantage of this approach is that it can be performed on a station-by-station basis, which allows for the detection of outliers more readily than network approaches.

Furthermore, it can be fully automated and thus is well suited for operational transient detection and classification.

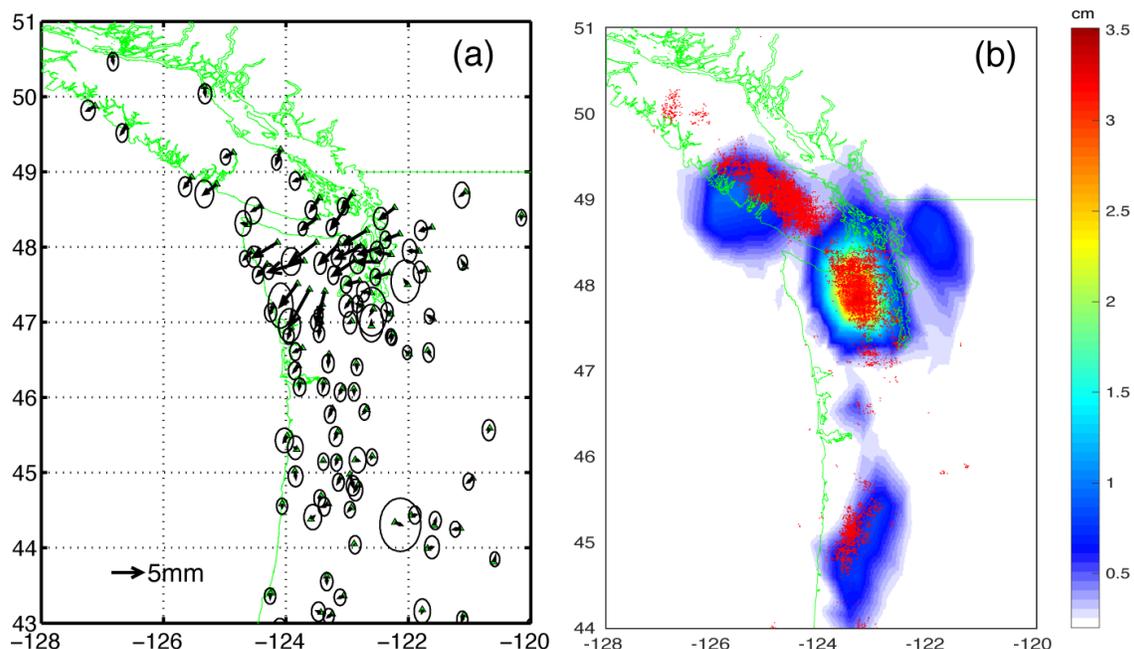


**Figure 21.** Model fit (red line) to the detrended position time series (black circles) at the Cascadia site ALBH. Top to bottom: East, North and Up components respectively. Source: (Crowell et al., 2016).

The RSI based algorithm provides initial estimates of the centroid time and duration of ETS events. To estimate the total displacement of the detected transients we model the residual displacement time series for inter-ETS linear rates, annual and semi-annual variations, and episodic slow slip (Figure 20) (Liu et al., 2015b). We use a hyperbolic function and employ a grid-search to estimate the optimal duration and centroid time. This parametric model ensures a robust estimate of transient displacement with uncertainties. Examination of the accumulated displacements for the ETS events in northern Cascadia margin shows considerable variability of surface deformation

in spite of fairly regular recurrence, implying underlying slip complexity.

Once the surface transients are quantified in space and time, the next step is to model transient slip on the fault interface using the mature Network Inversion Filter (NIF) (Figure 22) (Segall and Matthews, 1997; McGuire & Segall, 2003; Liu et al., 2010, 2015a, b). The NIF and its variants have been successfully applied to model slip transients in diverse tectonic settings including Cascadia (e.g., Schmidt and Gao 2010; Bartlow et al. 2011), Japan (e.g., Miyazaki et al. 2006; Ozawa et al. 2007; Liu et al. 2010, 2015a), New Zealand (e.g., Bartlow et al., 2014), southcentral Alaska (Fu et al., 2015), Hawaii (e.g., Segall et al. 2006) and Costa Rica (Voss et al., 2018). This ESDR will, for the first time, combine automated transient detection and NIF to systematically analyze the state of the Cascadia margin and other subduction zones around the globe.



**Figure 22.** (a) Total surface displacements for 2014 November ETS event along the Cascadia subduction zone; (b) Accumulated transient slip from slip inversion. Red dots: tremor from PNSN catalog.

To summarize, starting with the Level 1 combined displacement time series residuals (section 6), we will (1) identify the transients, their duration and centroid, (2) estimate the total surface displacements, (3) model the fault slip and (4) catalog the Level 4 results. We will continue to focus on Cascadia and expand to other tectonically active and transient rich regions as we include more GNSS sites in our network densification efforts.

We will seek community feedback on our ESDR content and formats.

### 7.3 Transient Products

The transient products are contained in a tar file with the name:

ProjectName\_YYYYMMDD at the date (YYYYMMDD) of the most recent upload to CDDIS

e.g., CascadiaETS\_20210412.tar.gz (“Cascadia” is region; “ETS” is the transient type)

The directory structure for the SOPAC archive is as follows:

Top directory *measures\_transient\_products* will include:

*ReadMe.txt*

Subdirectory for each region and type of transient, e.g., CascadiaETS

The subdirectory will include:

A description file in pdf format, e.g., *MEaSURES\_CascadiaETS*

*ETS\_event.list* - list of ETS transients with event tag, start and end times, e.g.,

Event	start	end
evt94	1994-Sep	1994-Dec
evt95	1995-Nov	1996-Mar

Then a folder for each event, *evtYY*, e.g.,

evt94  
evt95

In each folder:

*evttag\_disp\_grd.txt*: Transient displacements at uniform grid (0.2x0.2 deg) from slip model, Units: mm

Format: longitude latitude east(mm) north(mm) up(mm), e.g.,

Lon	Lat	e(mm)	n(mm)	u(mm)
-128.000	41.000	0.0189	0.0245	0.0029

*evttag\_disp\_grd.pdf*: Map of transient displacements on a uniform grid (Figure 21a)

*evttag\_disp.txt*: Transient displacements and uncertainties at GNSS sites, Units: mm

Format: site\_name start\_date end\_date longitude latitude e n u se sn su; se,sn and su are one sigma uncertainties, e.g.,

site	start_date	end_date	longitude	latitude	e(mm)	n(mm)	u(mm)	se(mm)	sn(mm)	su(mm)
ALBH	20001030	20010109	-123.487	48.390	-4.3486	-2.1548	-4.2028	0.318	0.460	1.339
BCOV	20001030	20010109	-126.843	50.544	0.4230	0.2306	-4.2355	0.335	0.472	1.398

*evttag\_disp.pdf*: Map of transient displacements at GNSS sites (Figure 21b)

*evttag\_slip.txt*: Accumulated transient slip of ETS event

e.g.,

lon1	lat1	z1	lon2	lat2	z2	lon3	lat3	z3	u1	u2	u3	u1sig	u2sig	u3sig
-126.9202	48.4140	-5.242	-126.6596	48.0974	-5.223	-126.4634	48.5169	-8.575	-0.000	0.000	0.000	0.001	0.001	0.000
-121.2872	44.6730	-106.319	-121.2872	45.0089	-106.046	-121.6892	44.9196	-90.296	-0.000	0.000	0.000	0.000	0.001	0.001

where:

*lon1,lat1,z1* – longitude, latitude, depth (km) of the first vertex of triangle patch

*lon2,lat2,z2* – longitude, latitude, depth (km) of the 2nd vertex of triangle patch

*lon3,lat1,z3* – longitude, latitude, depth (km) of the 3rd vertex of triangle patch

*u1,u2,u3* – Dip-slip (normal "+"), strike-slip (along-strike "+"), tensile component (opening "+") of slip vector at the center of triangle patch, Units: meters

*u1sig, u2sig, u3sig* – uncertainties of u1, u2, u3. Units, meters

*evttag\_slip.pdf*: Plot of accumulated transient slip model with PNSN tremor locations (when available)

*evttag\_movie.avi*: Movie of transient slip rate of ETS event with PNSN tremor locations (when available)

## 7.4 Status

A new set of displacements will be made available whenever a transient event is detected and analyzed and/or when newly updated time series solutions warrant the re-analysis.

We plan to expand our transient products to other subduction zones beyond Cascadia, such as Japan, New Zealand and Costa Rica, depending on the addition of a sufficient number of stations in these regions.

## 8. Level 4: Horizontal strain rate grids

**Note: This section is incomplete**

### 8.1 Background

We have been producing a horizontal strain rate product but plan to replace it with a method that takes into an account an underlying interseismic fault model for better resolution near faults and to better identify transients (Zeng & Shen 2017; Klein et al., 2019). The product is constructed from the weekly residual displacement time series (observed minus predicted) to construct strain and strain rate fields. Figure 12 shows displacement residual maps (vectors) and interpolated displacement fields at epoch 2018.59 and maximum shear strain rate and dilatation rate residual fields. Figure 13 shows the maximum shear and dilatation rates due to postseismic slip for four strike slip earthquakes one week after each event compared to the week before the event: the 1999 Mw7.1 Hector Mine, 2004 Mw6.0 Parkfield, 2010 Mw7.1 El Mayor-Cucapah and 2014 Mw6.0 Napa Valley earthquakes.

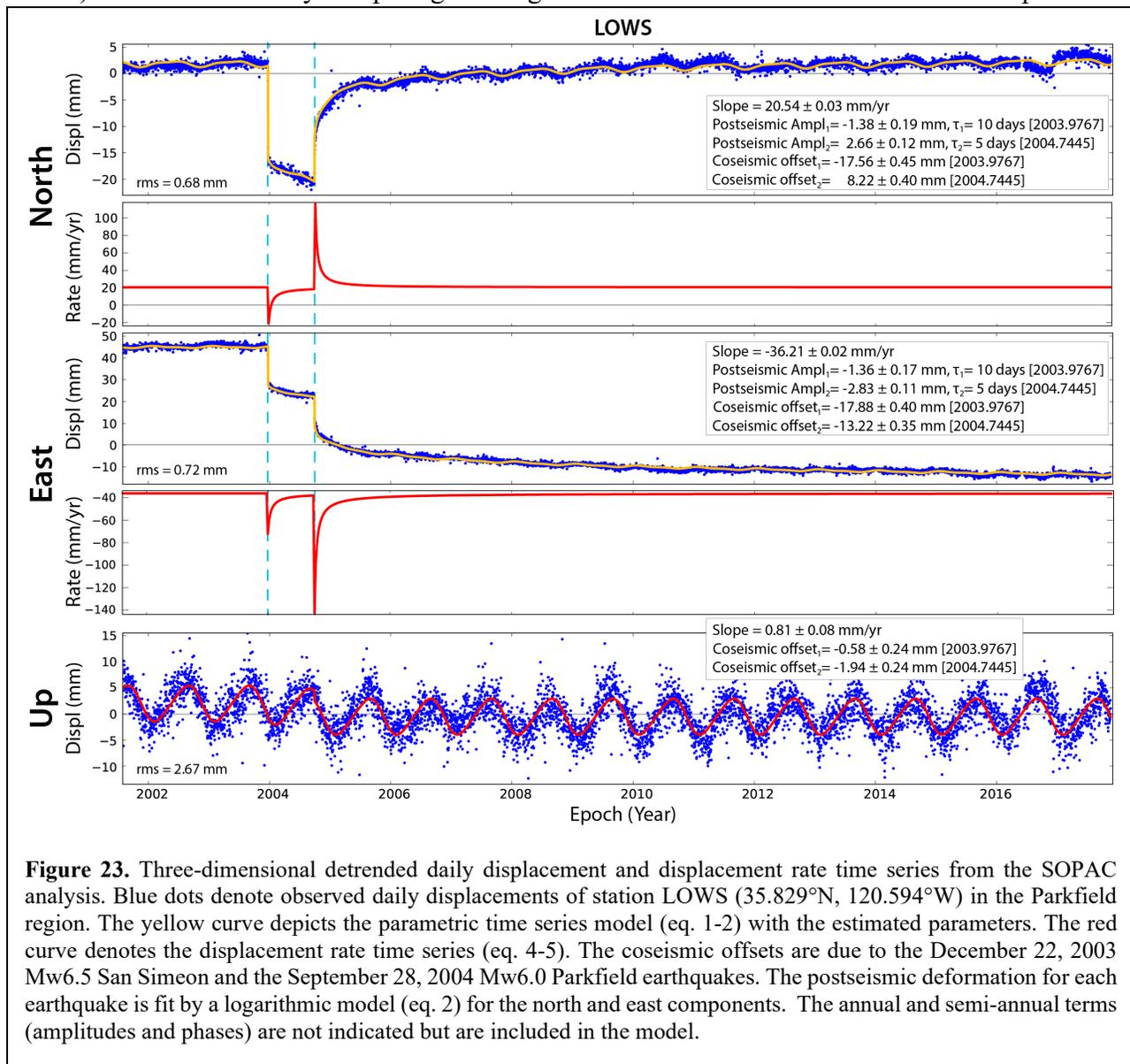
### 8.2 Methodology

To distinguish time-dependent and secular deformation, in particular postseismic, we take the derivative of the expressions for displacement (equations 12-13) (Klein et al., 2017),

$$\dot{y}(t_i) = (\hat{b} - v_M) + \sum_{j=1}^{n_h} h_j H(t_i - T_{h_j}) + \sum_{j=1}^{n_k} \frac{k_j}{t_i} e^{\left[-\left(\frac{t_i - T_{k_j}}{\tau_j}\right)\right]} H(t_i - T_{k_j}) + \varepsilon_i \quad (20)$$

$$\dot{y}(t_i) = (\hat{b} - v_M) + \sum_{j=1}^{n_h} h_j H(t_i - T_{h_j}) + \sum_{j=1}^{n_k} \frac{k_j}{\tau_j + t_i + T_k} H(t_i - T_{k_j}) + \varepsilon_i \quad (21)$$

and insert the estimated model parameters from the JPL, SIO and Combination time series. The term  $v_M$ , the predicted surface velocity from the fault slip model (Zeng & Shen 2017), is subtracted from the estimated weekly velocity. The seasonal terms in (equation 12) are ignored since their amplitudes are on the mm-level for the horizontal components and the effect on velocity estimates is minimal over the time period (10-20 years) spanned by the displacement time series. The term  $\varepsilon_i$  recognizes that there are errors in the estimated parameters in (eq. 20) and (eq. 21), as well as unmodeled time-dependent effects other than postseismic deformation, e.g., subsidence bleeding into horizontal. However, there is no inversion performed in computing the weekly velocities (eq. 20-21) – we are essentially computing the tangent to the time series model trace. We compare the



displacement time series and their derivatives for station LOWS in Figure 23 for which a logarithmic model (eq. 21) is applied.

The horizontal strain rate tensor components are then computed from the weekly residual velocity fields as follows:

$$\dot{\varepsilon}_{ij} = \frac{1}{2} \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right) \quad (22)$$

The derivatives are calculated using the *grdgradient* function in GMT. From these velocity grids, we calculate the principal strain rates

$$\dot{\varepsilon}_{1,2} = \frac{\dot{\varepsilon}_{xx} + \dot{\varepsilon}_{yy}}{2} \pm \sqrt{\left( \frac{\dot{\varepsilon}_{xx} - \dot{\varepsilon}_{yy}}{2} \right)^2 + \dot{\varepsilon}_{xy}^2}, \quad (23)$$

the maximum shear strain rate

$$\dot{\varepsilon}_{12}^{MAX} = \frac{\dot{\varepsilon}_1 - \dot{\varepsilon}_2}{2} = \sqrt{\left( \frac{\dot{\varepsilon}_{xx} - \dot{\varepsilon}_{yy}}{2} \right)^2 + \dot{\varepsilon}_{xy}^2}, \quad (24)$$

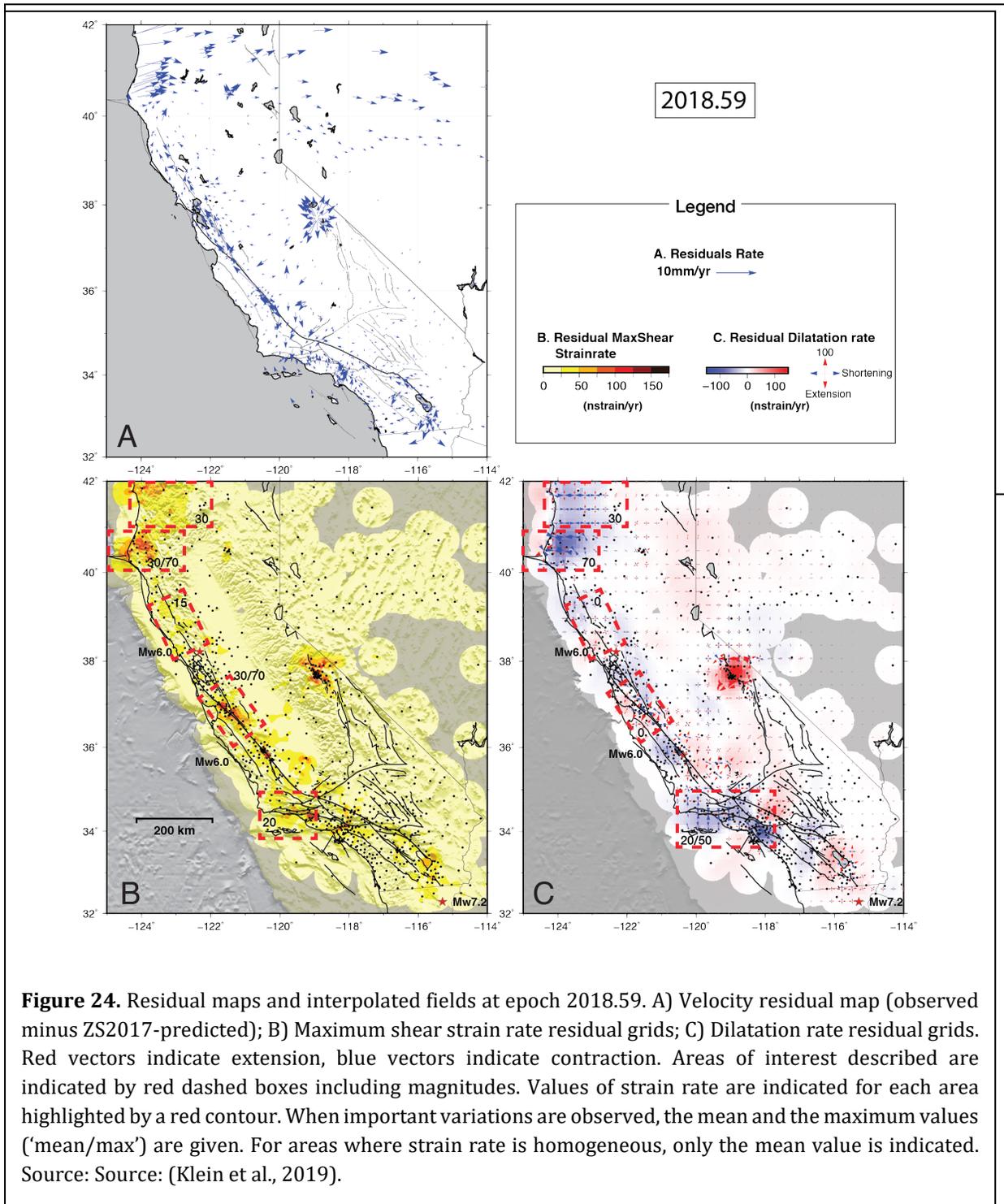
and the dilatation rate

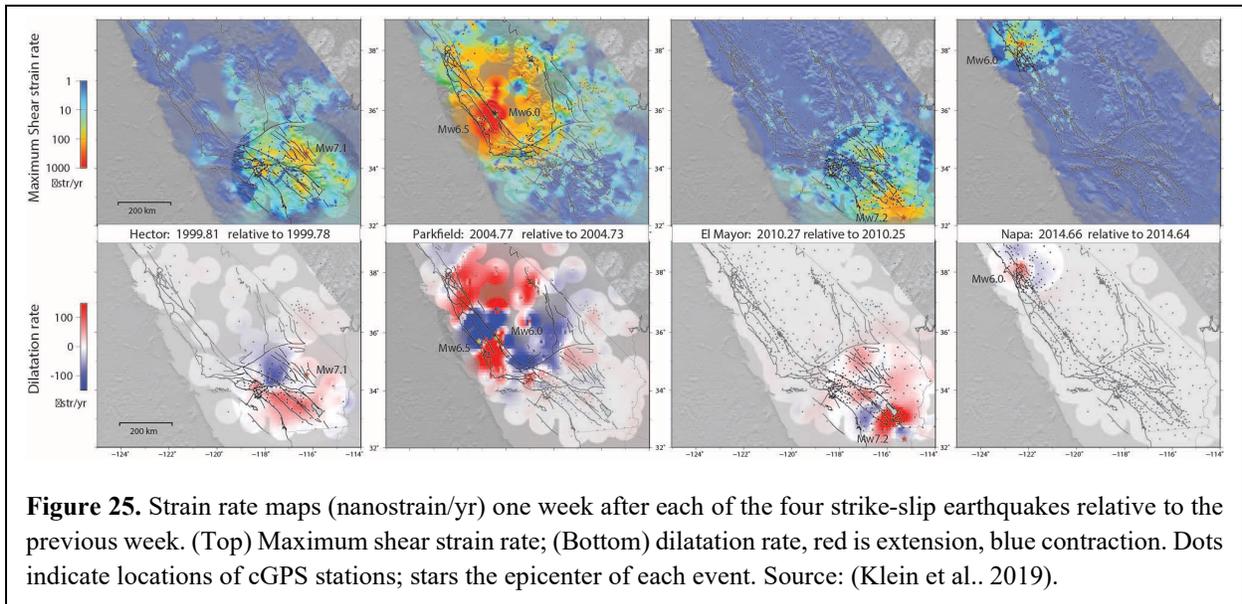
$$\delta = \dot{\varepsilon}_1 + \dot{\varepsilon}_2 = \dot{\varepsilon}_{xx} + \dot{\varepsilon}_{yy}. \quad (25)$$

### 8.3 Products

Gridded weekly maximum shear strain rate observations and model (Figure 24)

Gridded weekly dilatation rate residuals between observations and model (Figure 24)





## 9. Level 4 ESDR: Change in Total Water Storage Time Series

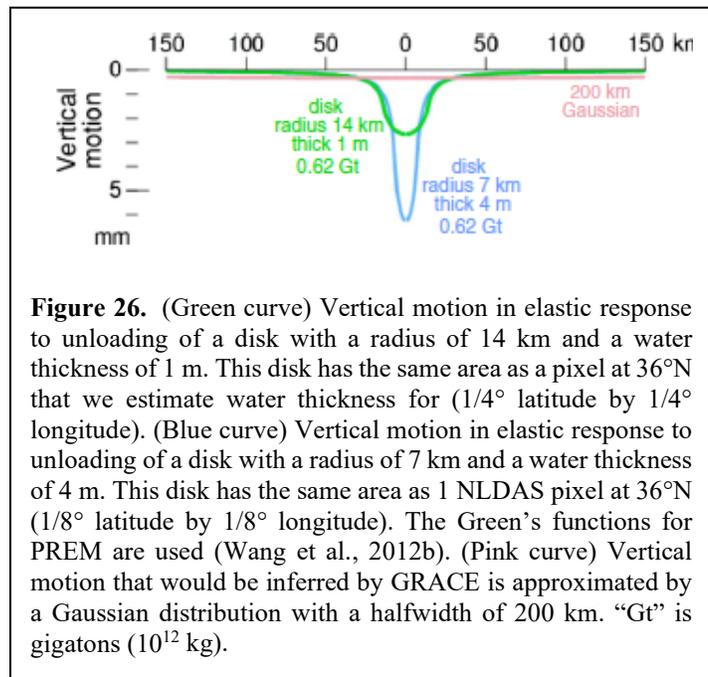
The capability to weigh mass change at Earth's surface with GPS is emerging as an excellent, effective technique to evaluate available water resources. Many studies have established that solid Earth responds elastically to changes in mass surface load, particularly in the vertical (Blewitt et al. 2001; Davis et al. 2004; Bevis et al. 2005; Tregoning et al. 2009; Nahami et al. 2012, Ouellette et al. 2013; Chew et al. 2014; Wahr et al. 2015). We and others have rigorously inferred changes in total water at Earth's surface as a function of location and time using elastic displacements of solid Earth (Argus et al. 2014, 2017; Borsa et al. 2014; Fu et al. 2015; Jin and Zhang 2016).

### 9.1 Background

#### 9.1.1 Solid Earth's elastic response to a mass load

We will follow the method of Argus et al. (2017) to infer change in water as a function of time and location. Solid Earth's elastic response to a point load is specified by  $u = m \times \text{GPS}(\theta)$ , where  $u$  is vertical displacement of Earth's surface (in m) at an angular distance  $\theta$  (in degrees) from the point load,  $m$  is the mass of the point load (in kg), and GPS is the Green's function (in m/kg), which depends on  $\theta$ . We use the Green's functions for a gravitating, stratified PREM Earth (Wang et al. 2012b). Solid Earth's response to a surface mass load is tight in space. For a disk with a radius of 7 km, the vertical displacement at 20 km from the load center is half that at 10 km from the load center (Figure 26) (Wahr et al. 2015; Argus et al. 2014). The spatial resolution of GPS's determination of mass change is

therefore high and limited only by the spacing of GPS sites. If a GPS array were to have a 10 km spacing, then GPS could determine mass change in individual watersheds and ice basins. We numerically integrate the Green's function to obtain a modified (Green's) function specifying solid Earth's elastic response to a disk load with a specific radius. We calculate many such modified (Green's) functions, varying the disk radius so that the disk area is equal to the area of a rectangular spherical cap bounded by specific latitude/longitude intervals.

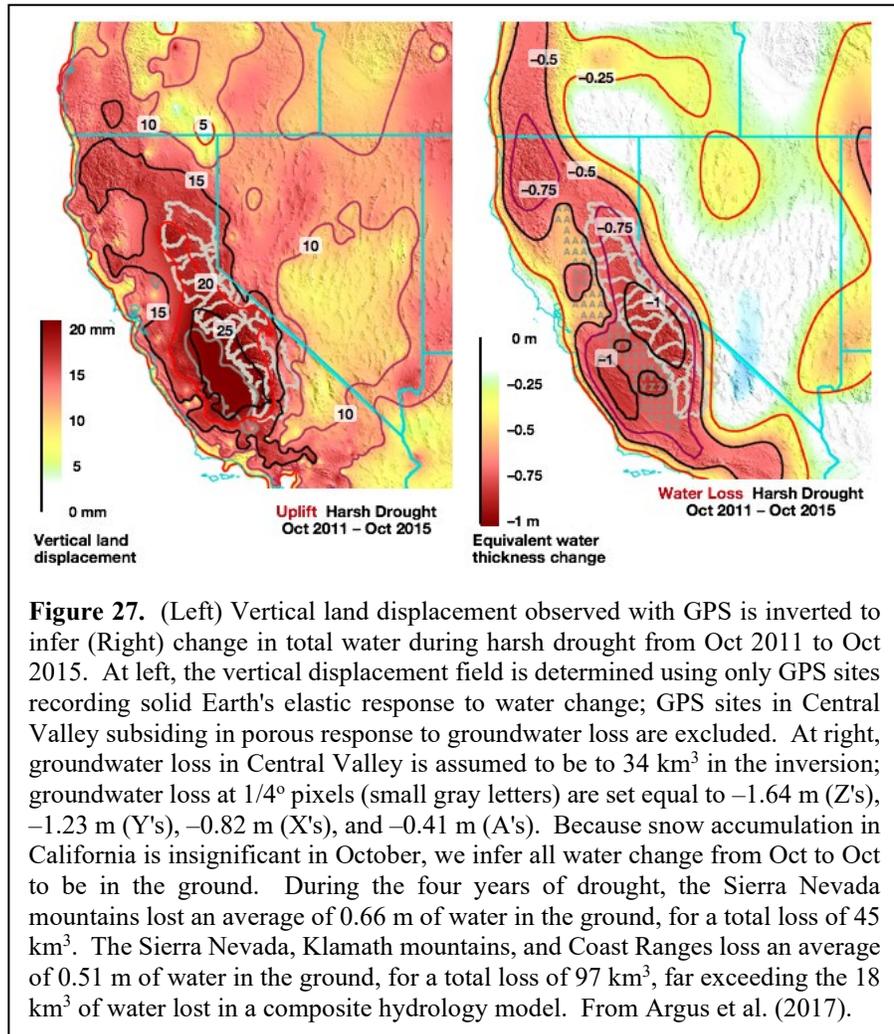


**Figure 26.** (Green curve) Vertical motion in elastic response to unloading of a disk with a radius of 14 km and a water thickness of 1 m. This disk has the same area as a pixel at 36°N that we estimate water thickness for (1/4° latitude by 1/4° longitude). (Blue curve) Vertical motion in elastic response to unloading of a disk with a radius of 7 km and a water thickness of 4 m. This disk has the same area as 1 NLDAS pixel at 36°N (1/8° latitude by 1/8° longitude). The Green's functions for PREM are used (Wang et al., 2012b). (Pink curve) Vertical motion that would be inferred by GRACE is approximated by a Gaussian distribution with a halfwidth of 200 km. "Gt" is gigatons ( $10^{12}$  kg).

### 9.1.2 Sustained changes in water in the ground during alternating periods of drought and heavy precipitation

GPS is providing striking new constraints on hydrology. Using GPS measurements of solid Earth's elastic displacement, Argus et al. (2017) quantify change in total water in three California mountain provinces (the Sierra Nevada, the Klamath mountains, and the Coast Ranges). In the western U.S., snow falls and accumulates on the ground in the fall and winter, then melts in the spring and summer, leaving negligible snow in October. Argus et al. (2017) thus quantify change in water in the ground by taking differences between successive Octobers. Argus et al. (2017) find California's three mountain provinces to have lost 97 km<sup>3</sup> of water during the four years of harsh California drought from Oct 2011 to 2015, exceeding by a factor of five the 18 km<sup>3</sup> of water lost in a composite hydrology model (Figure 27). We find the three mountain provinces to have gained 51 km<sup>3</sup> of water in the ground during two years of heavy precipitation from Oct 2015 to Oct 2017.

In summary, we are finding that in California's mountains more water in the ground is lost during drought and gained in heavy precipitation than in the hydrology models. The sustained changes in water cannot result from snow because snow accumulation is negligible in October. Either changes in soil moisture in the ground are far understated in the hydrology models or there are large changes in groundwater in river alluvium, pastures, and fractured crystalline basement that is not in the hydrology models. The ground must have a greater capacity to store water than previously believed.



## 9.2 Methodology

We will infer **changes in total water storage at Earth's surface** following a sequence of 10 carefully constructed and practiced steps following the techniques in Argus et al. (2017).

1. Carefully analyze all series of GNSS positions; identify all offsets due to antenna substitutions, earthquakes, and other phenomena; identify postseismic transients that are clearly associated in time and space with earthquakes; construct series of GNSS displacements of more than five years passing through January 2012 (by eliminating data after offsets occurring after Jan 2012 and data before offsets occurring before 2012).
2. Distinguish between GNSS sites primarily recording solid Earth's elastic response to mass changes; solid Earth's porous response to groundwater and oil changes; and solid Earth's response to magma changes in volcanoes.
3. Remove solid Earth's elastic response to changes in the atmosphere and non-tidal changes in the ocean.
4. Remove solid Earth's elastic response to known changes in surface water in artificial reservoirs and large lakes.
5. Remove interseismic strain accumulation produced by locking of the Cascadia subduction zone. Remove displacements produced by slow slip events occurring along the Cascadia megathrust.
6. Remove solid Earth's viscous response to unloading of the late Pleistocene ice sheets.
7. Transform Earth's reference frame into the frame minimizing differences between observations of vertical displacements and predictions from a postglacial rebound model. The velocity of Earth's mass center (CM) estimates using SLR observations of satellite LAGEOS is somewhat uncertain; We maintain that this transformation into the solid Earth's mass center (CE) results in more accurate estimates of vertical displacement (Argus 2007, 2012; Argus et al. 2014; Riddell et al. 2017).
8. Constrain total water change outside the western United States area for which water change is being estimated to be that inferred from GRACE.
9. Constrain groundwater change in California's Central Valley to an a priori hydrological model (Faunt et al. 2015; Xiao et al. 2017).
10. Invert for changes in total water storage ("**water.gps**") as a function of position at  $1/4^\circ$  intervals of latitude and longitude each month from Jan 2006 to the Present. Solid Earth's elastic response to a surface mass load is nearly known if the surface load is more than about 50 km across (Wahr et al. 2013; Argus et al. 2014b, 2017). Apply Laplacian regularization to limit water changes between adjacent pixels. Estimate uncertainty using linear propagation of errors on the basis of a realistic error budget.

### 9.3 Products

Changes in components of water storage are archived in seven text files. The first two columns in each file are latitude and longitude. The third column is the value of the product and the fourth column is uncertainty (units of mm).

- (1) Change in total water storage inferred from GPS – “water.gps”
- (2) Change in equivalent water thickness – “atmosphere”
- (3) Change in snow water equivalent (SWE) – “snow”  
Snow depth and snow water equivalent (SWE) data are available from NOAA’s National Weather Service's National Operational Hydrologic Remote Sensing Center (NOHRSC) SNOW Data Assimilation System (SNODAS). <https://nsidc.org/data/g02158>
- (4) Change in soil moisture content (SMC) – “soil”  
NLDAS\_NOAH is a monthly climatology data set contains a series of land surface parameters, including Soil Moisture Content (SMC), simulated from the Noah land-surface model (LSM) for Phase 2 of the North American Land Data Assimilation System (NLDAS-2). [https://disc.gsfc.nasa.gov/datasets/NLDAS\\_NOAH0125\\_MC\\_V002/summary](https://disc.gsfc.nasa.gov/datasets/NLDAS_NOAH0125_MC_V002/summary)
- (5) Change in artificial reservoir surface water – “reservoir”  
These hydrological data are from the California Data Exchange Center (CDEC) Weather Gauging Stations, including automatic snow reporting gages for the Cooperative Snow Surveys Program and precipitation and river stage sensors for flood forecasting. [https://www.calfish.org/ProgramsData/ReferenceLayersNaturalResources/\(CDEC\)WeatherGagingStations.aspx](https://www.calfish.org/ProgramsData/ReferenceLayersNaturalResources/(CDEC)WeatherGagingStations.aspx)
- (6) Change in total mass – “mass”  
Total mass = water.gps + reservoir + atmosphere
- (7) Change in water in the ground not in hydrology models – “ground”  
Inferred to be water.gps - snow - soil moisture

**Note: Check if accurate:** The start date for the water storage products is taking zero to be 1 Jan 2012, about halfway through the time series (circa May 2020). The start time will be modified to 1 Jan 2013 as the series lengthens.

### 9.4 Directory Structure

**CDDIS Product Name:** water\_storage

**CDDIS file path:** ~/GPS\_Explorer/archive/WaterStorage/YYYY.yyy\_YYYY.yyy-combwm/

Only first one (combwm) is sent to CDDIS.

/GPS\_Explorer/archive/WaterStorage/YYYY.yyy\_YYYY.yyy-combg/

/GPS\_Explorer/archive/WaterStorage/YYYY.yyy\_YYYY.yyy-jpl/

/GPS\_Explorer/archive/WaterStorage/YYYY.yyy\_YYYY.yyy-sio/

**Note: Check CDDIS links above**

WaterStorage\_yyyymmdd.tar.gz (yyymmdd indicates date that tar file was archived)

SOPAC archive directory:

[http://garner.ucsd.edu/pub/measuresESESES\\_products/WaterStorage](http://garner.ucsd.edu/pub/measuresESESES_products/WaterStorage)

Example:

[http://garner.ucsd.edu/pub/measuresESESES\\_products/WaterStorage/2006.042\\_2021.458-combwm/](http://garner.ucsd.edu/pub/measuresESESES_products/WaterStorage/2006.042_2021.458-combwm/)

2006.042\_2021.458: data set denoted by start and end dates in decimal years

Extensions (time series source):

-jpl

-sio

-combwm (weighted mean combination)

-combg (GLOBK combination)

**In water storage directories:**

*readme.txt* (update header when new product is ready to upload to JPL – source and tar file names), e.g.,:

NASA MEaSURES ESESES Project

Water Storage: Level 4 products

Source: Weighted Mean Combination of JPL and SIO solutions:

WNAM\_Clean\_TrendNeuTimeSeries\_combwm\_20210810.tar;

GLB\_Clean\_TrendNeuTimeSeries\_combwm\_20210810.tar

August 29, 2021 (date when archived)

*atmosphere*

*ground*

*mass*

*reservoir*

*snow*

*soil*

*water.gps*

The WaterStorage directories (atmosphere, ground, etc.) contain daily files named by decimal year. Formats described in *readme.txt* and section 9.3.

## 9.5 Data Grids

**Note: In progress**

*Data Grids*

Illustrations will be made each month of Water Year 2020, with zero being October 2019, to show water storage growing through the rainy Autumn and Winter.

1. Oct 2019 to Oct 2018 would quantify water change over Water Year 2019.
2. Oct 2019 to Feb 2020 would quantify water change to date over the current year.
3. Water change from Oct 2011 to Oct 2015 quantifies water change over the four years of harsh drought. Identical to the figure in Argus et al. 2017 and similar to that in the project logo.
4. Water change (to this month in that year) in a heavy precipitation year.
5. Water change (to this month in that year) in a drought year.

## 9.6 Status

Updated every 3-4 months.

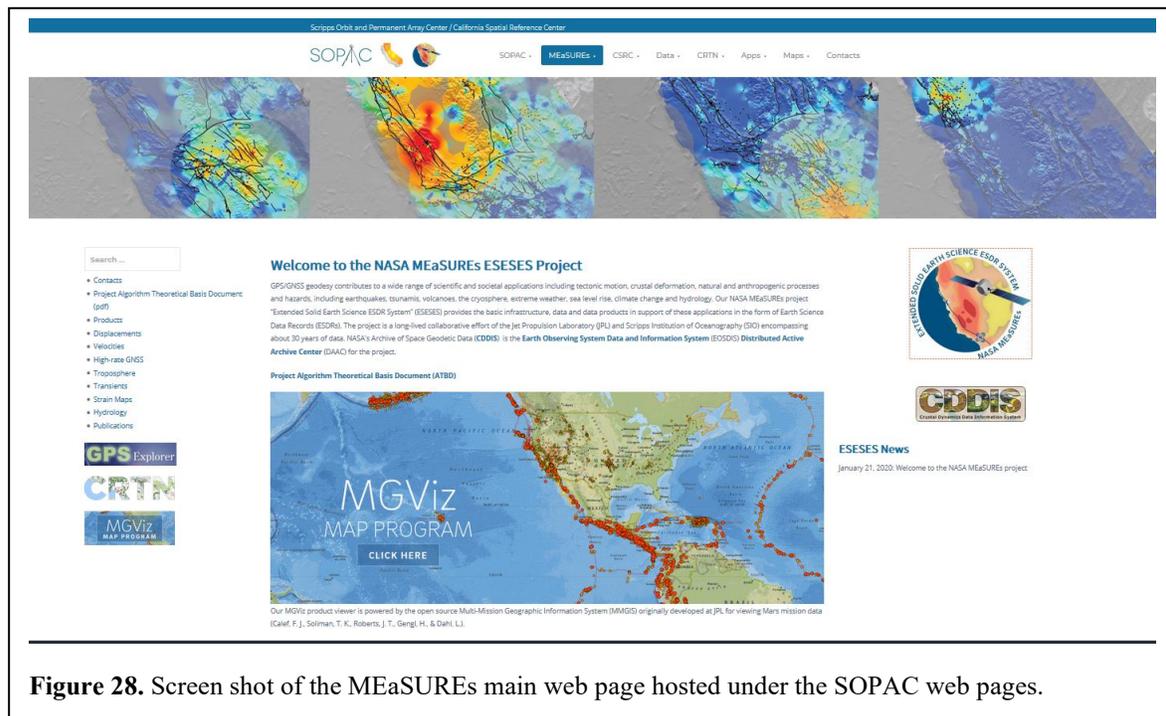
## 10. Web Presence

### 10.1 MEaSUREs Web Pages

The project logo and web pages are found at <http://sopac-csrc.ucsd.edu/index.php/measures-2/>. An ESESES page at DAAC CDDIS directs users to our products located there (<https://cddis.nasa.gov/>).

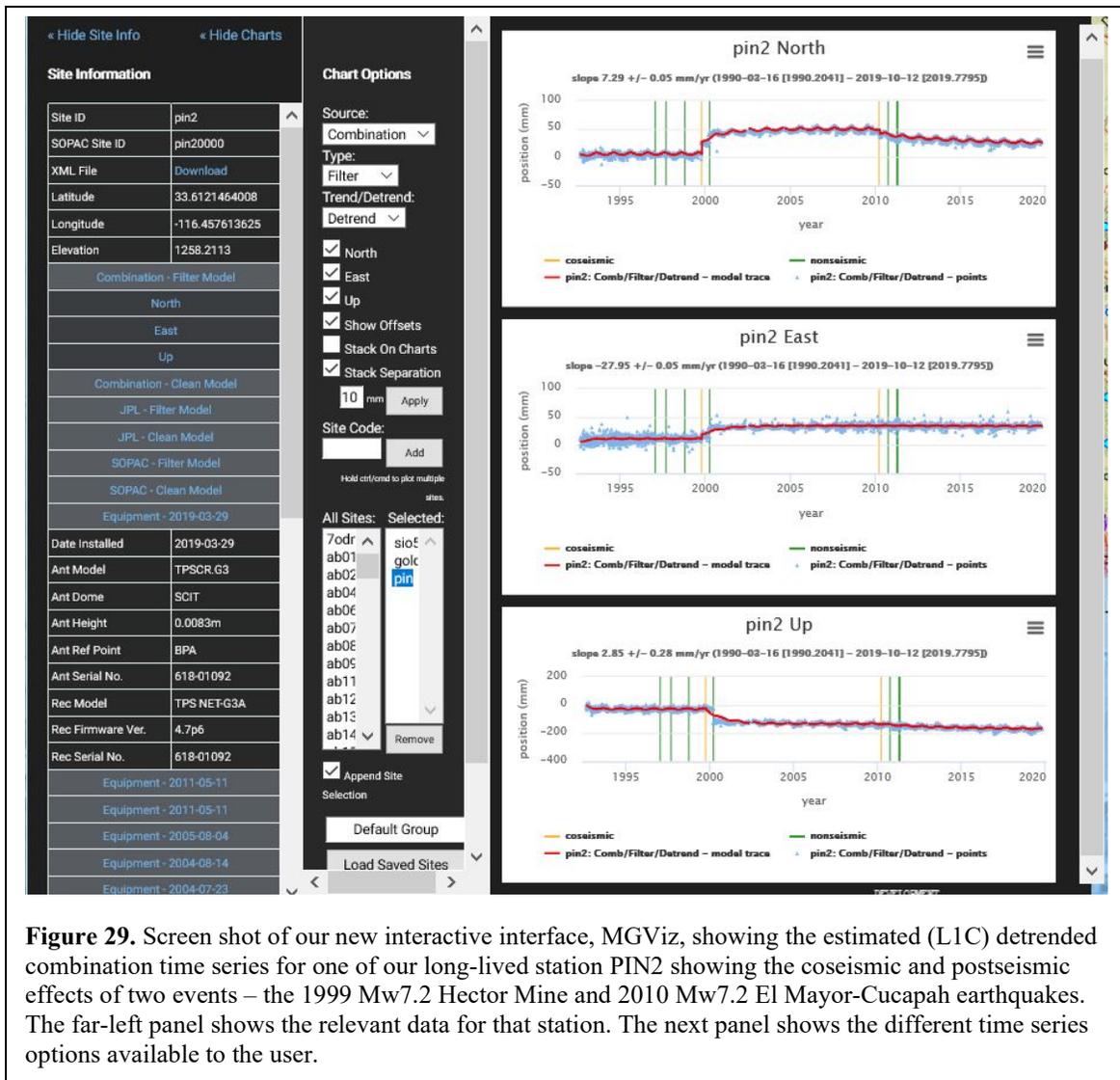
### 10.2 MGviz

The primary web interface to our ESDRs has shifted from GPS Explorer to the MEaSUREs GNSS Visualizer (MGviz) (Figure 28 and 29) ([MGviz - ESESES \(ucsd.edu\)](http://MGviz-ESESES(ucsd.edu))), which is based on the Multi-Mission Geographic Information System (MMGIS), previously developed at JPL to localize and visualize Mars mission science instrument data. This transition recognizes that due to evolution of technology over the past 15 years, GPS Explorer’s underlying portlet-based framework (GridSphere) has reached end of life, and Java time series applet support is unavailable in many browsers.



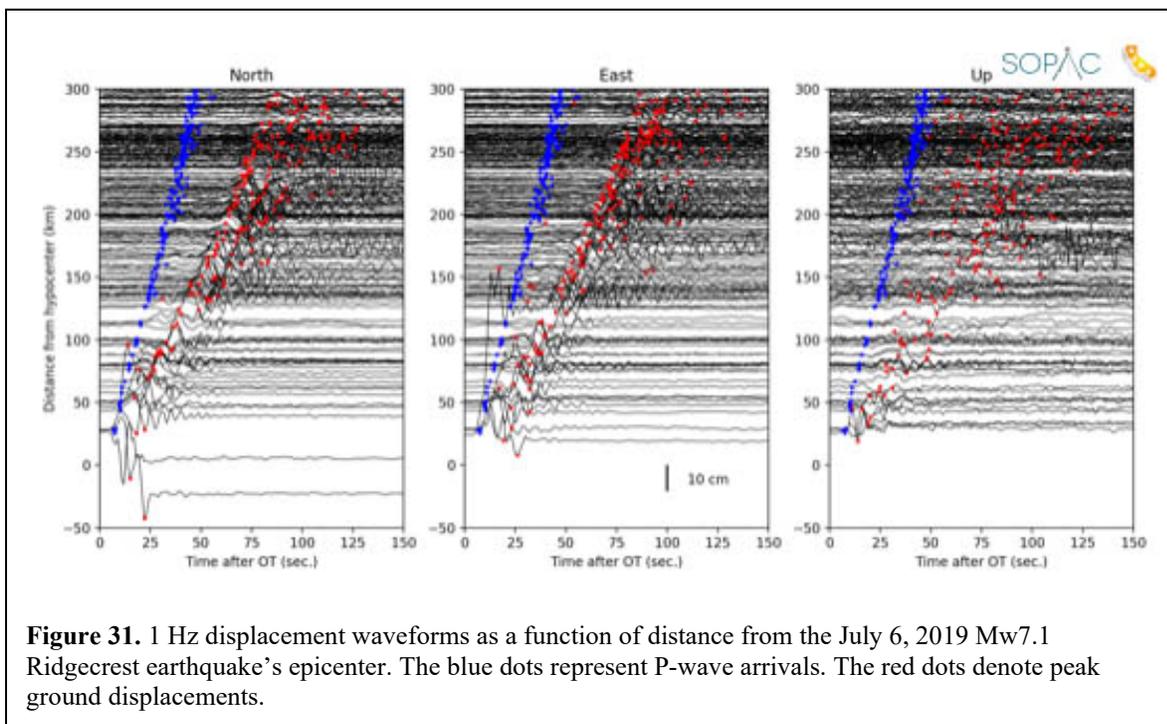
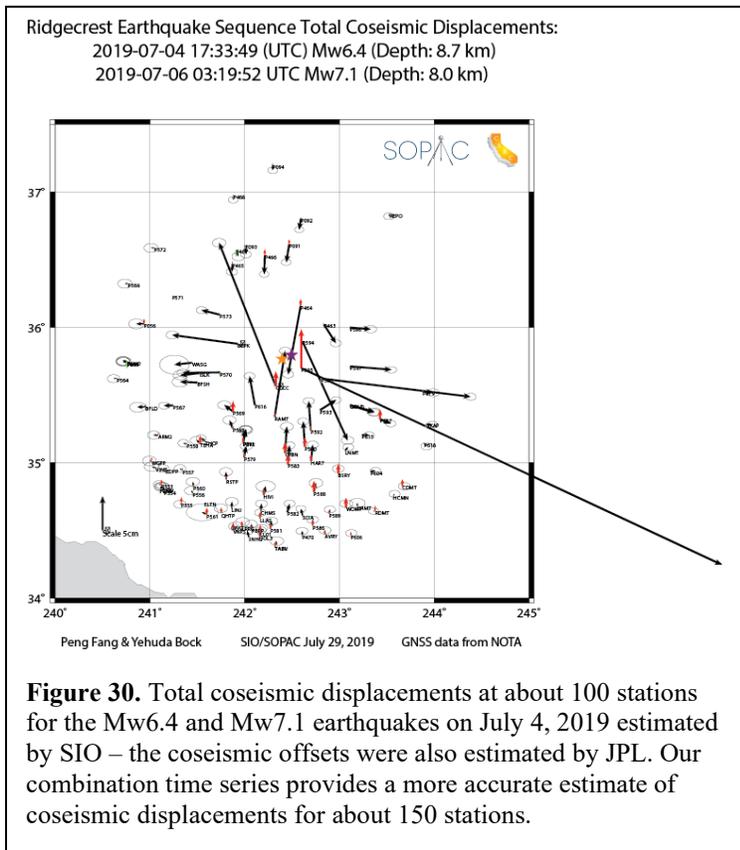
**Figure 28.** Screen shot of the MEaSUREs main web page hosted under the SOPAC web pages.

MGviz has been approved by JPL as open source and is available for download in the NASA Advanced Multi-Mission Operations System repository (<https://github.com/NASA-AMMOS>). It is now installed on a server at SOPAC. The GPS Explorer portal continues to provide the interactive interface for the administrator time series functions (sections 5 and 6).



### 10.3 Events Page

**Note: We are in the process of creating event pages.** For example, we responded to the July 2019 Mw6.2 and Mw7.1 earthquakes near Ridgecrest, California by estimating coseismic offsets (Figure 30) and subsequent postseismic deformation. In this case, we split the 24-hour period into pre- and post-earthquake data. Initially, we thought that about 100 stations had significant permanent coseismic offsets (Figure 26). Further, we determined that more than 50 additional stations were affected extending throughout the Los Angeles basin. Furthermore, for this L1C ESDR we estimated and archived the coseismic (dynamic and static) motions of the event itself (Figure 31). We created an event page for this earthquake sequence (<http://sopac-csre.ucsd.edu/index.php/ridgecrestjuly2019/>).



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## Appendix

### A1. Analyz\_tseri options

See [https://qoca.jpl.nasa.gov/advclass/tsa\\_intro.html](https://qoca.jpl.nasa.gov/advclass/tsa_intro.html) for explanation of this driver parameters

#### A1.1 Analyz\_tseri driver file (example)

```
=====
*      << key word-controlled driving file format >>          *
* symbol ":" must exist in command lines as index pointer      *
* any non-blank character at first column means comment line  *
* empty after ":" means comment line too, but line appears in *
=====
clean_template_singleHost.drv (cleaned time series)
----- part 1 -- general i/o information
apriori value file:          APRIORI_FILE
input file:                  TYPE_data_PROJECT.SEQ.list
sit_list file:               SITE_LIST
est_parameter file:         PARAM_FILE
output file:                 reg_PROJECT.MODE.SEQ.out 2
residual file:              reg_PROJECT.MODE.SEQ.resi
res_option:                  RES_OPTION
omitted_span file:         OMITSPAN_FILE
specific term_out file:     reg_PROJECT.MODE.SEQ.mdl
specific term_option:      SPEC_TERM_OPT
resi_file2:                 reg_both_PROJECT.MODE.SEQ.resi
res2_option:                 RES2_OPTION
mdl2_out:                   reg_both_PROJECT.MODE.SEQ.mdl
mdl2_option:                MDL2_OPTION
enu_correlation usage :    yes
color_noise analysis model : 2
jump_day removal :         no
adjust_allsite option :    yes
online_netformat :         yes
cutoff criterion: unit: year, give a numerical number, for example
    2.5 means 2.5 years. If the data span of this site is less than 2.5
years,
    this site will be neglected.
    Such a criterion is necessary to avoid weak site, in particular for
velocity and seasonal
    term estimates.
cutoff criterion:          0.5
span and sigma factor to estimate jump apr value: unit: year, real value.
    This is one-side span. The analyze_tseri program will check if there
are
    effective jump parameters. If the answer is yes, the program will use
the data
    within the span around the jump epoch to estimate the apriori value of
the jump
    parameter. Then reset the apriori value of the jump parameter using
the estimated
```

value and reset the jump parameter constraint using the formal  $\sigma \times \text{factor}$  value.

The default span value is 0.1 year. The default sigma factor is 0.2 (20%).

```
span and sigma factor to est jump apr (est_jump_span) : 0.5 20
weak_obs (big sigma) criteria :      40.0 40.0 80.0
outlier (big o-c) criteria mm :      OC_OUTLIER_FILE
very bad_obs criteria mm :          BAD_OBS_OUTLIER_FILE
t_interval:                          1990.0 2099.0
minimum interval for parameter (t_est) : 0.587 0.934 0.550
end:
```

----- part 2 -- apriori information

### A.1.2 Residual output options

If the option is empty, that means output original time series and hence the residual file is ignored.

The option is a bit map integer.

if bit(1) = 1 (number 1): the bias term is removed in residuals

if bit(2) = 1 (number 2): the secular motion is removed in residuals

if bit(3) = 1 (number 4): the annual terms are removed in residuals

if bit(4) = 1 (number 8): the semi-annual terms are removed in residuals

if bit(5) = 1 (number 16): the co-seismic jump terms are removed in residuals

if bit(6) = 1 (number 32): the user defined harmonic terms are removed in residuals

if bit(7) = 1 (number 64): the Spline function terms are removed in residuals

if bit(8) = 1 (number 128): the global quadratic terms are removed in residuals

if bit(9) = 1 (number 256): the global cubic terms are removed in residuals

if bit(10) = 1 (number 512): the modulation terms are removed in residuals

if bit(11) = 1 (number 1024): the postseismic decay terms are removed in residuals

if bit(12) = 1 (number 2048): the local polynomial terms are removed in residuals

if bit(13) = 1 (number 4096): the non-co-seismic jump terms are removed in residuals

For example, if the `res_option = 29`, that means the bias, jump, annual and semi-annual terms are removed. The residuals contain the other terms, including velocity (secular motion) term.

### A.1.3 Model term output options

specific term output file: output time series with specified terms.

specific term\_option: option to select the specific terms.

If the option is empty, that means output nothing.

The option is a bit map integer.

if bit(1) = 1 (number 1): the bias term is included in the output terms.

if bit(2) = 1 (number 2): the secular motion is included in the output terms.

if bit(3) = 1 (number 4): the annual terms are included in the output terms.

if bit(4) = 1 (number 8): the semi-annual terms are included in the output terms.

if bit(5) = 1 (number 16): the co-seismic jump terms are included in the output terms.  
 if bit(6) = 1 (number 32): the user defined harmonic terms are included in the output terms.  
 if bit(7) = 1 (number 64): the Spline function terms are included in the output terms.  
 if bit(8) = 1 (number 128): the global quadratic terms are included in the output terms.  
 if bit(9) = 1 (number 256): the global cubic terms are included in the output terms.  
 if bit(10) = 1 (number 512): the modulation terms are included in the output terms.  
 if bit(11) = 1 (number 1024): the postseismic decay terms are included in the output terms.  
 if bit(12) = 1 (number 2048): the local polynomial terms are included in the output terms.  
 if bit(13) = 1 (number 4096): the non-co-seismic jump terms are included in the output terms.  
 For example, if the `res_option = 29`, that means the bias, jump, annual and semi-annual terms are included in the specific output file.

## A.2 PCA Input file (example)

```
=====
*      << key word controlled driving file format >>      *
* symbol ":" must exist in command lines as index pointer      *
* any non-blank character at first column means comment line      *
* empty after ":" means comment line too, but line appears in out file *
=====
```

```
c----- part 1 -- general i/o information
job-type:                regional filtering
decomposition method:    PCA
apriori value file:      itr2008.net
input site list file(site_list):  pca_trans.site
input qob list file(in_list):    pca_data_jplATS.list
output file:             pca_jplATS.out
component file:          pca_jplATS.cpt
regional filtered time series file:  pca_jplATS.res
spatial eigenvector file:    pca_jplATS.seign
network range (sit_range, degree): 200.0 260.1 31.0 80.5
solution span (soln_span):    1990.0 2020.0
fill_gap option:          yes
adj_6par option:         no
outlier_sigma criterion (enu, mm): 50.0 50.0 100.0
outlier_value criterion (enu, mm): 100.0 100.0 300.0
minimum data percentage (cut_p): 10.0
minimum station percentage (cut_t): 3.0
reference frame:          WGS84
reference coordinate, rtime: geodetic 2005.000
end:
exit:
```

A Principal Component Analysis (PCA) filter is applied to the cleaned time series. The PCA driver file settings are as follows and include additional outlier criteria.

network range (longitude, latitude, decimal degrees): 200.0 260.1 31.0 80.5  
 outlier\_sigma criteria (enu, mm): 50.0 50.0 100.0  
 outlier\_value criteria (enu, mm): 100.0 100.0 300.0  
 minimum data percentage (cut\_p): 10.0  
 minimum station percentage (cut\_t): 3.0  
 reference frame: WGS84  
 reference coordinate, rtime: geodetic 2014.006.

### A.3 Weighted Mean of JPL and SIO solutions

Start with the JPL & SIO XYZ files: Raw\_M1,Raw\_M2 (section

[ftp://garner.ucsd.edu/pub/timeseries/measures/ats/WesternNorthAmerica/WNAM\\_Raw\\_M\\_TrendNeuTimeSeries\\_jpl\\_20210528.tar](ftp://garner.ucsd.edu/pub/timeseries/measures/ats/WesternNorthAmerica/WNAM_Raw_M_TrendNeuTimeSeries_jpl_20210528.tar)

[ftp://garner.ucsd.edu/pub/timeseries/measures/ats/WesternNorthAmerica/WNAM\\_Raw\\_TrendXYZTimeSeries\\_sopac\\_20210601.tar](ftp://garner.ucsd.edu/pub/timeseries/measures/ats/WesternNorthAmerica/WNAM_Raw_TrendXYZTimeSeries_sopac_20210601.tar)

Given (Epoch by Epoch):

$$A_1 = \begin{bmatrix} X_1 \\ Y_1 \\ Z_1 \end{bmatrix}; (X \text{ sig}; Y \text{ sig}; Z \text{ sig}; \text{CorrXY}; \text{CorrXZ}; \text{CorrYZ})_1$$

$$A_2 = \begin{bmatrix} X_2 \\ Y_2 \\ Z_2 \end{bmatrix}; (X \text{ sig}; Y \text{ sig}; Z \text{ sig}; \text{CorrXY}; \text{CorrXZ}; \text{CorrYZ})_2$$

Form covariance matrix:

$$C_1 = \begin{bmatrix} (X \text{ sig})^2 & (X \text{ sig})(Y \text{ sig})\text{CorrXY} & (X \text{ sig})(Z \text{ sig})\text{CorrXZ} \\ (X \text{ sig})(Y \text{ sig})\text{CorrXY} & (Y \text{ sig})^2 & (Y \text{ sig})(Z \text{ sig})\text{CorrYZ} \\ (X \text{ sig})(Z \text{ sig})\text{CorrXZ} & (Y \text{ sig})(Z \text{ sig})\text{CorrYZ} & (Z \text{ sig})^2 \end{bmatrix}_1$$

$$C_2 = \begin{bmatrix} (X \text{ sig})^2 & (X \text{ sig})(Y \text{ sig})\text{CorrXY} & (X \text{ sig})(Z \text{ sig})\text{CorrXZ} \\ (X \text{ sig})(Y \text{ sig})\text{CorrXY} & (Y \text{ sig})^2 & (Y \text{ sig})(Z \text{ sig})\text{CorrYZ} \\ (X \text{ sig})(Z \text{ sig})\text{CorrXZ} & (Y \text{ sig})(Z \text{ sig})\text{CorrYZ} & (Z \text{ sig})^2 \end{bmatrix}_2$$

Align epochs between the JPL and SIO values

If an epoch missing both JPL and SIO, skip

If only JPL or SIO, use the one value and skip mean computation

Observation equations:

$$A_1 = M + v_1$$

$$A_2 = M + v_2$$

$$\begin{bmatrix} A_1 \\ A_2 \end{bmatrix} = \begin{bmatrix} I \\ I \end{bmatrix} M + \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$

$$P_1 = C_1^{-1}; P_2 = C_2^{-1}$$

Weighted least-squares estimate:

$$\hat{M} = \left( \begin{bmatrix} I & I \end{bmatrix} \begin{bmatrix} P_1 & 0 \\ 0 & P_2 \end{bmatrix} \begin{bmatrix} I \\ I \end{bmatrix} \right)^{-1} \begin{bmatrix} I & I \end{bmatrix} \begin{bmatrix} P_1 & 0 \\ 0 & P_2 \end{bmatrix} \begin{bmatrix} A_1 \\ A_2 \end{bmatrix}; I = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}$$

$$\hat{M} = [P_1 + P_2]^{-1} [P_1 A_1 + P_2 A_2]$$

$$C_{\hat{M}} = \hat{\sigma}^2 [P_1 + P_2]^{-1}; \hat{\sigma}^2 = \hat{v}^T \begin{bmatrix} P_1 & 0 \\ 0 & P_2 \end{bmatrix} \hat{v}; \hat{v} = \begin{bmatrix} A_1 - \hat{M} \\ A_2 - \hat{M} \end{bmatrix} = \begin{bmatrix} A_{X1} - \hat{M}_X \\ A_{Y1} - \hat{M}_Y \\ A_{Z1} - \hat{M}_Z \\ A_{X2} - \hat{M}_X \\ A_{Y2} - \hat{M}_Y \\ A_{Z2} - \hat{M}_Z \end{bmatrix} \dots$$

Since there are only one degree of freedom in the computation of  $\hat{\sigma}^2$  and none in the case of only a JPL or SIO solution, we do not scale the covariance matrix. Also,  $\hat{v}$  may have a zero value if the two solutions may be identical. Therefore, we only use  $\hat{\sigma}^2$  as a diagnostic. If it is much greater than 1, it may point to an outlier in one of the solutions that could be the basis for further investigation.

This is now Raw\_Mc:

$$\hat{M} = \begin{bmatrix} X_C \\ Y_C \\ Z_C \end{bmatrix}; \text{combined XYZ values}$$

Convert  $C_{\hat{M}}$  to  $Coor_{\hat{M}}$

$$C_{\hat{M}} = \hat{\sigma}^2 \begin{bmatrix} (Xsig)^2 & (XY sig) & (XZ sig) \\ (XY sig) & (Ysig)^2 & (YZ sig) \\ (XZ sig) & (YZ sig) & (Zsig)^2 \end{bmatrix}_c$$

$$Corr_{\hat{M}} = \begin{bmatrix} 1 & \frac{(XY \text{ sig})}{(Xsig)(Ysig)} & \frac{(XZ \text{ sig})}{(Xsig)(Zsig)} \\ \frac{(XY \text{ sig})}{(Xsig)(Ysig)} & 1 & \frac{(YZ \text{ sig})}{(Ysig)(Zsig)} \\ \frac{(XZ \text{ sig})}{(Xsig)(Zsig)} & \frac{(YZ \text{ sig})}{(Ysig)(Zsig)} & 1 \end{bmatrix} = \begin{bmatrix} 1 & CorrXY & CorrXZ \\ CorrXY & 1 & CorrYZ \\ CorrXZ & CorrYZ & 1 \end{bmatrix}$$

The combined (c) data points then are output as:

$(Dec \ Yr; \ Yr; \ DayOfYr; \ X; \ Y; \ Z; \ X \ \text{sig}; \ Y \ \text{sig}; \ Z \ \text{sig}; \ CorrXY; \ CorrXZ; \ CorrYZ)_c$

Add  $\hat{\sigma}^2$  into time series:

$(Dec \ Yr; \ Yr; \ DayOfYr; \ X; \ Y; \ Z; \ X \ \text{sig}; \ Y \ \text{sig}; \ Z \ \text{sig}; \ CorrXY; \ CorrXZ; \ CorrYZ; \ \hat{\sigma}^2)_c$

Convert to N,E,U at each epoch using first mean value and WGS84 ellipsoid

$$\begin{bmatrix} \Delta N_i(t_i) \\ \Delta E_i(t_i) \\ \Delta U_i(t_i) \end{bmatrix} = \begin{bmatrix} -\sin\phi\cos\lambda & -\sin\lambda\sin\phi & \cos\phi \\ -\sin\lambda & \cos\lambda & 0 \\ \cos\lambda\cos\phi & \cos\phi\sin\lambda & \sin\phi \end{bmatrix}_{t_0} \left\{ \begin{bmatrix} X_i(t_i) \\ Y_i(t_i) \\ Z_i(t_i) \end{bmatrix} - \begin{bmatrix} X_{t_0} \\ Y_{t_0} \\ Z_{t_0} \end{bmatrix} \right\}$$

Run weighted mean time series through ATS, run post-ATS to created new combination tar files.